

Simulations of a Miniaturized Cylindrical Hall Thruster

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Abstract—A miniaturized cylindrical Hall thruster (CHT) is studied using a 2-D hybrid model. The simulation results are compared with experimental results for 100-W laboratory CHT. The channel of this thruster has a short coaxial part and a longer cylindrical region with a larger volume-to-surface ratio to reduce erosion. The 2-D model combines a fluid description of the electrons (continuity and momentum equations) and a particle description of the ions and the neutral atoms. The simulations confirm that the ionization takes place in the annular part of the channel, while the unusually high propellant utilization efficiency is found to be due to doubly charged ions.

Index Terms—Cylindrical Hall thruster (CHT), simulations.

NOMENCLATURE

B	Magnetic field magnitude.
e	Electron charge constant.
I_{back} and I_{front}	Back and front coil currents, respectively.
I_d and I_i	Discharge and ion currents, respectively.
k_B	Bohm fitting parameter.
m_a	Xenon anode mass flow.
m_e and M	Electron and neutral atom masses, respectively.
$n, n_0, n_e,$ and n_i	Plasma, reference, electron, and ion densities, respectively.
N	Neutral gas density.
S	Ionization source term.
T	Thrust.
T_e	Electron temperature.
U	Fitting parameter (sheath potential).
V	Electric potential.
V_d	Discharge voltage.
W	Electron–wall effective energy loss coefficient.
x and r	Axial and radial coordinates, respectively.
Xe^+ and Xe^{2+}	Singly and doubly charged ions, respectively.
α_ε	Adjustable parameter.
β	Boltzmann factor.

ε	Electron mean energy.
Γ_e and Γ_i	Electron and ion fluxes, respectively.
κ	Inelastic effective energy loss coefficient.
$\bar{\mu}, \mu_{//},$ and μ_{\perp}	Electron mobility tensor, parallel electron mobility, and perpendicular electron mobility, respectively.
ν_B	Equivalent Bohm collision frequency.
ν_m	Electron–atom momentum transfer frequency.
$\eta, \eta_c,$ and η_u	Anode, current utilization, and propellant utilization efficiencies, respectively.
ω_c	Cyclotron pulsation.
Ω	Hall parameter.

I. INTRODUCTION

A SCALE-DOWN of Hall effect thrusters—HETs—operating at a lower electric power is suitable for low-mass spacecraft or multiple microspacecraft flying in constellations for scientific missions [1]. The reduction of electric power implies a decrease in the discharge current. The consequence is that a low neutral mass flow must be injected. To maintain a high propellant utilization efficiency (which means a large ionization of the injected mass flow) in a shorter channel length, the magnetic field must be increased. The magnetic saturation of the circuit near the inner pole induces challenges to reach an optimal magnetic field magnitude. Moreover, because there is no room for an inner coil, a scale-down of the thruster size leads also to some difficulty to achieve a desired magnetic field shape. The magnetic field in the exhaust region cannot be radial, leading to large ion losses and inner wall erosion. Low-power HETs, based on conventional annular channel, operating in the range of 100–300 W offer low anode efficiency η [2].

Another concept of electromagnetic thruster based on axial electric field and radial magnetic field as in a HET has been proposed a few years ago. This concept named cylindrical Hall thruster (CHT) [3] features a channel with a short annular region and a longer cylindrical region as in Fig. 1. The xenon mass flow is injected through the anode, and the ceramics of the channel are made up of boron nitride as in conventional HETs. Two coils (a front and a back one) are connected to a separate power supply. A cusp magnetic field shape is obtained with counterdirected coil currents, as shown in Fig. 1. Compared to the conventional annular geometry, the CHT offers a larger volume-to-surface ratio and, therefore, potentially smaller ion losses and wall erosion of the inner part [3], [4]. Variants of the CHT with and without a short annular channel were

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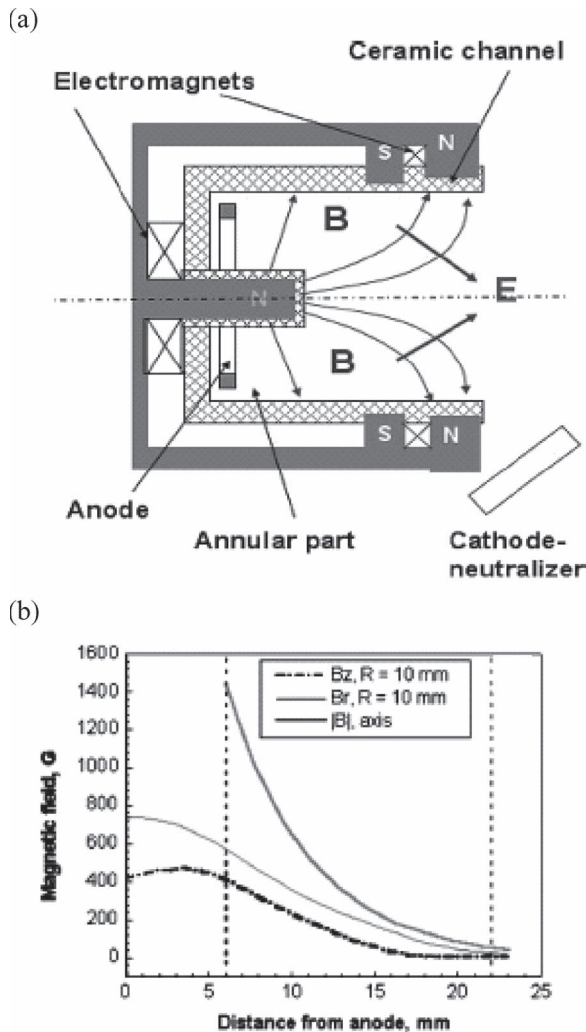


