



M3D-C¹ simulations of plasma response in ELM-mitigated AUG and DIII-D discharges

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Meeting of the SciDAC Center for Extended MHD Modeling

Savannah, GA

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Acknowledgments

- **DIII-D study**
 - Data analyzed largely by C. Paz-Soldan and is the subject of a forthcoming paper
 - “Equilibrium drives of the low and high field side $n=2$ plasma response and impact on global confinement”
 - To be submitted to *Nuclear Fusion*
 - MARS-F modeling performed by S.R Haskey
 - IPEC modeling performed by N.C. Logan
- **ASDEX-Upgrade data analyzed largely by W. Suttrop**

Introduction

- **External three-dimensional magnetic perturbations have become a principal means of mitigating or suppressing edge-localized modes (ELMs) in tokamaks**
- **Sophisticated magnetohydrodynamics (MHD) modeling is required to understand how the plasma responds to these perturbations**
- **M3D-C¹ is used to model the plasma response in a variety of plasma and magnetic perturbation configurations**
 - Phasing (differential phase angle) between multiple coils
 - Variations in pressure and current profiles
- **Results compared to**
 - Experimental data and observations
 - Numerical results from IPEC and MARS-F

ELMs can be mitigated or suppressed by external 3D magnetic fields

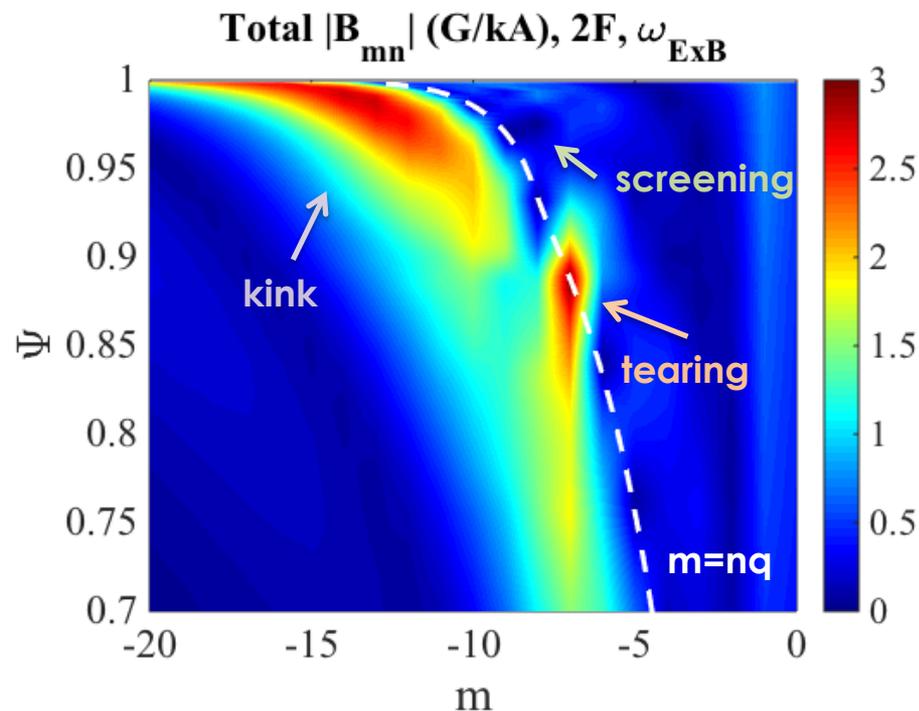
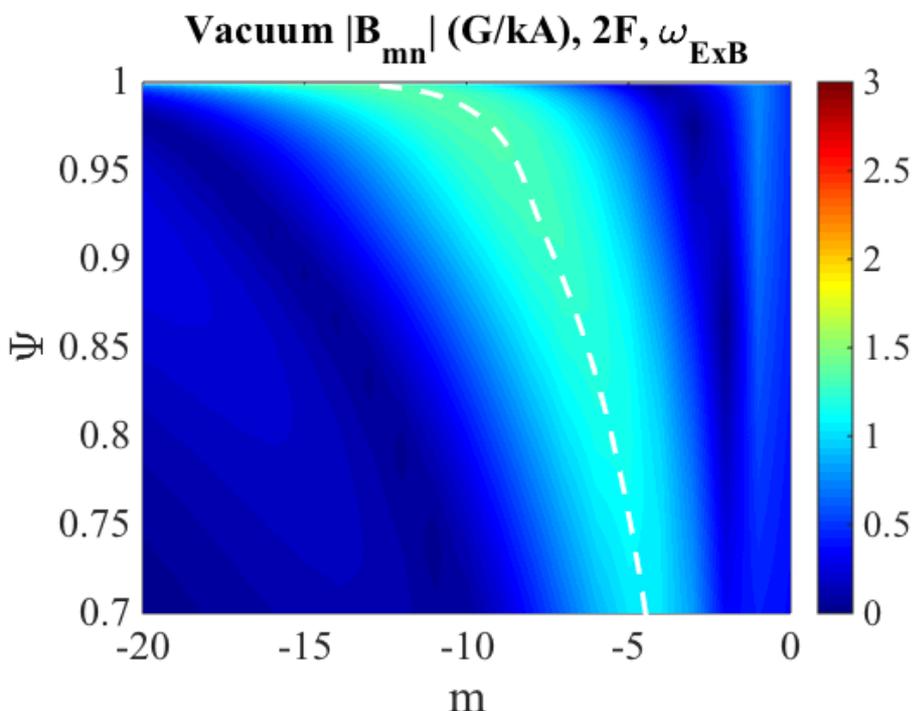
- **DIII-D has demonstrated complete suppression of ELMs using externally-applied 3D magnetic perturbations**
 - Evans, T.E. et al. Nat. Phys. **2**, 419 (2006).
 - Among others
- **Results motivated installation of coils on several machines**
 - ASDEX Upgrade
 - KSTAR
 - MAST
 - NSTX-U
 - ITER (planned)

Theoretical understanding is still incomplete

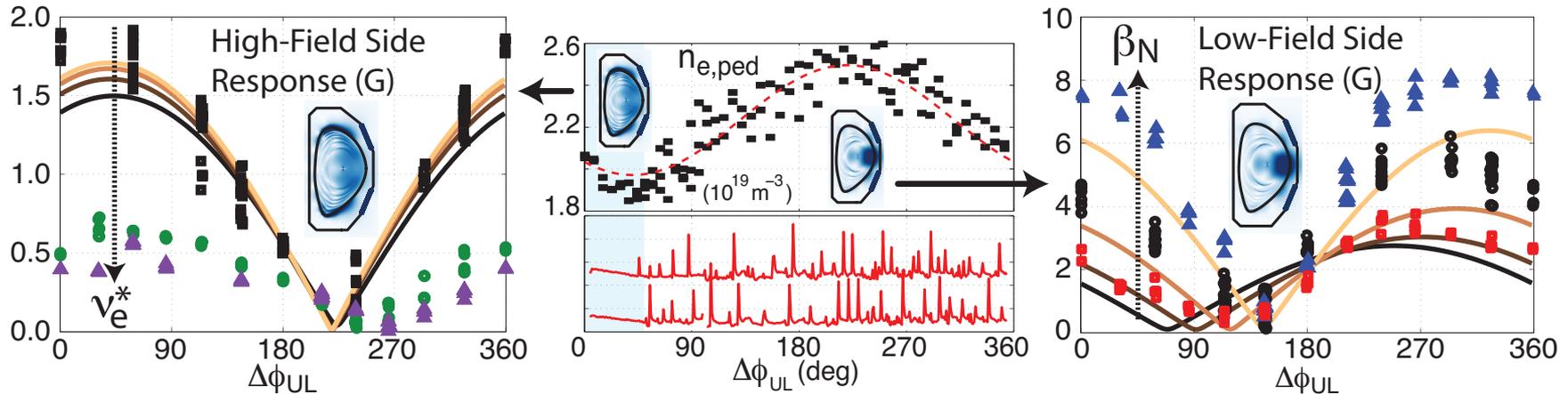
- **Early theoretical work focused on the nature of the applied vacuum field**
 - Resonant perturbations at rational surfaces open islands
 - Overlapping of islands at edge-pedestal boundary produces stochastic fields
 - Increased transport in stochastic layer maintains pedestal height/width below ELM stability thresholds
- **Recent MHD simulations have demonstrated the importance of the plasma response**
 - Ideally, resonant fields are completely shielded by plasma currents
 - Resistively, resonant fields can be enhanced by tearing
 - Non-resonant fields excite kink-like deformations with $m > nq$
 - Kink and tearing structures can couple to each other

Plasma response can greatly alter perturbed magnetic spectrum

- **SURFMN-like field decomposition** $\delta B_r(\psi) = \sum_{m,n} B_{mn}(\psi) \exp [i (m\theta - n\phi)]$
- **Resonant response at rational surfaces ($m=nq$)**
 - Tearing enhances
 - Screening suppresses
- **Kink response amplifies non-resonant fields with $m > nq$**



Ideal and resistive MHD modeling capture some, but not all trends



- **IPEC (solid lines) and MARS-F modeling versus data from magnetic probes (symbols)**
 - Generally captures trends as pressure is varied (far right)
 - Struggles to reproduce trends as current profile is varied (far left)
- **Can extended MHD modeling with M3D-C¹ reproduce or improve these results?**

M3D-C¹ allows for extended MHD simulations of the plasma response to applied 3D fields

