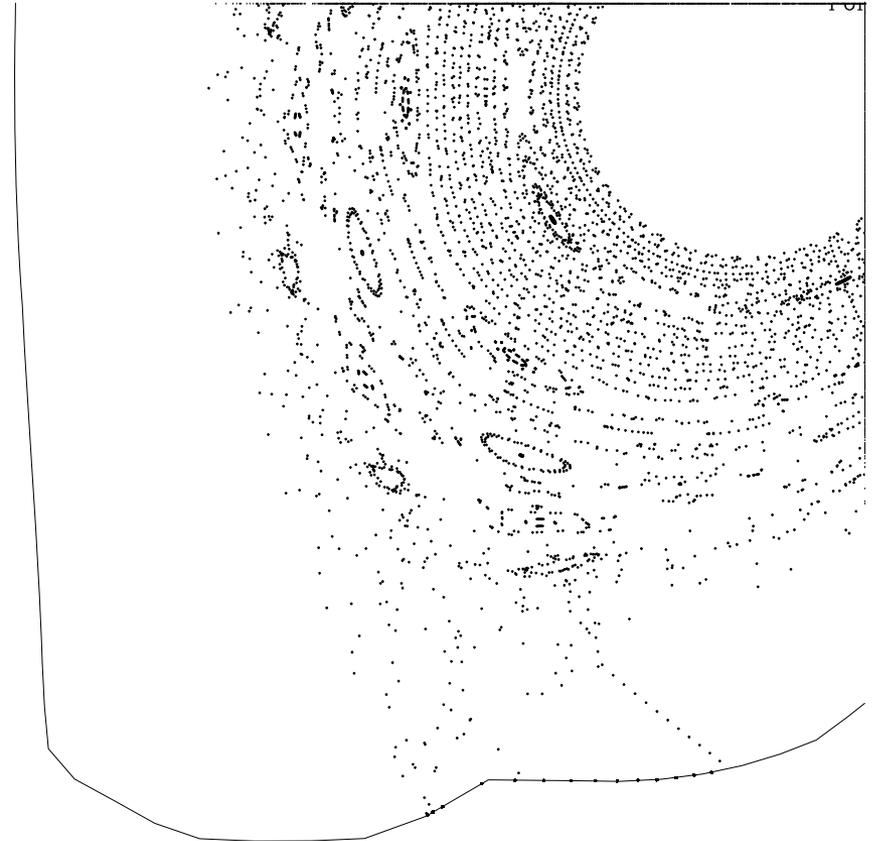


# M3D Simulation of RMPs, ELMs, RWMs

H. R. Strauss

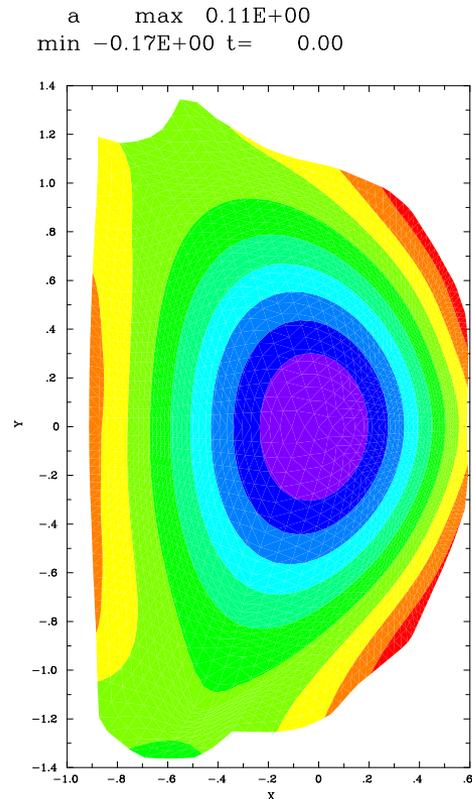
# RMP – resonant magnetic perturbations

- RMP has suppressed ELMs in DIII-D
  - 1 coil produces  $n=3$  magnetic perturbations
  - “vacuum” RMP produces stochastic magnetic field in outer 1/3 of plasma