Fig. 1. (a) Schematic of the CHT (from [3]). (b) Magnetic field profiles in the CHT ($I_{\text{back}} = 2.5$ A and $I_{\text{front}} = -1$ A). The dashed lines at $x = 6$ and 22 mm show the edge of the annular channel part and the thruster exit, respectively ([4]).

proposed and developed [3]–[6]. The short annular channel is used to maintain high propellant utilization efficiency in the CHT [3], [4]. On the other hand, the absence of the annular channel may be advantageous with respect to the thruster lifetime [5], [6].

The miniaturized CHT of 2.6-cm diameter (called micro-CHT in the rest of this paper) was developed and characterized at the Princeton Plasma Physics Laboratory (PPPL). For this micro-CHT, comprehensive measurements of performance, plume characteristics, including ion angular distribution and ion energy distribution function, and plasma properties of the thruster discharge are described elsewhere [4], [7]–[10]. In parallel to the experimental studies, theoretical work has been carried out in order to understand the electron cross-field transport in such complex magnetic field topology [9], [10].

The main conclusions of these experimental and theoretical studies can be summarized as follows.

- 1) The propellant utilization (defined as the ratio of ion current considering singly charged ions to the propellant mass flow expressed in units of electric current) in the

micro-CHT is higher than in a conventional annular HET of same diameter. Moreover, the propellant utilization in the micro-CHT is higher than one, and a significant fraction of doubly charged ions seems to be present [8], [10].

- 2) The performance of the micro-CHT is comparable with that of the state-of-the-art conventional annular Hall thrusters of similar power levels [4].
- 3) The plasma density is nonuniform in the radial direction, with the peak being at the thruster axis. The potential drop is concentrated mainly in the cylindrical part of the channel and in the plume. The ion bombardment on the ceramic walls should be reduced in comparison with annular HET [7]. The diamagnetic force is assumed to play an important role in the electron confinement [9].
- 4) The ion beam divergence, defined as the angle which contains 90% of the ion current, is large 70° – 80° (compared to 45° for standard HETs) which, of course, leads to a thrust reduction in the axial direction. In the most recent experiments [8], an important 20%–30% plume narrowing leading to substantial 50%–60% increase of the thruster anode efficiency at 100–200 W has been observed. These improvements were achieved by increasing the discharge current over and above what is normally required for sustaining the steady-state discharge.
- 5) Bohm-type anomalous diffusion of the electron transport with a collision frequency ν_B on the order of the Bohm value ($\nu_B \sim \omega_c/16 - \omega_c$ is the cyclotron pulsation) matches the measured experimental current [9], [10].

A 2-D model has been developed in the context of conventional HETs [11] and extended to double-stage HET [12]. In this paper, we use the full 2-D model to study the micro-CHT working. This paper is organized as follows. We describe the model in Section II, the results are detailed and commented in Section III, and we finally end this paper with a conclusion in Section IV.

II. DESCRIPTION OF THE MODEL

In the 2-D hybrid model, the treatment of the heavy species (singly charged ions Xe^+ , doubly charged ions Xe^{2+} , and neutrals) is based on particle tracing as done in PIC simulation (see Section II-A). The electron transport is described with fluid equations, and the electric potential profile in two dimensions (without assuming a Boltzmann relation along the magnetic lines) is calculated from a current conservation equation forcing quasi-neutrality (see Section II-B). We end this section (see Section II-C) with the procedure used to fit the anomalous cross-field electron conductivity and the electron–wall energy losses by comparisons between calculations and experimental results.

A. Ion and Neutral Transport

The motion of heavy particles Xe , Xe^+ , and Xe^{2+} is solved in two dimensions in space and three dimensions in velocity.