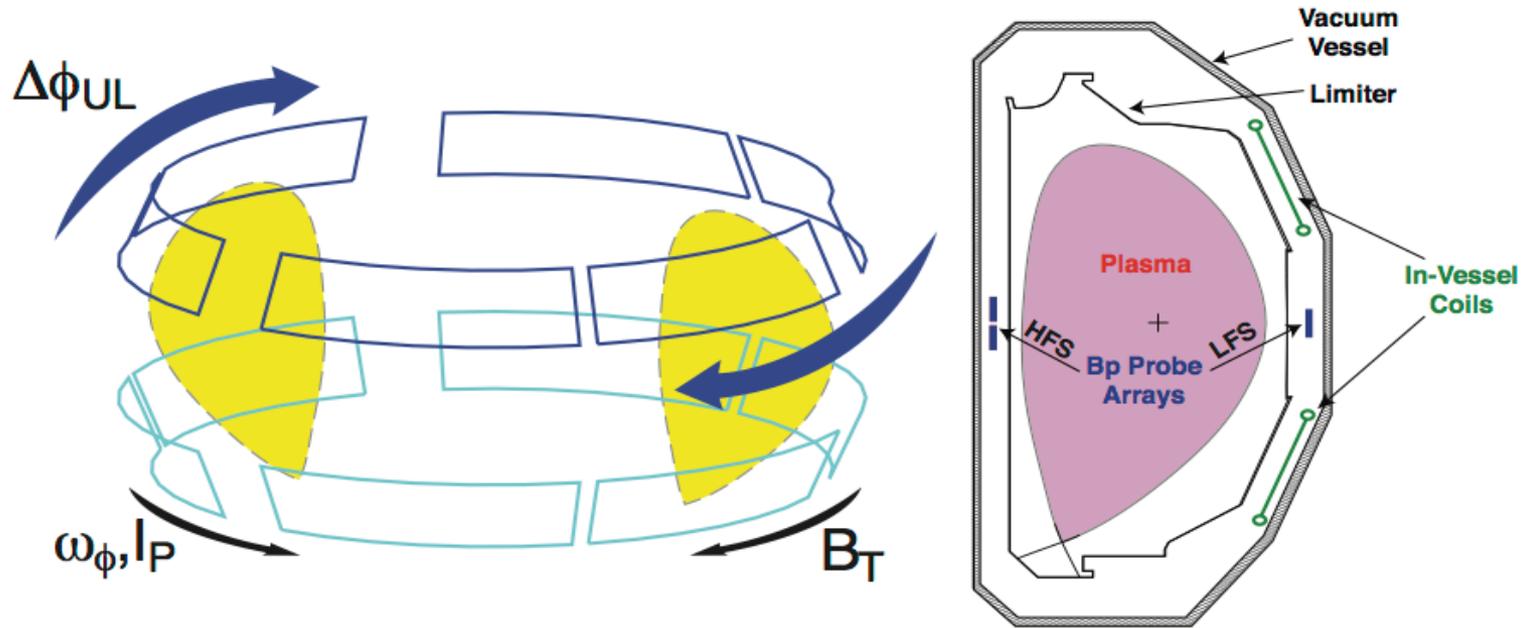
- **M3D-C¹ [1] is a sophisticated extended MHD code**
 - Fully three-dimensional
 - Two-fluid
 - Linear and nonlinear modes
 - EFIT Grad-Shafranov equilibrium recomputed on adaptive mesh with high-order finite element representation
- **Plasma response calculations**
 - Linear (single toroidal mode number)
 - Time-independent
 - Single- and two-fluid
 - Mostly single-fluid here
 - Experimental kinetic & rotation profiles
 - Extended beyond separatrix
 - Resistive wall model

[1] S. C. Jardin, et al., Comput. Sci. Discovery 5, 014002 (2012).

DIII-D Reference Equilibrium

158103.03796

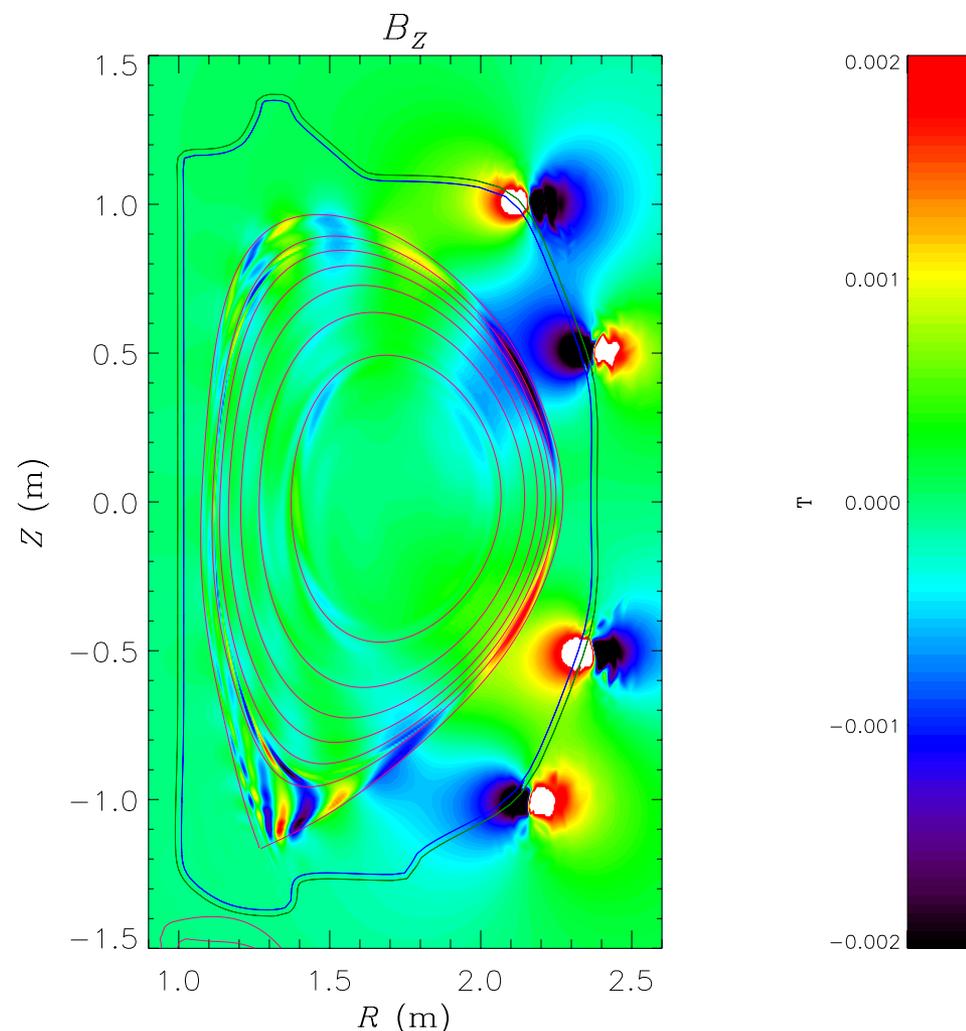
External field coils on DIII-D



- **Three rows of six saddle coils**
 - Two in-vessel rows (I-coils)
 - One external row (C-coils, not pictured)
 - Toroidal mode number of perturbations up to $n=3$
- **For $n=2$ fields, phasing $\Delta\phi_{UL} = \phi_{up} - \phi_{low}$ can be varied between upper and lower coils sets**

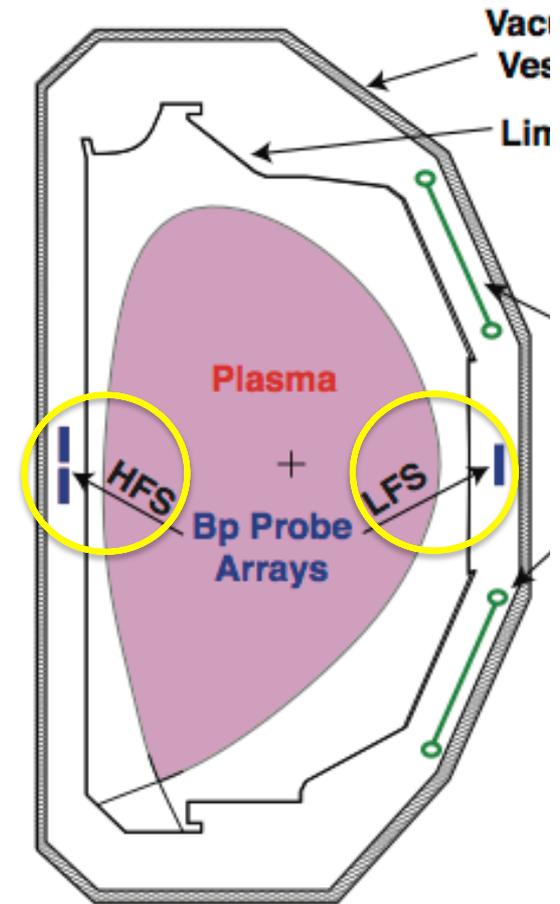
Reference is ITER-similar shape, lower single null plasma

- **Reference equilibrium (shot 158103 at 3796 ms) has**
 - $B_T = 1.93$ T and $I_p = 1.36$ MA
 - $\beta_N = 2.2$
 - $\nu_{e^*} = 0.3$
 - $q_{95} = 4.15$
- **n=2 external 3D field applied with I-coils**
 - Relative phase (phasing) between upper and lower coil changed in piecewise fashion
 - Phase of both coils flipped throughout shot for diagnostic purposes



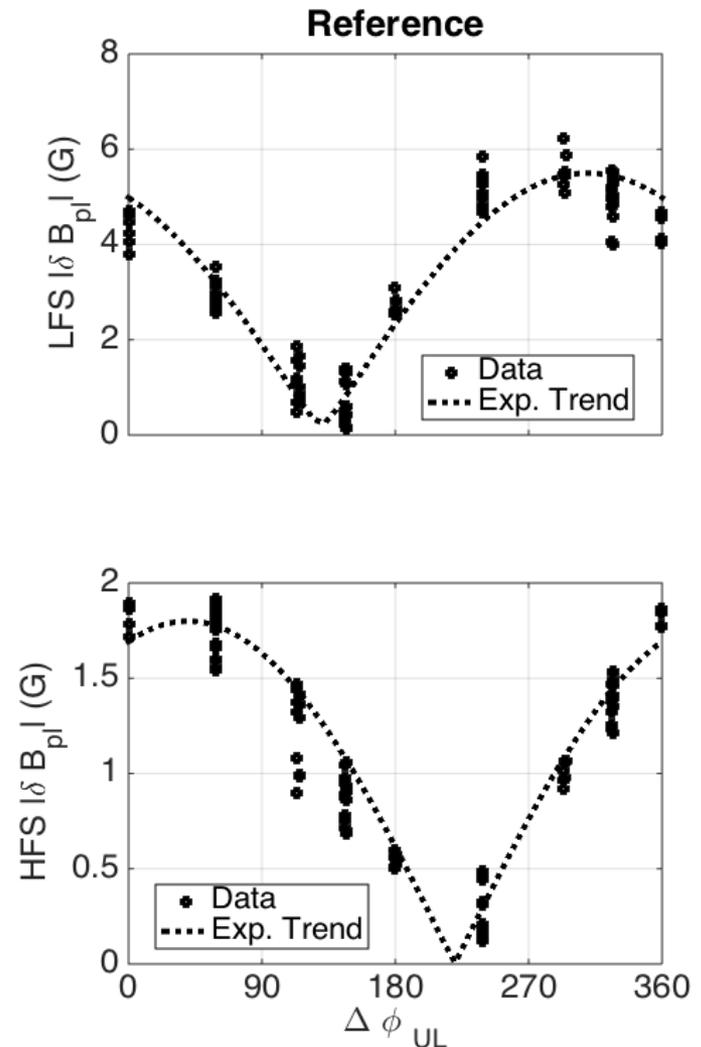
LFS and HFS magnetic response measurements show multimode response on DIII-D

- **These plots show**
 - Magnitude of perturbed magnetic field as the phasing is varied
 - Signal at low-field side (LFS) and high-field side (HFS) probes
 - Field from plasma response only
 - Null occurring where response from upper and lower coils cancels
- **Signals at LFS and HFS have different phasing dependences**
- **Indicates multiple modes are being driven simultaneously in DIII-D with $n=2$ fields**
- **For more detail, see C. Paz-Soldan et al., PRL 114, 105001 (2015)**