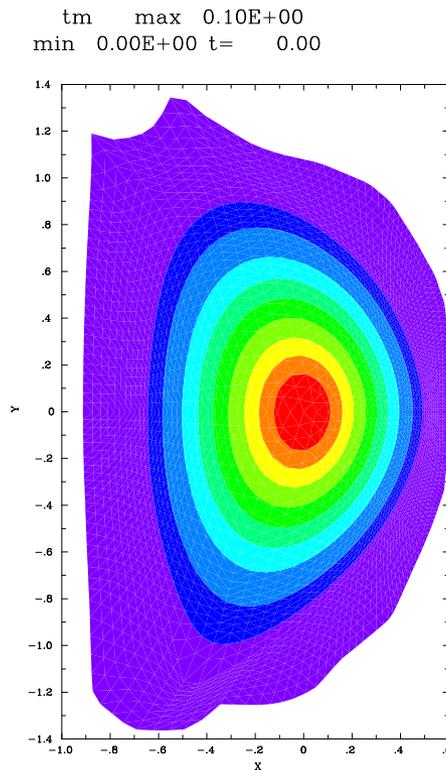


# M3D MHD simulations – initial state

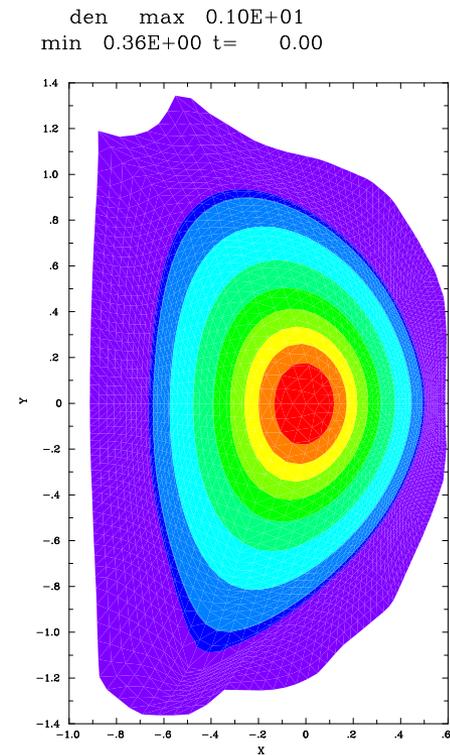
- M3D MHD simulations
  - Initialized from DIII-D eqdsk file of equilibrium reconstruction g126006