The computational domain assumes a cylindrical symmetry. The domain goes from the thruster centerline to 6.0 cm in the radial direction r and from the anode to 4.5 cm in the axial direction x . The domain contains the channel of the micro-CHT (annular and cylindrical regions) and the cathode. The cathode is positioned at $r = 5.4$ cm and $x = 3.5$ cm. We typically use 60 cells in the x -direction and 80 cells in the r -direction. The neutrals are injected in the anode plane, assuming a Maxwellian distribution of the flux in the axial direction for a given temperature equal to 300 K. We also account for the background neutral atoms due to the background pressure of the experimental facility by injecting an additional neutral flux at the thermal velocity (temperature of 300 K) from the boundaries of the computational domain. The mass flow of neutral atoms through the cathode with a mass flow of 0.2 mg/s has also been included in some simulations (see Section III-B). The effect of the neutral atoms flowing through the cathode orifice has been considered assuming that the temperatures of neutral atoms are in equilibrium with the walls (a rough estimation gives a temperature that is approximately 1200 K [13]). Neutrals colliding with the walls are reflected back in the domain.

The ion source term is calculated assuming a Maxwellian distribution function for the electrons. The origin of Xe^+ is the ionization of the ground state of xenon, whereas the origin of Xe^{2+} is the direct double ionization of the ground state of xenon and the stepwise ionization of Xe^+ . We neglect the effect of triply charged ions. The ionization threshold for the ground state is 70 eV for xenon. Due to the large Larmor radius, the magnetic field effect on the ions is neglected. The ion trajectories are followed until the xenon ions leave the computational domain or impinge the walls. When ions impact on walls, they are neutralized, and new neutral atoms at the wall temperature (300 K) are reemitted. The angular distribution is assumed semi-isotropic.

B. Electron Transport

The electron fluid transport is described with the continuity, momentum, and energy equations. The equation for the electron conservation is

$$\frac{\partial n_e}{\partial t} + \nabla \cdot \Gamma_e = S \quad (1)$$

where n_e is the electron density, Γ_e is the electron flux, and S is the ionization source term.

The electron momentum equation is written—in the form of drift–diffusion approximation—as

$$\Gamma_e = \bar{\mu} (n_e \nabla V - \nabla(n_e T_e)) \quad (2)$$

where T_e is the electron temperature. We recognize the electric force and the kinetic pressure gradient in the first and second terms of (2), respectively. Due to the magnetic field, the mobility $\bar{\mu}$ is not a scalar but a tensor [14], where the components

parallel and perpendicular to the magnetic field are given by the following relations:

$$\mu_{\parallel} = \frac{e}{m_e \nu_m} \quad (3)$$

$$\mu_{\perp} = \frac{1}{1 + \Omega^2} \mu_{\parallel} = \frac{e \nu_m / m_e}{\nu_m^2 + \omega_c^2} \quad (4)$$

where Ω is the Hall parameter (with $\Omega = \omega_c / \nu_m - \nu_m$ being the electron–neutral momentum collision frequency). For typical conditions, the Ω parameter varies between 10^2 and 10^4 . The perpendicular mobility is therefore lower by orders of magnitude than the parallel one.

Combining (1) and (2) and forcing quasi-neutrality ($n \approx n_i \approx n_e$), the electric potential V is calculated to solve the following:

$$\nabla \cdot \Gamma_e = \nabla \cdot [\bar{\mu} (n \nabla V - \nabla(n T_e))] = \nabla \cdot \Gamma_i \quad (5)$$

In (5), the plasma density n and the ion flux Γ_i are deduced from the ion transport. The aforementioned elliptic equation is solved on the same computational grid as the grid used to transport ion and neutrals. The difficulty in the resolution of (5) comes from the strong anisotropy of the mobility tensor $\bar{\mu}$. An accurate numerical scheme must be used; otherwise, the cross-field transport (in the perpendicular direction) is determined by the numerical errors, not by the physical cross-field transport [15]. Since we consider a Maxwellian distribution function for the electrons, mirror forces are not included in this approach. A description of the mirror force requires separate equations for the electron energy in the direction parallel and perpendicular to the magnetic field lines.

The boundary conditions are zero potential at the cathode and discharge potential at the anode. On the dielectric walls, on the front plane, and on the free-space edge of the computational domain, the electron flux Γ_e is set equal to the ion flux Γ_i .