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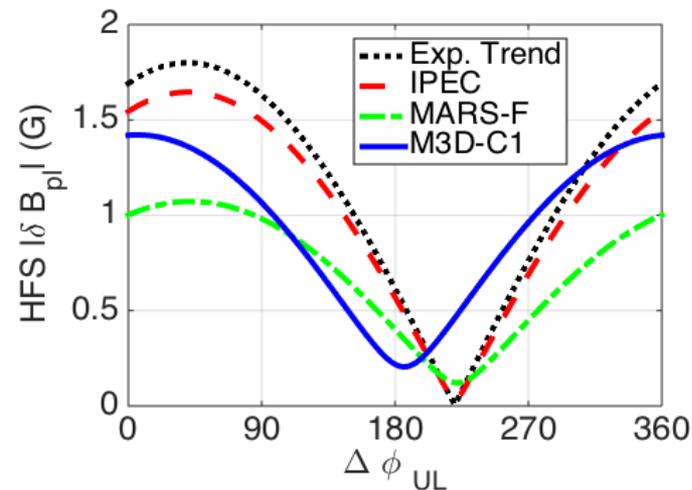
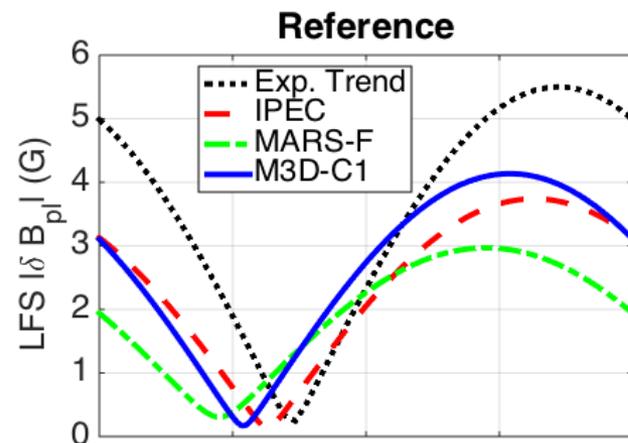


Modeling of reference shows excellent agreement between experimental data and various codes

- **IPEC¹ uses an ideal MHD model**
 - No rotation
 - Perfect screening at rational surfaces
- **MARS-F² uses a single-fluid, resistive MHD model**
 - Simulations performed with carbon toroidal rotation profile
 - Resistivity allows for tearing or imperfect screening
- **Here, M3D-C¹ use single-fluid model with ExB rotation profile**

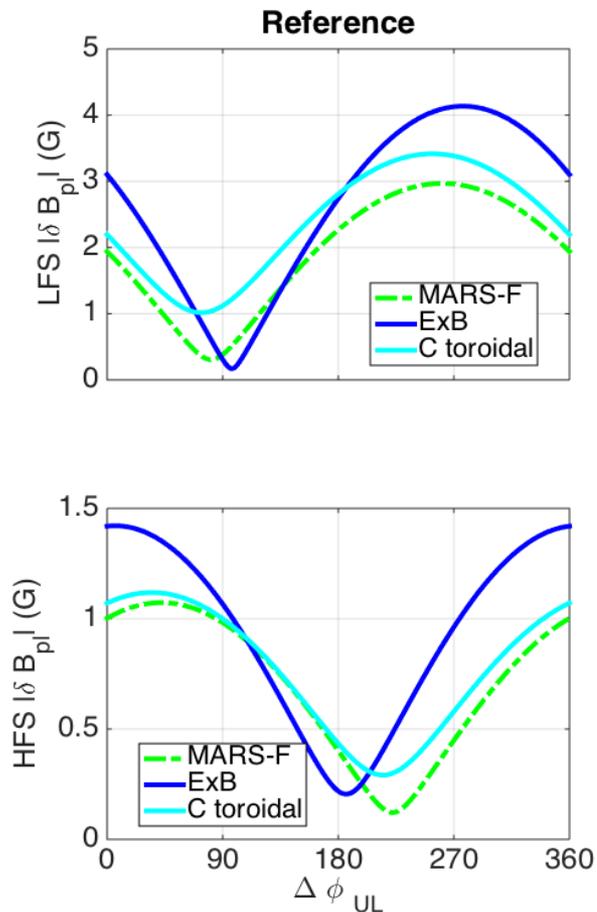
¹ J.-K. Park, A.H. Boozer, and A.H. Glasser, Phys. Plasmas 14, 052110 (2007).

² Y. Q. Liu, et al., Phys. Plasmas 7, 3681 (2000).

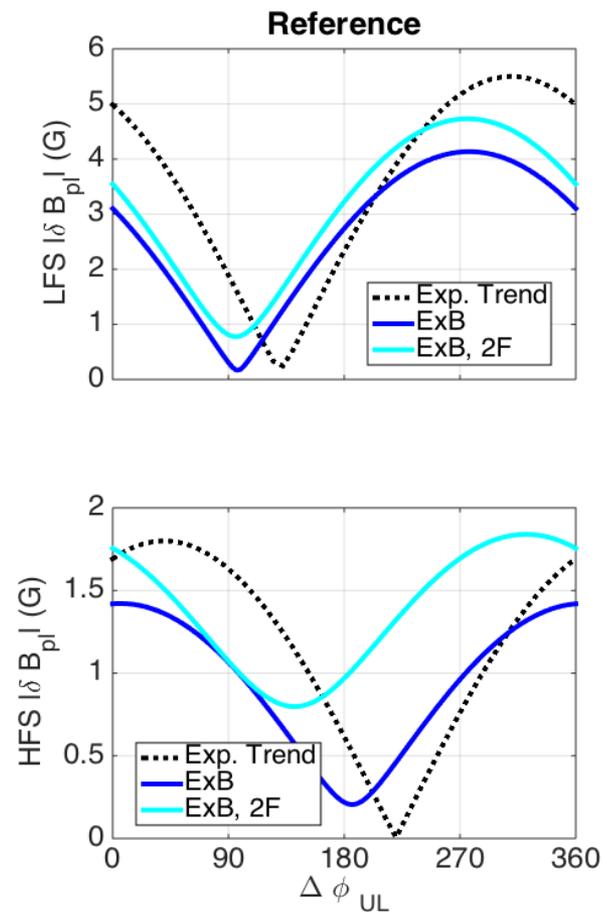


M3D-C¹ results sensitive to changes in non-ideal effects

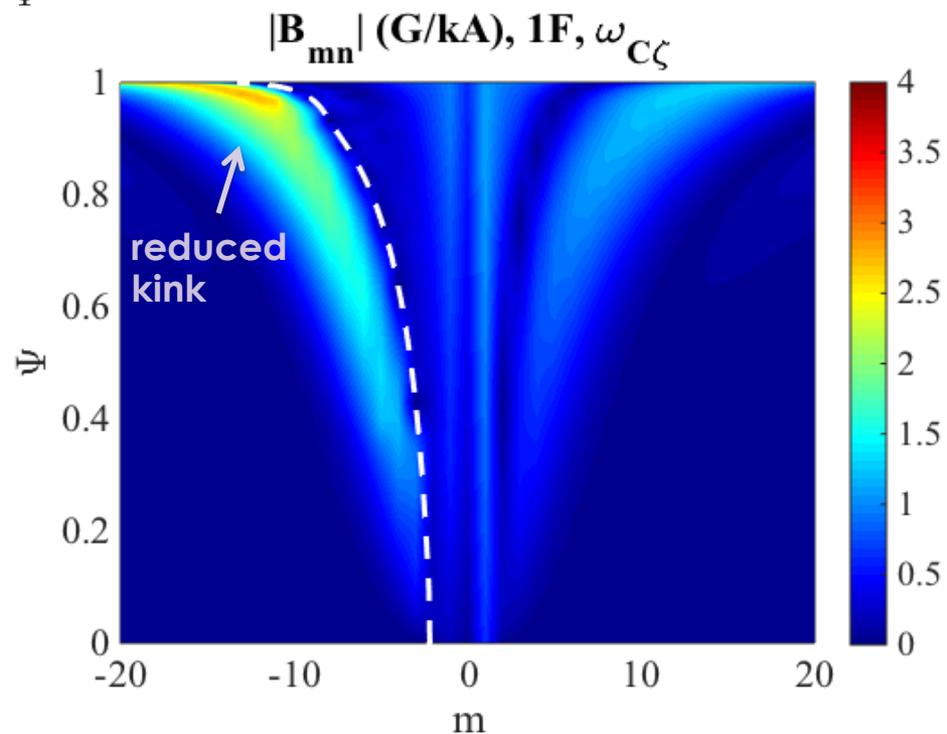
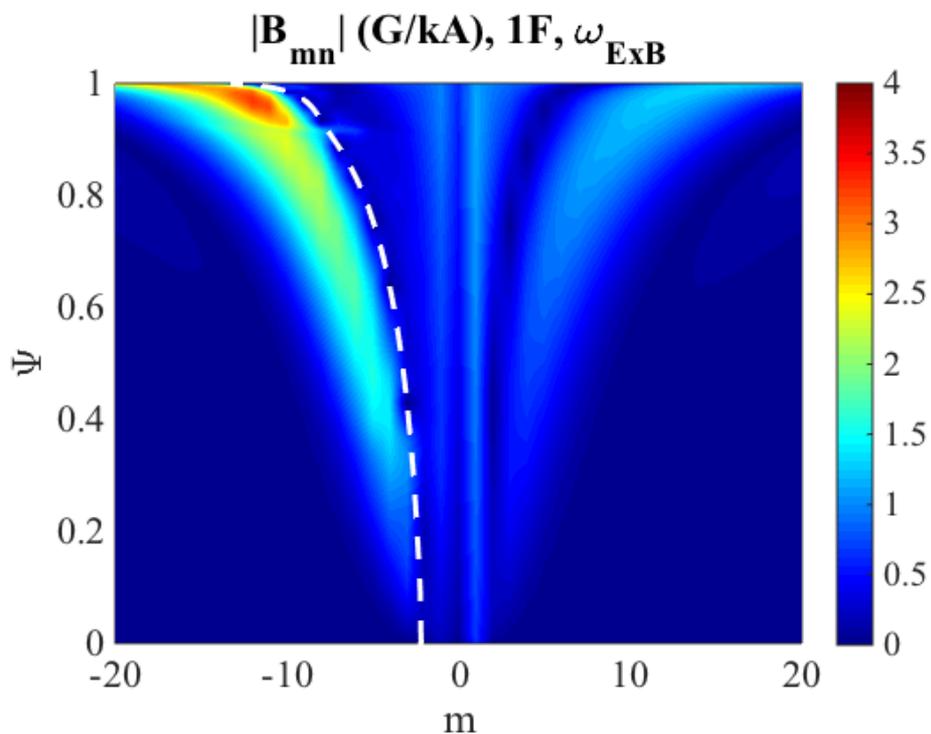
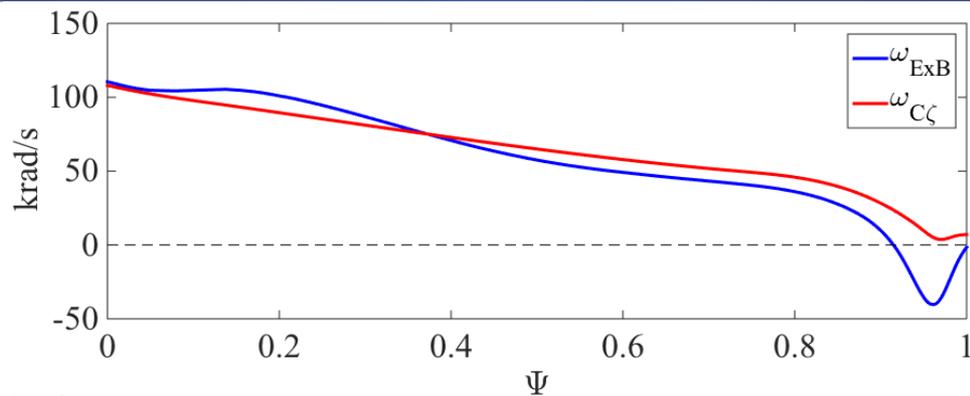
Using carbon toroidal rotation improves agreement with MARS-F