Magnetic flux



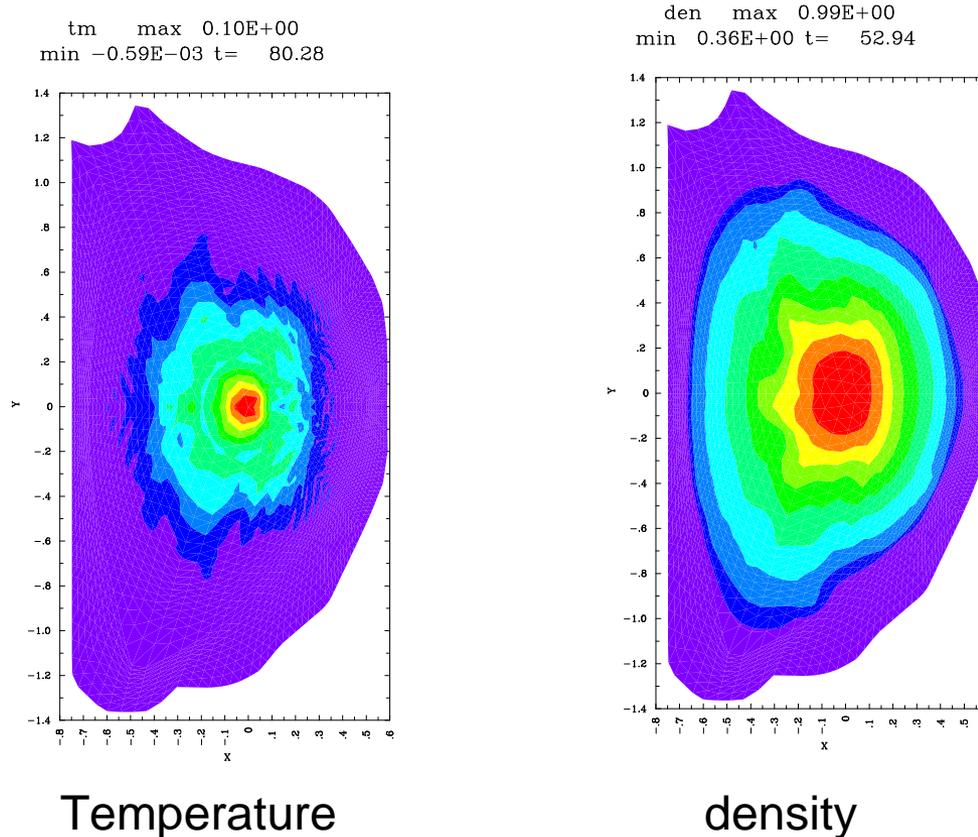
temperature



density

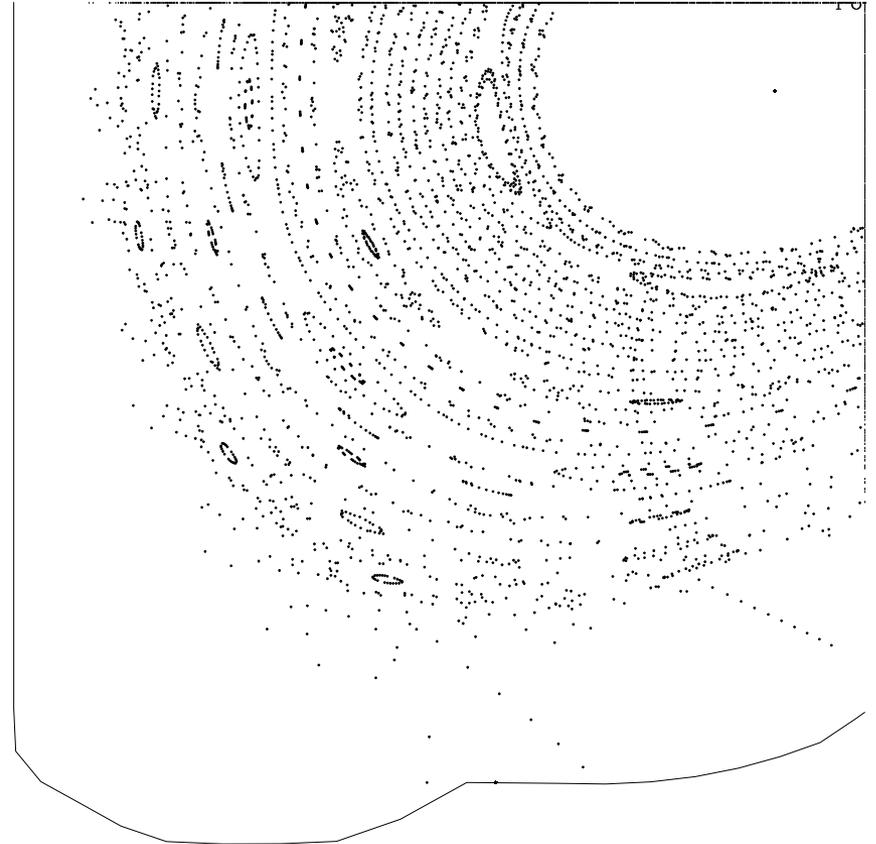
# Effect of “vacuum” RMP

- “vacuum” RMP added to initial equilibrium
  - Initial state evolved until  $t=80$   $\tau_A = R/v_A$
  - Rapid cooling due to large parallel thermal conduction
  - Slower density loss
- This is not what happens in DIII-D!