In order to determine the electron temperature T_e (or the electron mean energy $\varepsilon = 3/2\beta T_e$, where β is the Boltzmann constant), we solve an energy equation

$$\begin{aligned} \frac{\partial(n\varepsilon)}{\partial t} + \frac{5}{3} \nabla \cdot (\Gamma_e \varepsilon) - \frac{10}{9e} \nabla \cdot (\mu n \varepsilon \nabla \varepsilon) \\ = e \Gamma_e \cdot \nabla V - N n \kappa - n W \end{aligned} \quad (6)$$

where N is the neutral gas density. The last two terms in the energy equation represent energy loss by collisions with gas particles and with the walls, respectively, where κ and W are the effective energy loss coefficients. The inelastic rates between electrons and neutrals are calculated assuming a Maxwellian distribution and a given set of cross sections. The inelastic cross sections (single direct ionization and excitation) come from Puech and Mizzi [16]. The double-direct-ionization cross sections from the xenon ground state come from Wetzel *et al.* [17]. The cross sections for ionization of Xe^+ are taken from Achenbach *et al.* [18]. The boundary conditions are the following: We assume a given electron mean energy of 10 eV on the

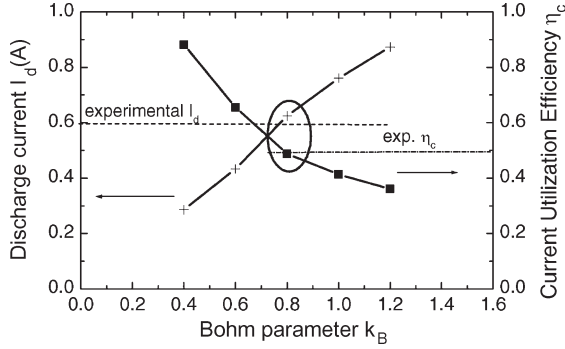


Fig. 2. Calculations of the discharge current I_d and current utilization efficiency η_c for different values of the k_B coefficient. The conditions are the following: a discharge voltage V_d of 250 V, a mass flow of xenon of 0.4 mg/s, and a background pressure of 9 mPa. The experimental values are given in [4].

anode plane, 10 eV in the cathode, and 5 eV in the near plume region. The energy flux to the wall q_w is

$$q_w = \frac{5}{3} \Gamma_e \cdot \varepsilon. \quad (7)$$

C. Cross-Field Electron Mobility and Electron–Wall Energy Losses

As in conventional HETs, the electron cross-field transport is still an open problem in the micro-CHT. A Monte Carlo model of the electron dynamics has been developed in a previous study in order to quantify the mechanism responsible of the electron transport in the direction perpendicular to the magnetic field [9]. The Monte Carlo model accounts for elastic and inelastic collisions with neutrals (assuming a constant neutral density into the computational domain), electron–wall collisions (including secondary electron emission and electron attachment), and Bohm diffusion (through an equivalent collision frequency). The main conclusion of this paper is that the main mechanism which can explain the cross-field transport is the Bohm diffusion $\nu_B \sim \omega_c/16$, with the electron–wall interactions playing a role only on the electron energy losses.

Based on the same idea, in the hybrid model, we treat the electron cross-field transport with a frequency related to a momentum transfer between electrons and neutrals (ν_m —the momentum transfer frequency is assumed constant $k_m = 2.5 \times 10^{-13} \text{ m}^3 \cdot \text{s}^{-1}$) and due to field fluctuations (with an equivalent frequency $\nu_B = k_B \omega_c/16$, where k_B is a fitting parameter)

$$\mu_{\perp} = \frac{e\nu/m_e}{\nu^2 + \omega_c^2} \approx \frac{m_e\nu}{eB^2} = \frac{m_e(\nu_m + \nu_B)}{eB^2}. \quad (8)$$

In order to quantify the k_B parameter, we have calculated the discharge current I_d and the current utilization efficiency η_c defined as I_i/I_d as a function of k_B . These simulation results are compared with experimental results for the discharge voltage of 250 V and the anode xenon gas flow rate of 0.4 mg/s [4], [7], [9], [10]. The simulated values of I_d and η_c give the best agreement with experimental results for $k_B = 0.8$ (see Fig. 2), confirming a k_B parameter that is few times larger than those of conventional HETs [19] ($k_B \sim 0.1$ – 0.2). We

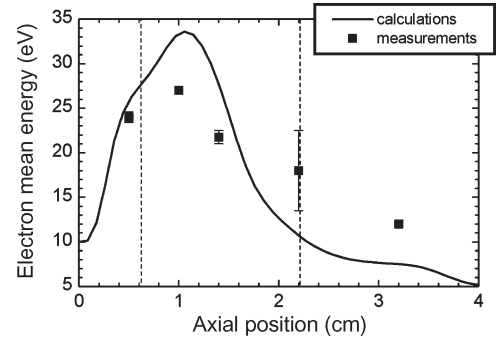


Fig. 3. Calculated and measured [7] profiles of the electron mean energy near the outer wall. The dashed lines at $x = 0.6$ and 2.2 cm represent the edge of the annular channel region and the thruster axis, respectively. The conditions are the same as those in Fig. 2. The vertical bars indicate the uncertainty of the electron mean energy measurements.

remark that the magnetic field reaches 700 G in the annular region, which is three or four times higher than the magnetic field magnitude in the exhaust plane of a conventional HET. The cross-field transport must be increased in the same ratio in order to explain the measured discharge current. We assume that the k_B parameter remains constant when the discharge voltage varies (see Section III).