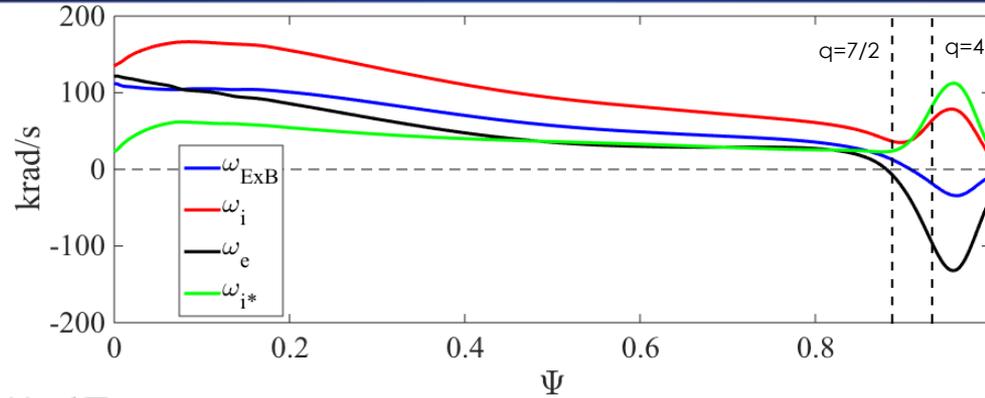
Including two-fluid terms gives poorer agreement with data



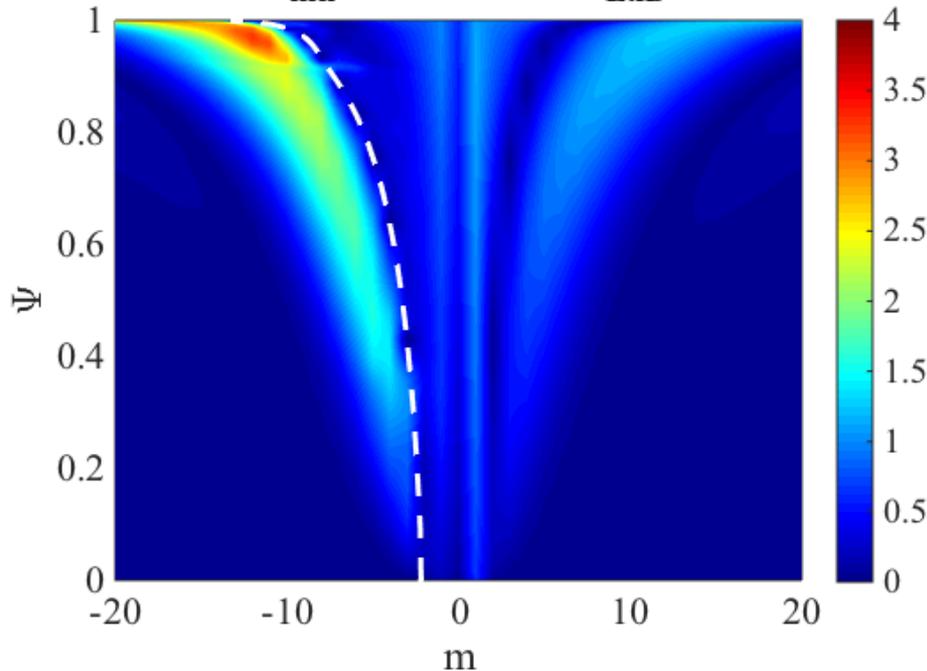
Carbon toroidal rotation profile results in reduced kink response



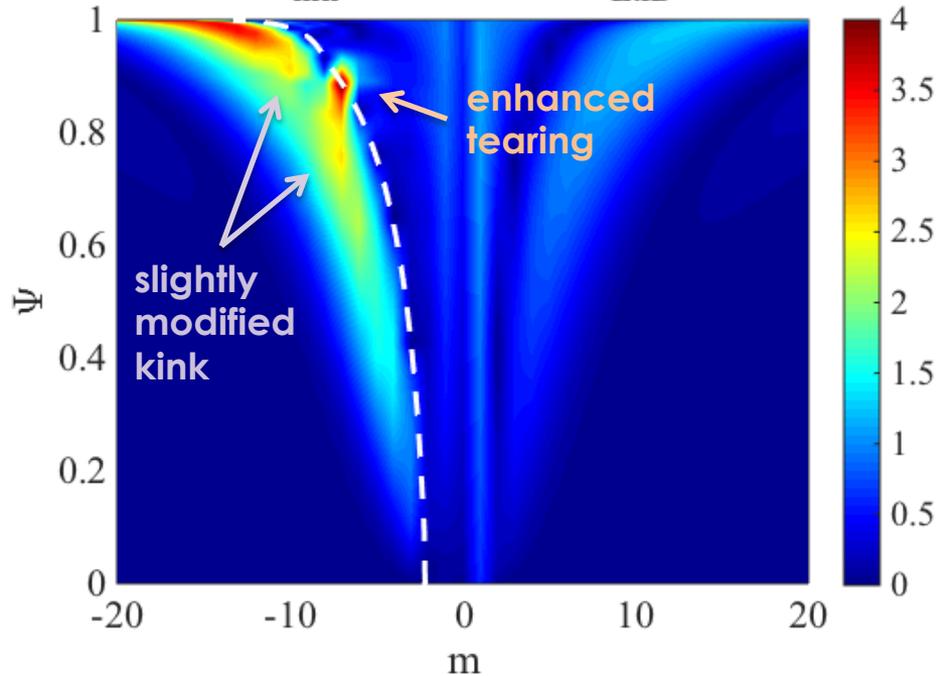
Enhanced tearing in two-fluid simulation due to electron rotation zero crossing near $q=7/2$



$|\mathbf{B}_{\text{mn}}|$ (G/kA), 1F, ω_{ExB}



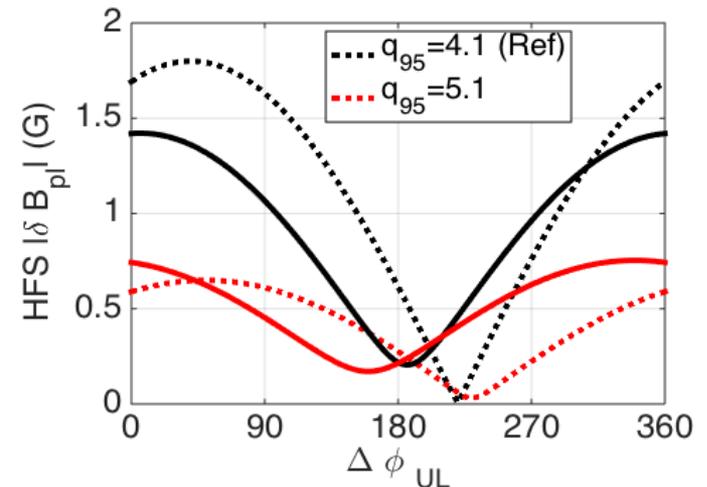
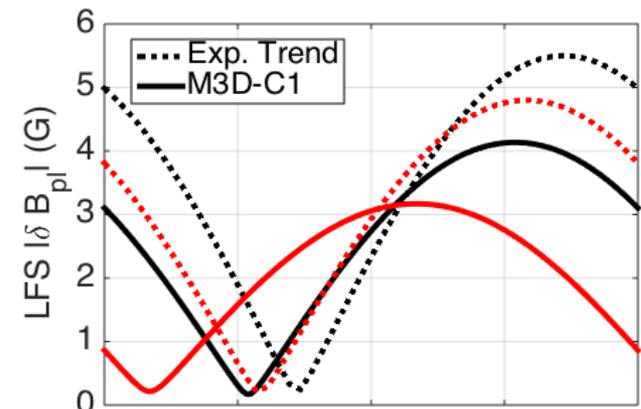
$|\mathbf{B}_{\text{mn}}|$ (G/kA), 2F, ω_{ExB}



Plasma response variation with equilibrium parameters

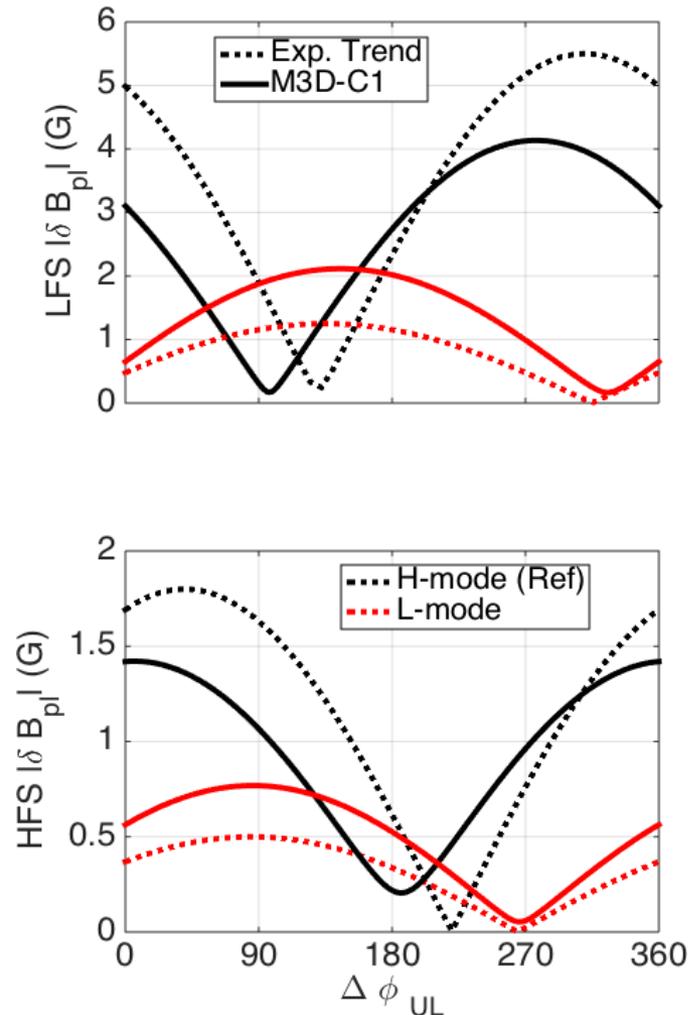
High q_{95} trends on both LFS and HFS roughly captured by M3D-C¹ modeling