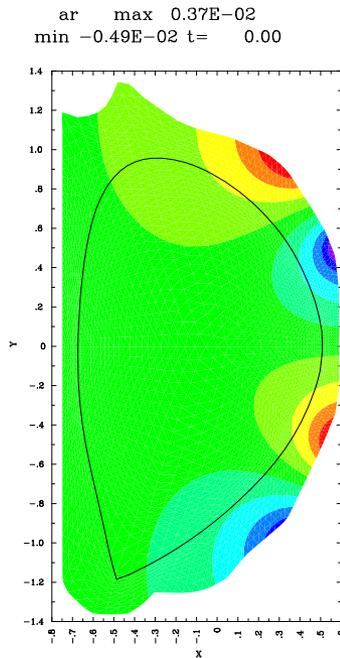
# Rotational screening of RMP

- In RMP experiments (Evans et al., PoP 12, 2006, Moyer et al. PoP 11, 2005) have a different behavior
  - Temperature is hardly affected by RMP
  - Density gradient relaxes
  - Density is pumped out
- Effect of rotation in M3D
  - First, consider purely toroidal rotation
  - Magnetic islands shrink
  - Plot at  $t = 56$

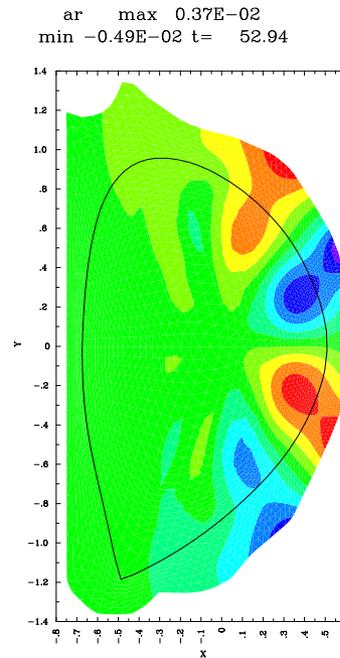


# Effect of rotation on RMP flux

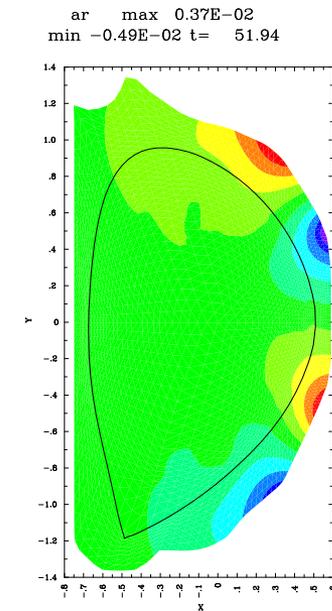
- In resistive MHD, the RMP appears to couple to a resistive mode
  - Magnetic perturbations exceed the “vacuum” RMP
  - Rotation suppresses this mode, as well as screening the RMP
  - Rotating and non rotating poloidal flux compared at  $t=52$ .