The fluid model shows that energy losses due to electron–atom collisions are not sufficient to reproduce experimental results. To represent energy losses due to electron–wall interactions, we use in this paper the same empirical energy loss coefficient as in [11]. The energy loss per second per electron is taken as

$$W = \alpha_{\varepsilon} 10^7 \varepsilon \exp\left(-\frac{U}{\varepsilon}\right) \quad (9)$$

where α_{ε} and U are the constant fitting parameters. We have compared the calculated and the measured electron mean energy ($\varepsilon = 3/2\beta T_e$) to fix the α_{ε} and U parameters. Fig. 3 shows an acceptable agreement between the measured and the calculated profile of ε for $\alpha_{\varepsilon} = 0.7$ and $U = 20$ eV (the conditions are the same as those in Fig. 2, and $k_B = 0.8$).

III. RESULTS AND DISCUSSION

We performed calculations for a given set of coil currents $I_{\text{back}} = 2.5$ A, $I_{\text{front}} = -1$ A, for two anode mass flows of 0.4 and 0.6 mg/s; the discharge voltage varies from 200 to 300 V. We present in Section III-A the plasma characteristics for an anode mass flow of 0.4 mg/s and a discharge voltage V_d of 250 V. We also compare simulation results with experimental measurements of electric potential and plasma density. The current–voltage characteristic and the propellant utilization efficiency are presented in Section III-B. We then analyze in the same section the origin of a large propellant utilization efficiency in the micro-CHT.

A. Plasma Characteristics

The time-averaged spatial distributions of electric potential, ionization source term, and neutral atom and ion densities for