- High q_{95} discharge has $q_{95} = 5.1$ $\beta_N = 2.2$ $\nu_{e^*} = 0.25$
- LFS probe shows slight shift in phasing variation
- HFS probe shows significant amplitude decrease
- M3D-C¹ sees both these trends, although
 - LFS phase shift somewhat larger than experiment
 - HFS amplitude decrease somewhat smaller than exp.
- IPEC and MARS-F find phase shift on LFS but don't capture amplitude reduction on HFS



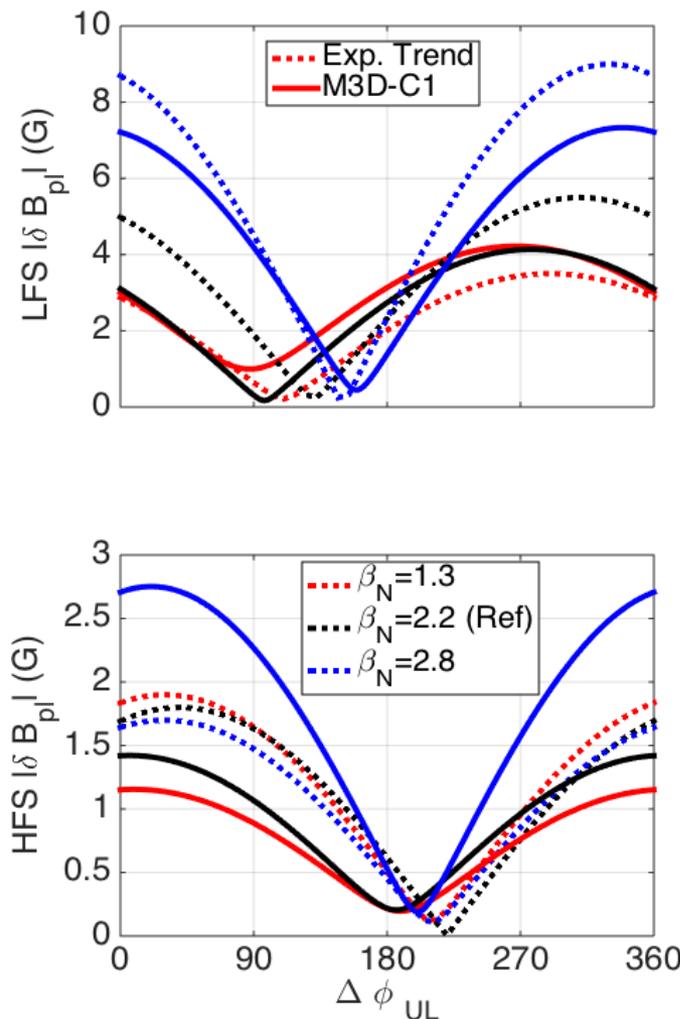
H- to L-mode trends on both LFS and HFS captured by M3D-C¹ modeling

- **L-mode discharge has**
 $q_{95} = 3.8$ $\beta_N = 0.50$ $v_{e^*} = 15$
- **LFS probe shows**
 - significant amplitude decrease
 - large shift in phasing variation
- **HFS probe shows**
 - significant amplitude decrease
 - slight shift in phasing variation
- **L-mode closer to single-mode response**
- **M3D-C¹ sees these trends, though the amplitude decreases are somewhat smaller**
- **IPEC and MARS-F capture LFS but not HFS trends**



M3D-C¹ struggles to reproduce β trends

- **Low- β discharge**
 $\beta_N = 1.3$ $\nu_{e^*} = 0.3$ $q_{95} = 4.05$
- **High- β discharge**
 $\beta_N = 2.8$ $\nu_{e^*} = 0.15$ $q_{95} = 4.25$
- **LFS probe shows**
 - significant amplitude increase
 - slight phasing shift w/ increasing β
- **HFS probe response largely insensitive to β**
- **M3D-C¹ modeling**
 - Does an okay reproducing LFS trend, especially at highest β
 - Does not capture HFS invariance
- **IPEC captures both trends for smoothly-varied equilibria**

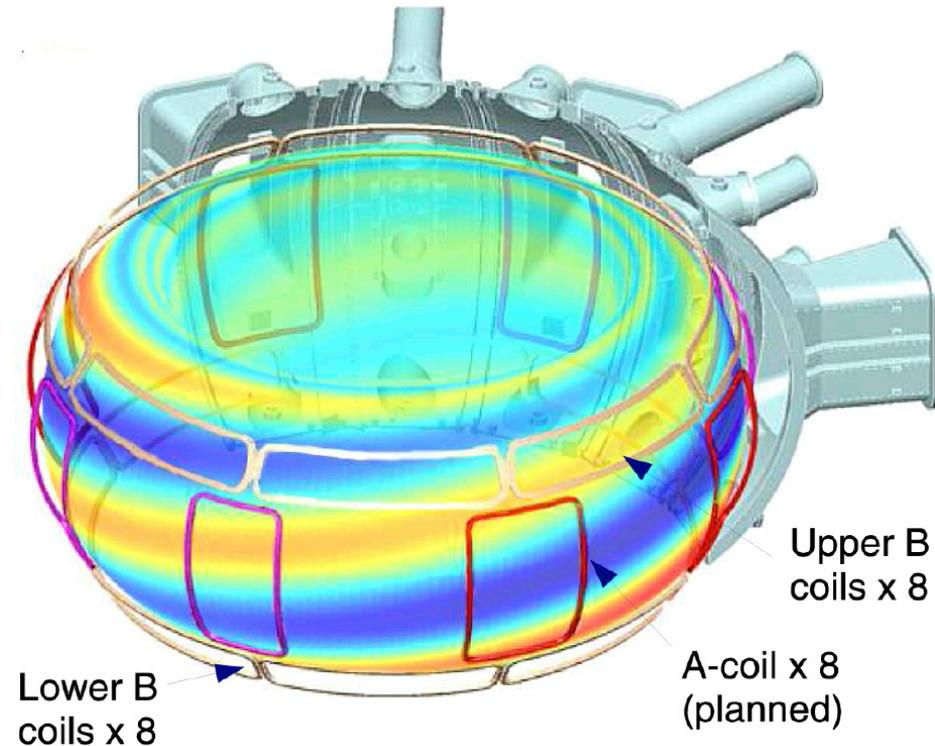


ASDEX Upgrade

External field coils on ASDEX Upgrade

- Two rows of eight in-vessel saddle coils
- Toroidal mode number of perturbations up to $n=4$
- For $n=2$ fields, the differential phase angle (AKA phasing) can be varied between upper and lower coils sets
 - $\Delta\varphi = \phi_{up} - \phi_{low}$
 - Varies the magnetic pitch angle of the applied field
 - Affects coupling of resonant and non-resonant fields

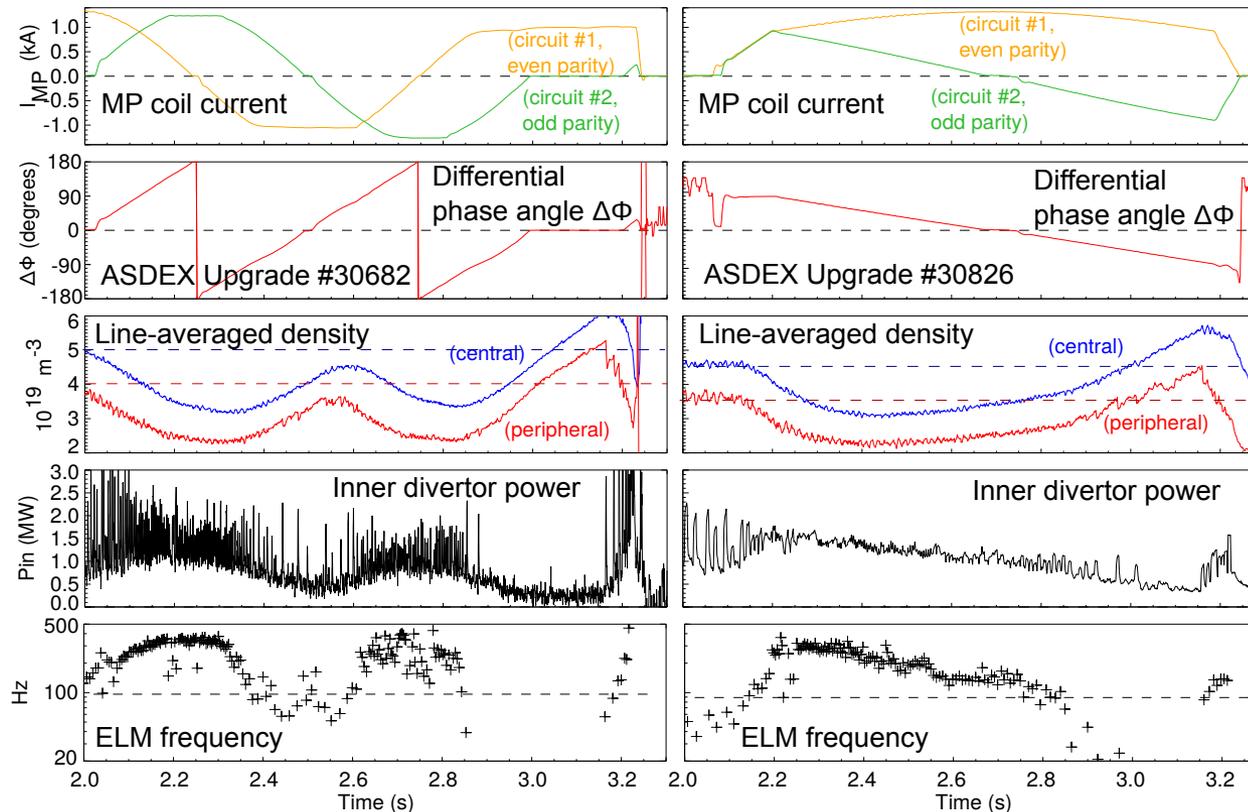
Figure 1 from G D Conway et al 2015 Plasma Phys. Control. Fusion 57 014035



Phasing affects the magnitude of ELM mitigation

- Density and ELM frequency are modulated by phasing
- Strongest mitigation at minimum density

Suttrop, W. et al. EX/P1-23. IAEA FEC 2014.

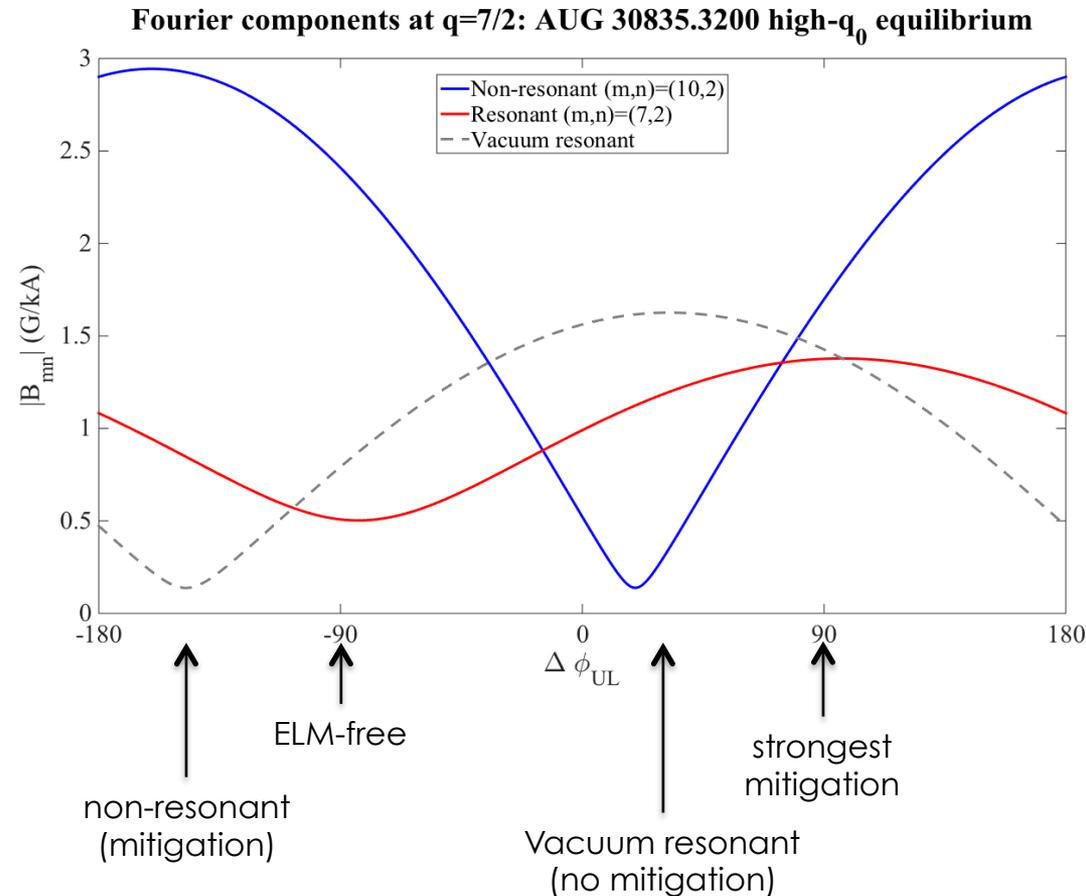


M3D-C¹ has calculated the plasma response for ASDEX Upgrade shot 30835

- **Good ELM mitigation observed with n=2 fields in 30835 and similar shots**
- **Four phasings have been studied with MARS-F and VMEC**
 - $\Delta\varphi = 30^\circ$: Optimum vacuum resonance
 - $\Delta\varphi = 90^\circ$: Strongest ELM mitigation
 - $\Delta\varphi = -90^\circ$: Classical, non-stationary ELM-free phase
 - $\Delta\varphi = -150^\circ$: Optimum non-resonant field (ELM mitigation observed)
- **We've used M3D-C¹ to examine this shot**
 - Time-independent, linear analysis
 - Not quantitative validation work
 - Not comparing to measured field data
 - Only examining qualitative trends/correlations

Resonant and non-resonant fields may both impact ELM mitigation

- Strongest ELM mitigation occurs where resonant field is maximized
- Non-resonant field may play significant role
 - Resonant field similar at $\Delta\varphi = 30^\circ$ & $\Delta\varphi = -150^\circ$
 - Non-resonant field significantly stronger at $\Delta\varphi = -150^\circ$ where ELM mitigation is observed



Summary

- **M3D-C¹ has been used to calculate the linear, steady-state plasma response of DIII-D and ASDEX Upgrade to external, three-dimensional magnetic perturbations**
- **Validation against magnetic probe signals on DIII-D shows**
 - Good agreement with reference, L-mode, and high- q_{95} equilibria
 - Poor agreement with data as β is varied
- **Cross-code verification work with IPEC and MARS-F**
 - M3D-C¹ captures some trends on the magnetic probes not captured by IPEC and MARS-F, and vice versa
 - Source of discrepancies in between the codes, and with the data, still uncertain
 - M3D-C¹ modeling demonstrates sensitivity to the rotation profile
 - MARS-F may achieve better agreement with data if ExB rotation profile is used
 - Small changes in the degree of resonant penetration can have relatively large impact on magnetic signals

Summary (continued) and future work

- **Preliminary investigations on ASDEX Upgrade suggest that ELM mitigation is determined by both resonant and non-resonant affects**
- **Future work**
 - Detailed comparison between Fourier spectra from M3D-C¹, IPEC, and MARS-F solutions to determine source of discrepancies
 - Further examination of sensitivities to nonideal effects
 - Rotation profile variation on M3D-C¹ and MARS-F
 - Improved two-fluid analysis with M3D-C¹
 - Additional studies of ASDEX Upgrade plasmas
 - Examine other shots, especially from recent experiments
 - Perform quantitative validation work
 - New collaboration with KSTAR to study ELM suppression experiments, including multiple toroidal harmonics



Low-collisionality drift-kinetic calculations in up-down asymmetric M3D-C¹ equilibria

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NIES solves to the low-collisionality drift-kinetic distribution function

- **The Neoclassical Ion-Electron Solver (NIES) solves a set of drift kinetic equations (DKEs)**
 - Steady-state distribution function in general, axisymmetric geometries
 - Deep in low-collisionality regime
 - Conductivity, flows, and bootstrap currents can be calculated
 - DKEs reduce to solvability conditions on the linearized Fokker-Planck-Landau collision operator

$$\oint_{\psi, w, \lambda} \frac{dl}{w_{\parallel}} C_s [\zeta H K_s] = - \oint_{\psi, w, \lambda} dl S_s$$

$$C_s [K_s] = \frac{2\nu_{Ds}(w)}{w} \frac{\partial}{\partial \lambda} \left(\eta_1(\lambda) \lambda \frac{\partial K_s}{\partial \lambda} \right) + \frac{4\pi\nu_s v_{ths}^3}{nw} f_{Ms} \eta_2(\lambda) K_s$$

$$+ \nu_s \eta_2(\lambda) \frac{v_{ths}^3}{w^3} \frac{\partial}{\partial w} \left[\xi_s \left(w \frac{\partial K_s}{\partial w} + \frac{w^2}{v_{ths}^2} K_s \right) + \xi_{s'} \left(w \frac{\partial K_s}{\partial w} + \frac{m_s w^2}{m_{s'} v_{ths'}^2} K_s \right) \right]$$

$$- \frac{\nu_s v_{ths}}{nw} f_{Ms} \int_0^{2\pi} \frac{JB}{y(\theta, \lambda)} \Phi_s d\theta + \frac{\nu_s w}{n v_{ths}} f_{Ms} \frac{d^2}{dw^2} \int_0^{2\pi} \frac{JB}{y(\theta, \lambda)} \Psi_s d\theta.$$

$$S_e = \left\{ \frac{eV_0 I}{T_e} \int_0^{2\pi} \frac{\mathcal{J}}{R^2} d\theta + \frac{\nu_e v_{the}}{v_{thi}^2 w} \xi_i \left(U_i \int_0^{2\pi} \mathcal{J} B^2 d\theta + \frac{I}{en} \frac{dp}{d\psi} \int_0^{2\pi} \mathcal{J} d\theta \right) \right.$$

$$\left. + \frac{\nu_e m_e I}{e T_e} \frac{dT_e}{d\psi} \frac{v_{the}}{w} \left[2\varphi_e - 10\xi_e + \frac{1}{2}\varphi_i - \frac{5v_{the}^2}{2v_{thi}^2} \xi_i \right] \int_0^{2\pi} \mathcal{J} d\theta \right\} f_{Me}$$