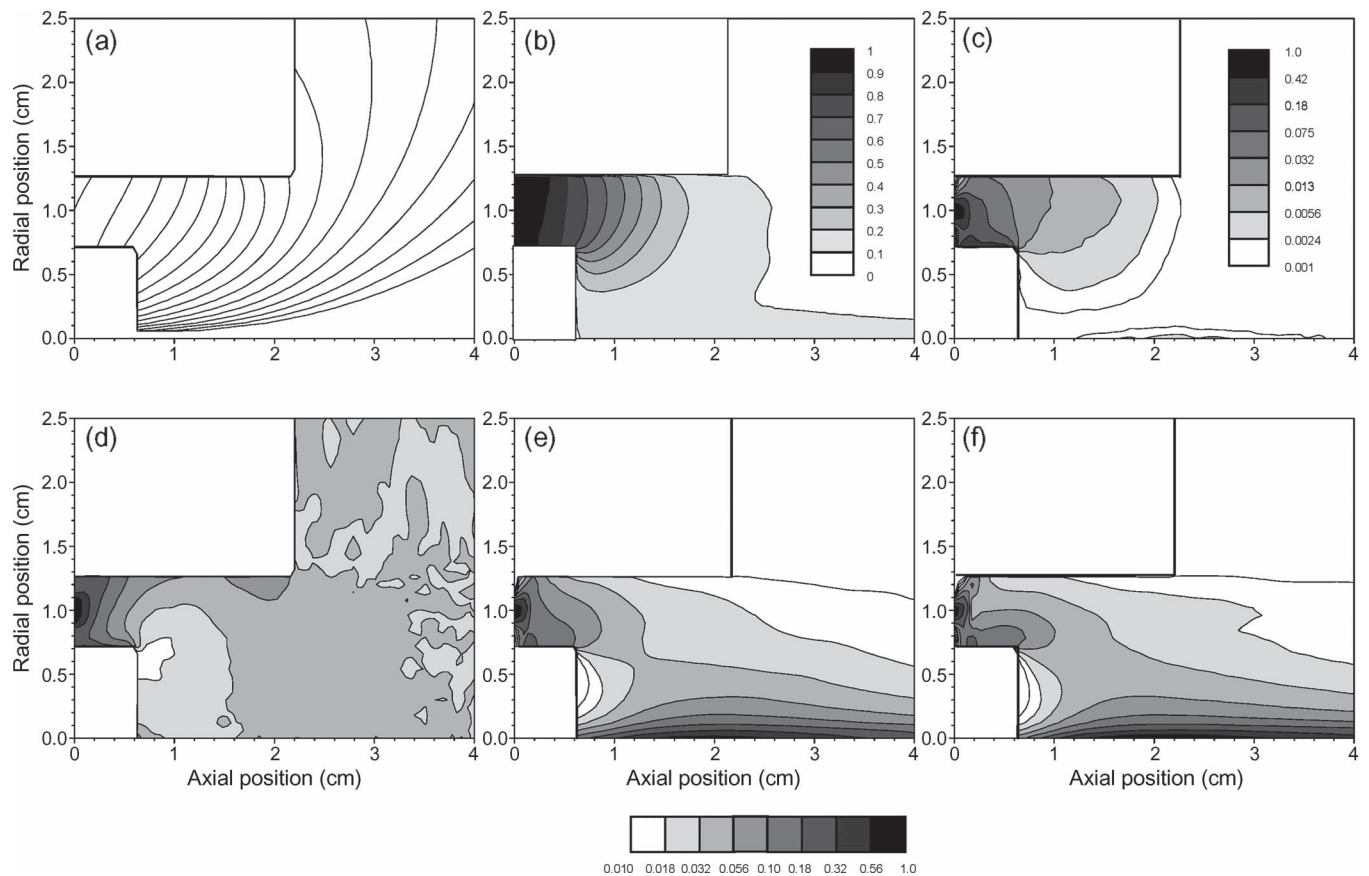


Fig. 4. Plasma characteristics on the subset of the computational domain for a discharge voltage V_d of 250 V, for an anode mass flow of xenon of 0.4 mg/s, and for a background pressure of 9 mPa. (a) Magnetic field lines. (b) Electric potential (max: 250 V). (c) Ionization source term log scale 3 decades (max: $1.6 \times 10^{25} \text{ m}^{-3}\text{s}^{-1}$). (d) Neutral atom density log scale 2 decades (max: $7 \times 10^{19} \text{ m}^{-3}$). (e) Xe^+ density log scale 2 decades (max: 10^{19} m^{-3}). (f) Xe^{2+} density log scale 2 decades (max: $6 \times 10^{17} \text{ m}^{-3}$).

the interior and near field of the micro-CHT configuration are shown in Fig. 4 for $V_d = 250$ V, an anode xenon mass flow of 0.4 mg/s, and a background pressure of 9 mPa. The injection of atoms through the cathode is not included in this section. Fig. 4(a) shows the magnetic field lines. The computational domain is not limited by the magnetic field lines which intercept the cathode, as in previous studies where the electric potential was calculated assuming a Boltzmann relation for the electrons [11], [20], [21]. The electric potential shown in Fig. 4(b) demonstrates that the potential drop is concentrated in the region of high magnetic field which covers the annular and cylindrical parts, with a nonnegligible drop being outside the exit plane. We also see that the electric potential contours do not follow the magnetic field lines inside the coaxial part and outside the micro-CHT channel [compare Fig. 4(a) and (b)]. We observe that the electric potential variation along a magnetic field line which intercepts the magnetic inner pole and the cathode is few tens of volts.

The maximum of ionization is achieved in the annular region, as shown in Fig. 4(c). In this region, the neutral atom density is large [see Fig. 4(d)], the electron energy exceeds 10 eV (as we note in Fig. 3), and the electrons are strongly confined by the strong magnetic field magnitude. The neutral density is maximum in front of the region of atom injection as expected ($\sim 10^{20} \text{ m}^{-3}$) and then strongly decreases due to intense ionization. We note a region of nonnegligible atom density due

to ion recombination near the outer wall of the cylindrical region. The neutral atom density in the outside region is about $2 \times 10^{18} \text{ m}^{-3}$ arising from the background pressure flow. We observe in Fig. 4(e) two peaks of Xe^+ ion density—the first one in the annular zone due to the ionization of the neutral gas (with density being in the range of 10^{19} m^{-3}) and the second one in the region of the axis of symmetry ($\sim 5 \times 10^{18} \text{ m}^{-3}$) due to the convergent ion flux. Although the xenon mass flowing through the anode is relatively low (ten times less than the mass flow injected for 1-kW HETs), the Xe^+ ion density is high due to the small channel cross section and volume of the annular region of the micro-CHT (2 cm^{-3} compared with 50 cm^{-3} of the 9-cm-diameter CHT). A possible effect of Xe^{2+} has been invoked to a possible explanation of the high propellant utilization efficiency of the micro-CHT [4], [10]. We have shown in Fig. 4(f) the profile of Xe^{2+} ion density. We observe that the profile has the same shape with the Xe^+ ion density profile, which indicates that the Xe^{2+} ions are mainly produced by ionization of the singly charged ions. The electron energy is not large enough to produce a substantial fraction of Xe^{2+} ions by direct impact ionization of the xenon atom. The interesting result is that the fraction of doubly charged ions already represents a few percent of the total ion density for an anode mass flow of xenon of 0.4 mg/s. Same calculations for a mass flow of 0.6 mg/s lead to a higher density in the coaxial part with a percentage of doubly charged ions which attains 10% of the total ion density.