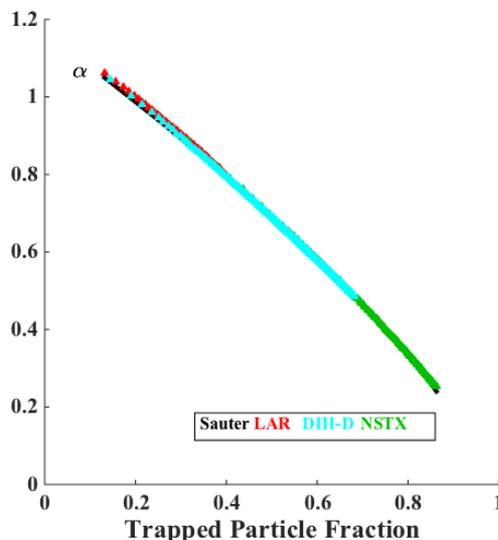
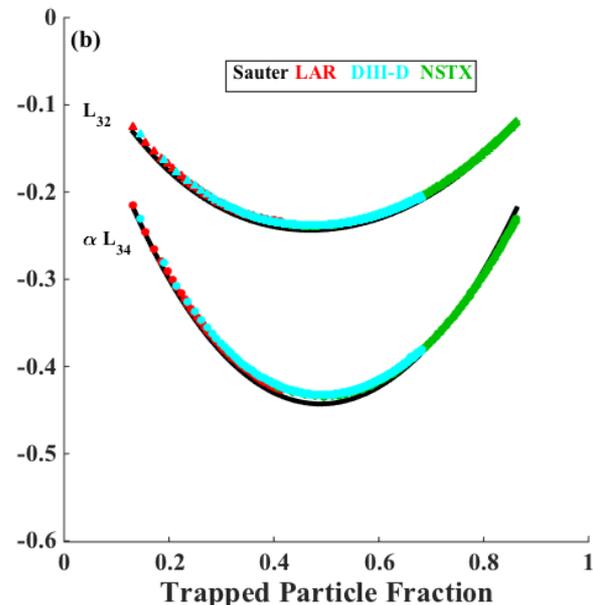
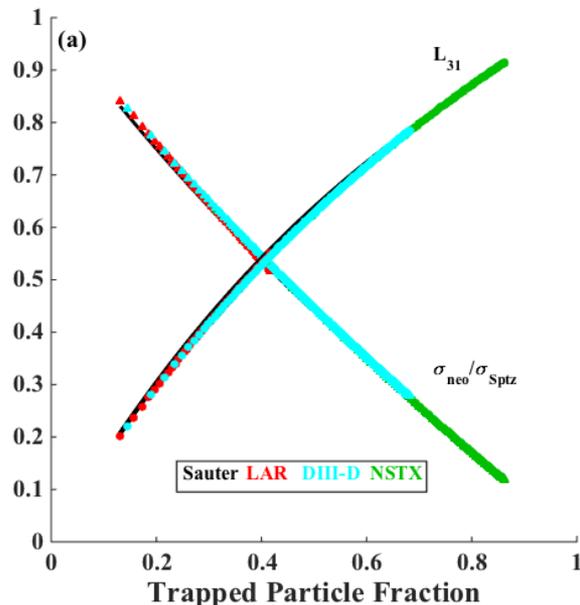
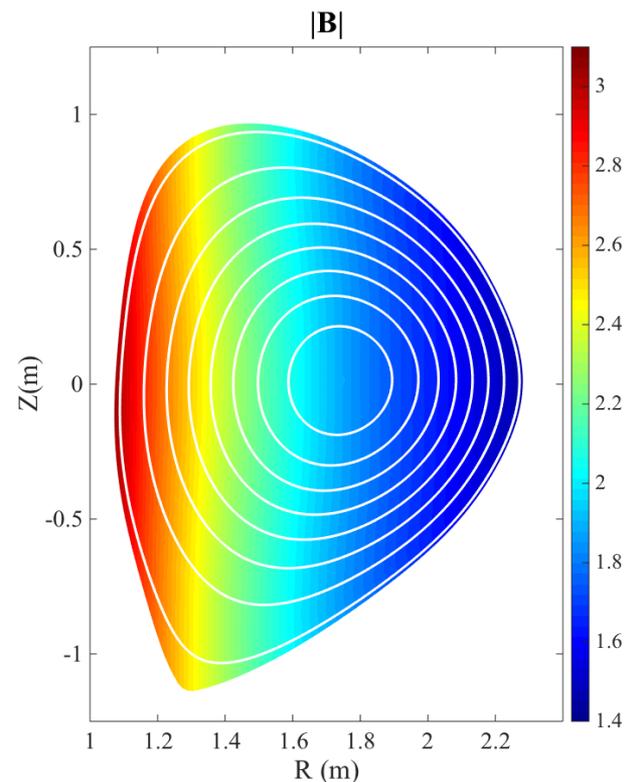
$$S_i = - \frac{\nu_i m_i I}{e T_i} \frac{dT_i}{d\psi} \frac{v_{thi}}{w} [2\varphi_i - 10\xi_i] f_{Mi} \int_0^{2\pi} \mathcal{J} d\theta$$

NIES can now accept M3D-C¹ equilibria as input

- **Previously NIES used**
 - Analytic, large aspect ratio equilibria
 - Numerical equilibria from JSOLVER
 - Only up-down symmetric equilibria had been considered
- **IDL routines written by N.M. Ferraro output necessary quantities from M3D-C¹ equilibria**
 - Translate equilibria to flux coordinates as used by NIES
 - NetCDF standard output
- **NIES modified to read these equilibria**
 - Initialization subroutines convert NetCDF input to NIES data structures
 - Few other changes needed to NIES

NIES conductivity and bootstrap currents for M3D-C¹ and JSOLVER equilibria benchmarked to Sauter fits

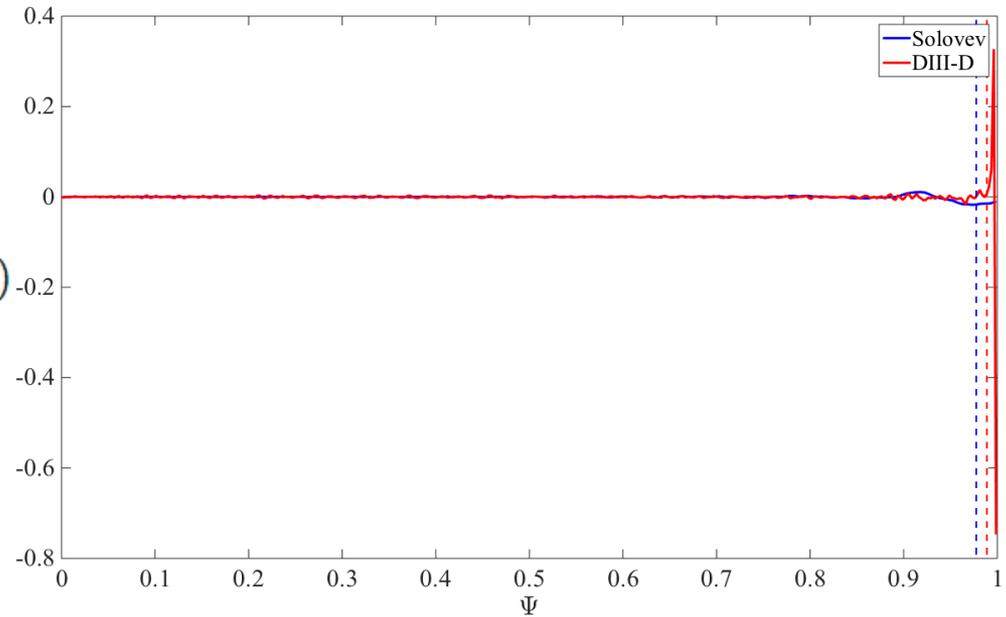
DIII-D equilibrium below is from M3D-C¹



LAR & NSTX equilibria are from JSOLVER

Up-down asymmetric equilibria allow for the numerical evaluation of the geometric function Γ

$$\Gamma(\psi) = 2 \frac{d}{d\psi} \oint d\ell \mathbf{B} \cdot \nabla R^2 + \oint \frac{d\ell}{B} [2\mathbf{b} \cdot \nabla (\nabla\psi \cdot \nabla \ln R^2) + \nabla\psi \cdot \nabla (\mathbf{b} \cdot \nabla \ln B)]$$



- Appears in ion DKE when $\nu_* \sim \delta \ll 1$
- Trivially zero for up-down symmetric equilibria
- Numerical evaluation within NIES from M3D-C¹ equilibria showed it to be small, albeit noisy
- Prompted further analytic evaluation, revealing it to be identically zero in all Grad-Shafranov equilibria

Summary and future work

- **NIES**

- Now interfaces with M3D-C¹ axisymmetric equilibria, solving for
 - Steady-state, low-collisionality distribution functions
 - Neoclassical conductivity, poloidal flow, and bootstrap currents
- Numerical evaluation and subsequent analytic evaluation of novel geometric factor present at extremely low collisionality has revealed it to be identically zero
- NIES is therefore accurate in the $\nu_* \sim \delta \ll 1$ regime for both ions and electrons without further modification

- **DK4D**

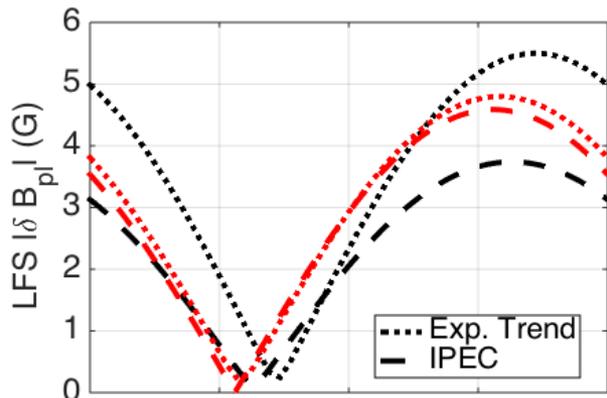
- Finite-collisionality, time-dependent DKE solver uses much of the same machinery that NIES uses
- Should be able to interface with M3D-C¹ equilibria relatively easily
- Will be used to provide neoclassical closure for M3D-C¹
- Transport-timescale evaluation of axisymmetric steady-state equilibria with self-consistent resistivity and bootstrap currents

ADDITIONAL SLIDES

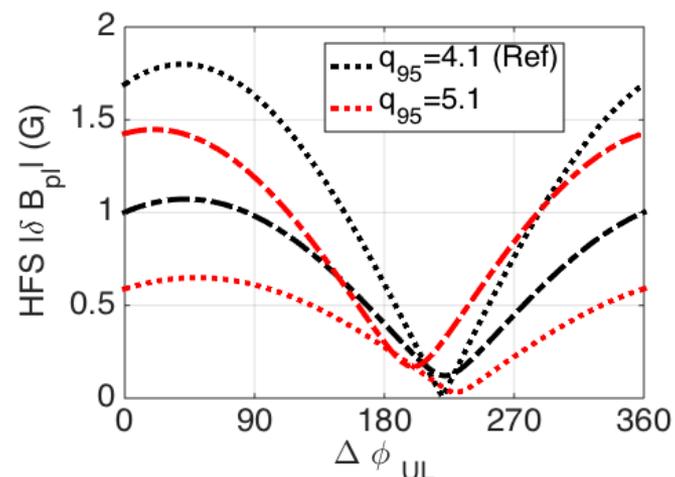
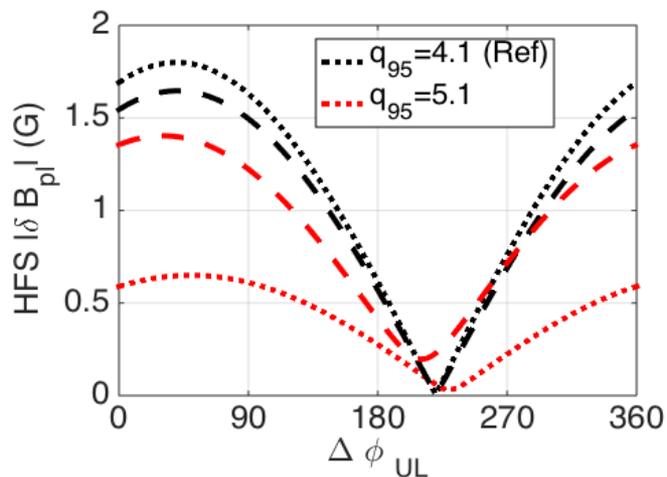
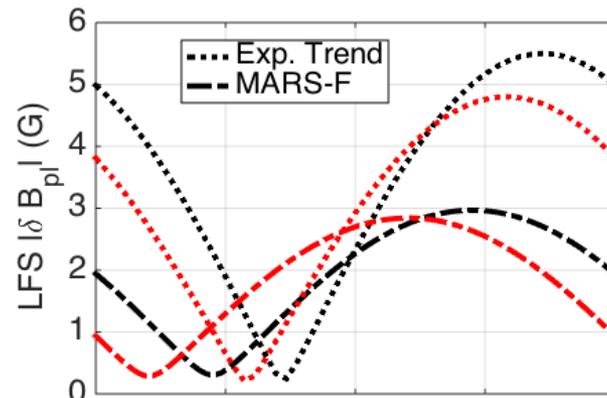