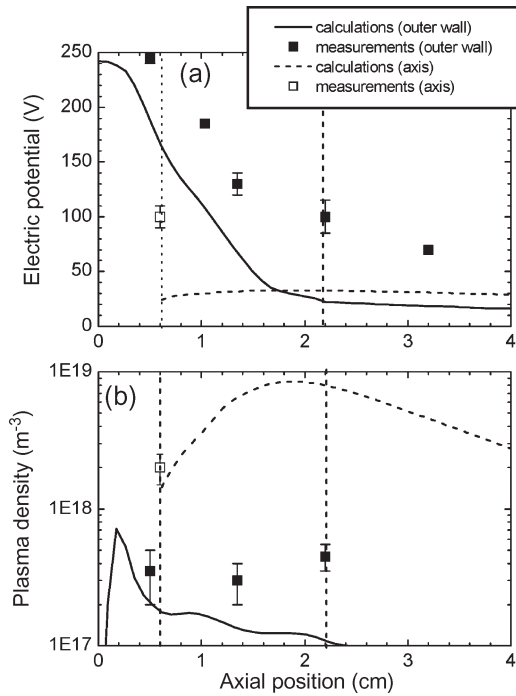


Fig. 5. Comparisons between the calculated and measured profiles [7] of (a) electric potential and (b) plasma density for a discharge voltage V_d of 250 V, a mass flow of xenon of 0.4 mg/s, and a background pressure of 9 mPa. The vertical bars indicate the uncertainty of the measurements.

There are considerable discrepancies between simulated and measured [7] results of the electric potential distribution [Fig. 5(a)]. In the simulations, the voltage potential drop in the annular channel is much larger than in the experiments. In addition, the electric potential at the channel exit is almost four times lower than that measured for the 2.6-cm micro-CHT. We can make two remarks on the possible causes of these discrepancies. The first remark is related to the effect of anomalous transport coefficient on the electric potential profile, as it has been shown in [19] and [21]. We have taken the same anomalous Bohm coefficient in the annular and cylindrical regions, but there is no evidence to do so. A higher Bohm coefficient inside the annular region, representing a larger electron conductivity near the anode, would lead to a smaller potential drop inside this region. The second remark concerns the pressure force (2). We underestimate the electron energy in the region near the exhaust plane (see Fig. 3) by a factor of two, which can maybe explain some differences between the simulated and measured values of electric potential in this region. Again, we use the same parameter to account for the electron energy losses due to electron–wall interactions inside and outside the coaxial part. The boundary condition on the electron energy in the plume may also affect the simulation results.

As observed experimentally, the calculated plasma density near the outer wall is lower than on the thruster axis by more than one order of magnitude [see Fig. 5(b)]. We note some difference beyond the exit plane. The measured plasma density reaches $6 \times 10^{17} \text{ m}^{-3}$, which is five times the calculated plasma density at the same location. It is maybe due to the ionization of neutrals coming from ion recombination. We observe a non-

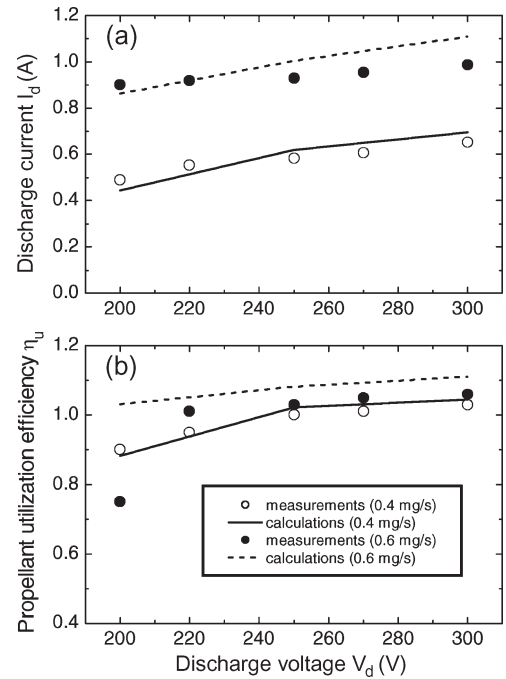


Fig. 6. (a) Current–voltage characteristic for two anode mass flows of xenon. (b) Propellant utilization efficiency versus discharge voltage. The background pressure is 9 mPa. The propellant utilization efficiency does not include the cathode gas flow rate.

negligible neutral density in the cylindrical region near the outer wall [see Fig. 4(d)], but it seems that the ionization of the neutral atoms is still low due to a low electron energy in the channel exit region. Despite the fact that we do not account for the diamagnetic force effect, we do think that the main origin of the discrepancies between the experiments and the calculations are related to the bad estimation of the parameters involved in the fluid description of the electrons (k_B and α_ε in the momentum and energy equations, respectively).

B. Ion Current and Current–Voltage Characteristics

We have shown in Fig. 6(a) the discharge current as a function of the discharge voltage for two anode mass flows of xenon (0.4 and 0.6 mg/s) and for discharge voltages in the range of 200–300 V. The agreement between the measured and calculated currents is reasonable, given that the coil currents are kept constant in all calculations.

A more interesting result is shown in Fig. 6(b), where we have calculated the propellant utilization efficiency η_u in the same conditions as in Fig. 6(a), assuming singly charged ions. We recall that η_u is defined as

$$\eta_u = \frac{I_i M}{e m_a} \quad (10)$$

where I_i is the total ion current, M is the mass of the propellant gas, and m_a is the anode mass flow of xenon. We observe in Fig. 6(b) that η_u is higher than one at high voltage. The possible mechanisms responsible for a large η_u are the presence of doubly charged ions and/or a residual neutral atom mass flow which can result from the neutral background pressure and from the neutral flowing through the cathode. We then have examined

TABLE I
CALCULATIONS OF PROPELLANT UTILIZATION EFFICIENCY η_u FOR DIFFERENT CONDITIONS, A DISCHARGE VOLTAGE V_d OF 250 V,
A MASS FLOW OF XENON OF 0.6 mg/s

CASE	Facility background pressure (mPa)	xenon cathode flow (mg/s)	doubly charged ions	propellant utilization efficiency η_u
1	0	0	No	0.95
2	0	0.2	No	0.95
3	9	0	No	0.97
4	20	0	No	1.01
5	30	0	No	1.19
6	0	0	Yes	1.05

different scenarios in order to understand the origin of the high propellant utilization efficiency in the micro-CHT.

All the simulations in this section fixed the anode mass flow rate to 0.6 mg/s and the discharge voltage to 250 V. A summary of the conditions studied and the calculated propellant utilization efficiency is presented in Table I. Note that, in the simulations, for the sake of simplicity, the angle between the thruster and the cathode is 90° , while in the experiments, this angle is actually 30° . As has been recently studied experimentally ([22]), CASE 1 and CASE 3 confirm that the neutral flow from the cathode does not significantly affect the propellant utilization efficiency. In the experiments, the micro-CHT thruster was characterized at high (9 mPa $\sim 7 \times 10^{-5}$ torr) [23] and low (0.4–0.8 mPa $\sim 3\text{--}6 \times 10^{-6}$ torr) [8], [10], [22] background pressure environments. CASE 3, CASE 4, and CASE 5 represent a similar sensibility study of the background pressure on η_u . We note that, for the high background pressure, the propellant utilization efficiency remains below the calculated values shown in Fig. 6(b) ($\eta_u = 1.05$). The effect of the background pressure is determined by the pressure balance in the exit. To reach $\eta_u = 1.05$, the background pressure must be in the range of 25 mPa, which is on the order of one order of magnitude higher than the experimental study conditions. Finally, in CASE 6, we have introduced Xe^{2+} ions, where we have not observed a large increase in the propellant utilization efficiency. From this study, we can conclude that the Xe^{2+} ions seem to play a larger role on the observed high propellant utilization efficiency in the micro-CHT than the neutrals coming from the background pressure or external cathode.

IV. CONCLUSION

A linear scale-down of Hall thrusters to low power levels requires that the magnitude of the magnetic field is increased as the dimension of the HETs is reduced in order to preserve a high degree of ionization of the neutral flux. This scaling is questionable because there is no room to implement a sophisticated magnetic circuit with inner coils and magnetic screens, which are typically used for larger high-performance Hall thrusters

of medium and high power levels. The optimization of the magnetic field configuration is made difficult leading to large ion wall losses and possible erosion of the thruster channel. The anode efficiency η of conventional HETs remains low. The micro-CHT was designed to improve efficiency by changing the physical geometry as well to promote higher propellant efficiency.

The aim of this paper is to use a 2-D hybrid model in order to answer some questions or confirm some hypotheses concerning thruster operation. We can summarize the main results as follows.

- 1) Plasma instabilities seem to play a big role in the special magnetic field configuration of the micro-CHT. In order to reproduce the measured discharge current, a supplementary equivalent collision frequency on the order of $\nu_B \sim \omega_c/16$ (Bohm formula) must be taken into account in the fluid description of the electron cross-field transport.
- 2) The potential drop begins in the annular region and sharply decreases in the cylindrical part. The electric potential in the plume is few tens of electron volts. We observe two peaks of plasma density—the first one in the annular region and the second one on the thruster axis due to the convergent ion flux. A comparison between the experimental and calculated profiles of electric potential and plasma density shows noticeable differences.
- 3) The calculations show a high level of propellant utilization efficiency. Different scenarios have been proposed to understand the origin of high propellant utilization efficiency. We have seen that the supplementary xenon cathode flow or background pressure does not play a crucial role. The doubly charged ions produced by ionization of Xe^+ highly influence the level of propellant utilization efficiency.

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