HFS q_{95} trends not captured by IPEC or MARS

IPEC



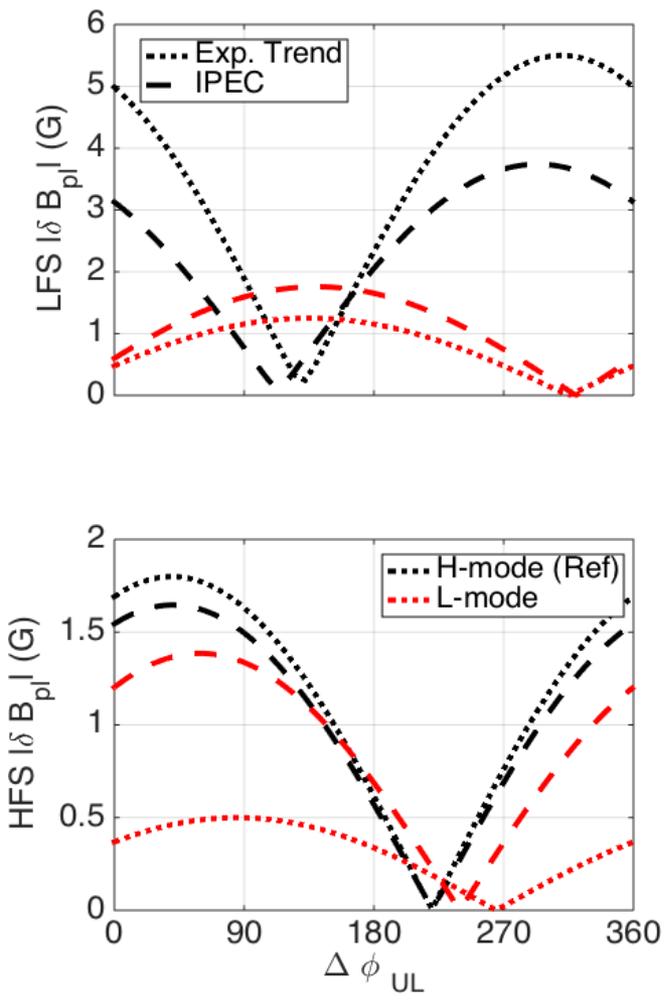
MARS-F



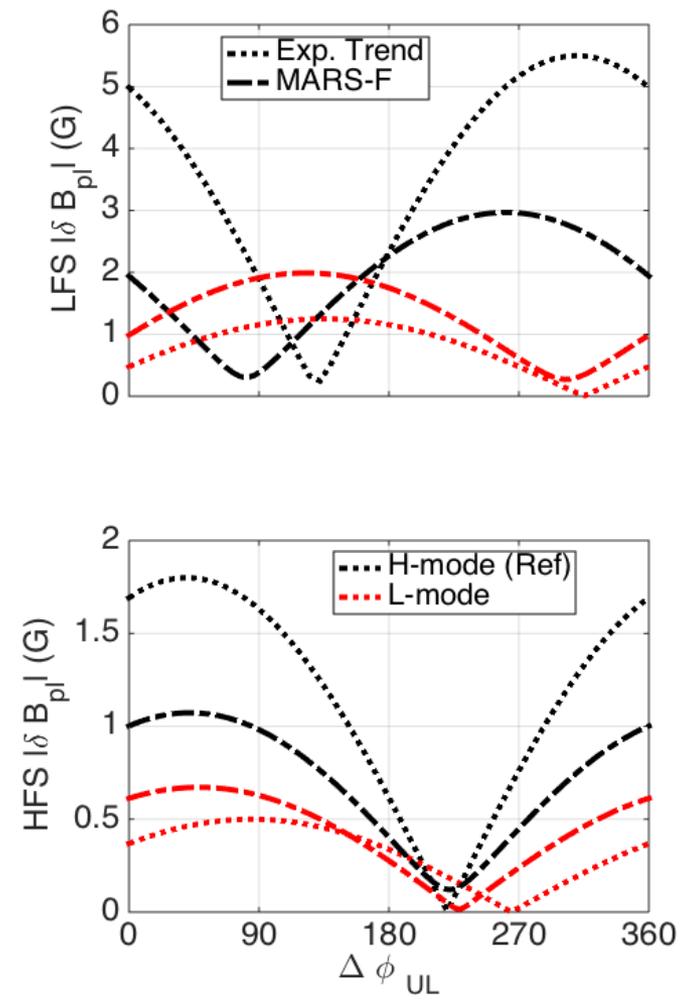


HFS H- to L-mode trends not captured by IPEC or MARS

IPEC

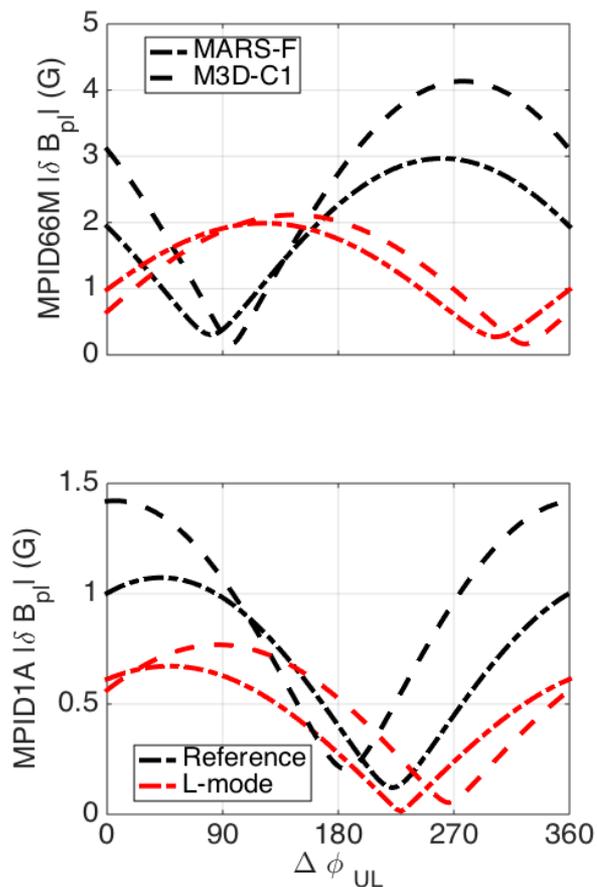


MARS-F

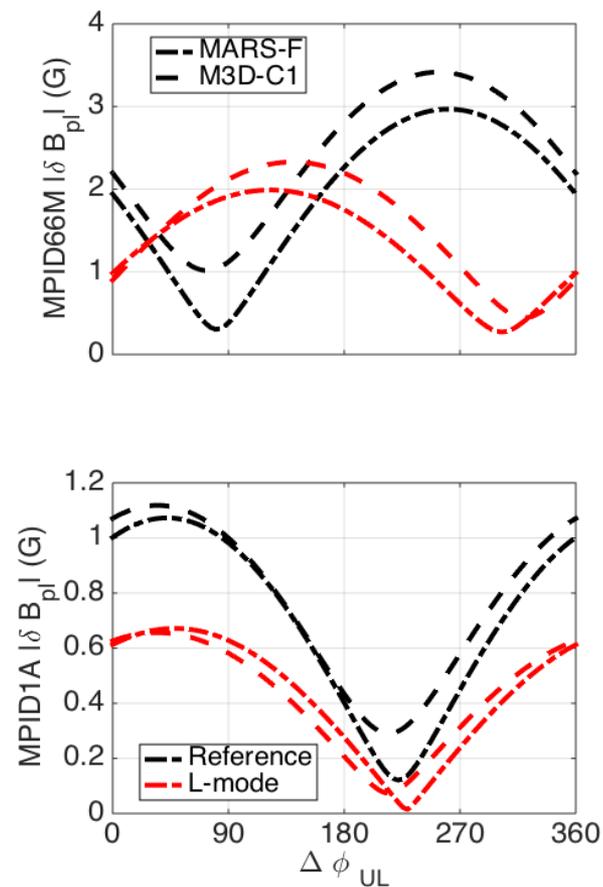


MARS-F agreement with L-mode data could be improved by using ExB rotation profile

Compared to M3D-C¹ using ExB rotation

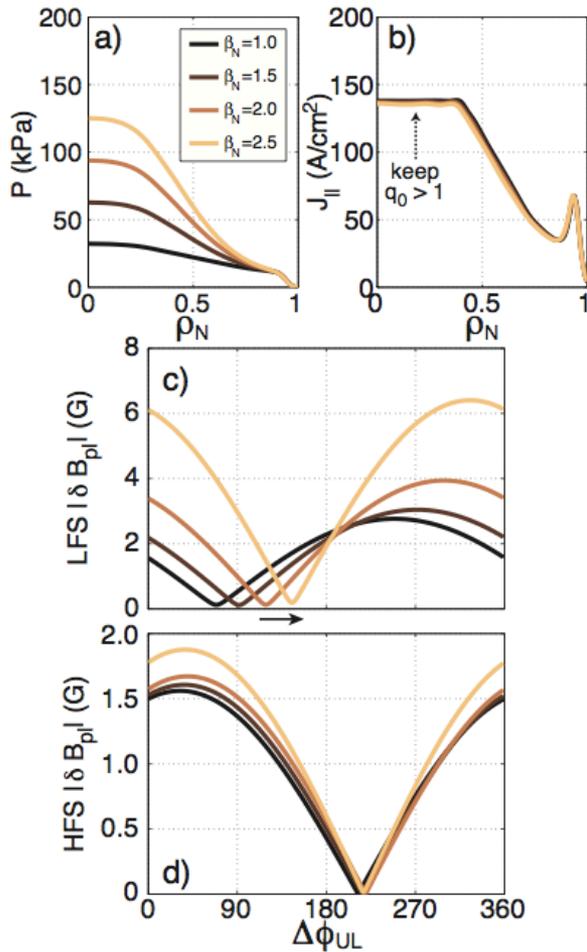


Compared to M3D-C¹ using carbon toroidal rotation



★ β trends are captured by IPEC for smoothly-varied equilibria, but not experimental reconstructions

VARYPED equilibria



Experimental reconstructions