Vacuum RMP  
N=3 Poloidal flux



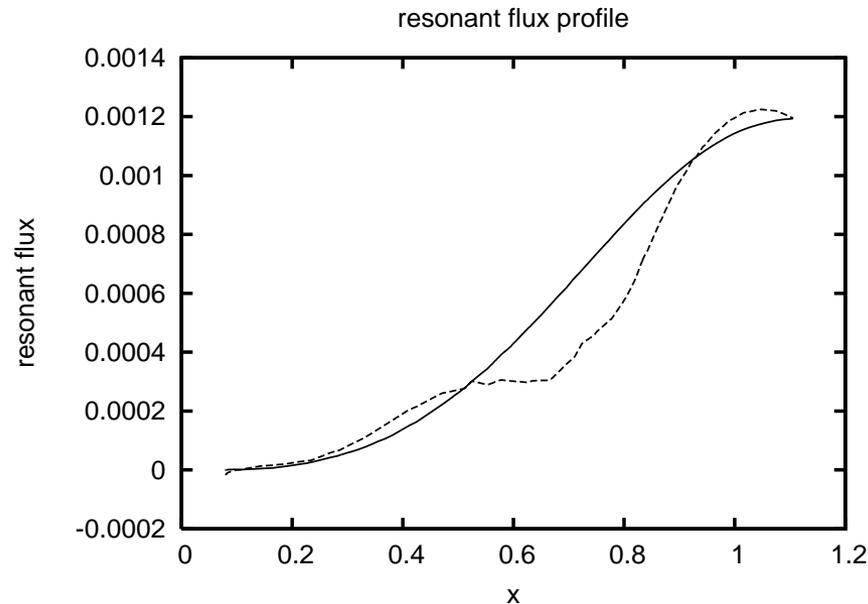
No rotation  
Poloidal flux



Rotation suppresses  
Mode and screens RMP

# Effect of rotation on flux penetration profile

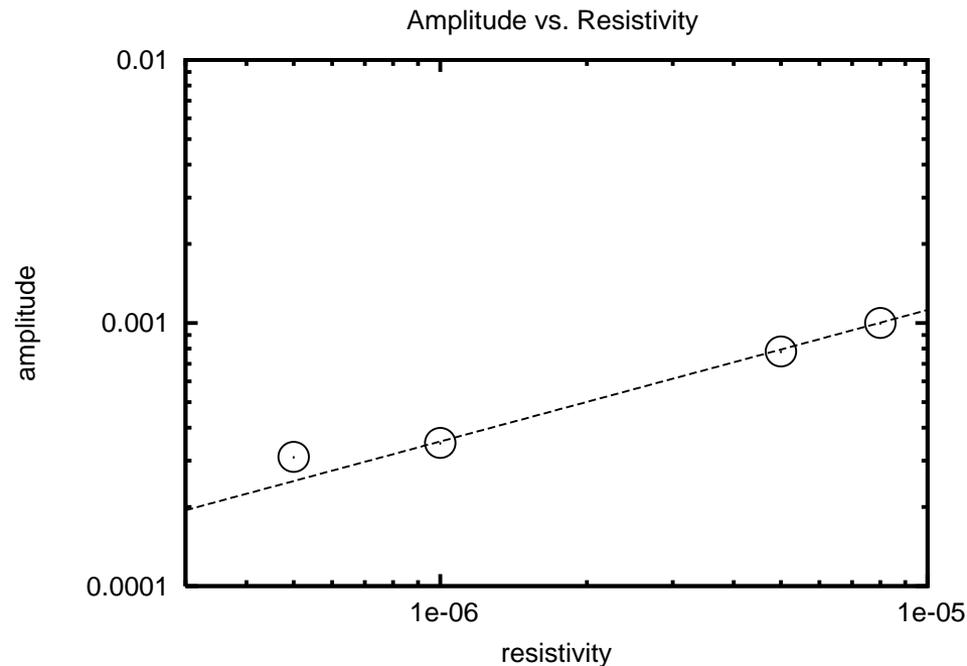
- Rotation excludes perturbed flux from the plasma
  - Profiles of perturbed flux along a ray from the magnetic axis to a point on the boundary where the flux is maximum
  - Solid curve: initial RMP flux, dashed curve: flux at  $t=52$  with rotation
- Flux penetration profile depends on rotation (especially poloidal rotation)



Perturbed poloidal  $n=3$  flux along a ray – solid: initial flux

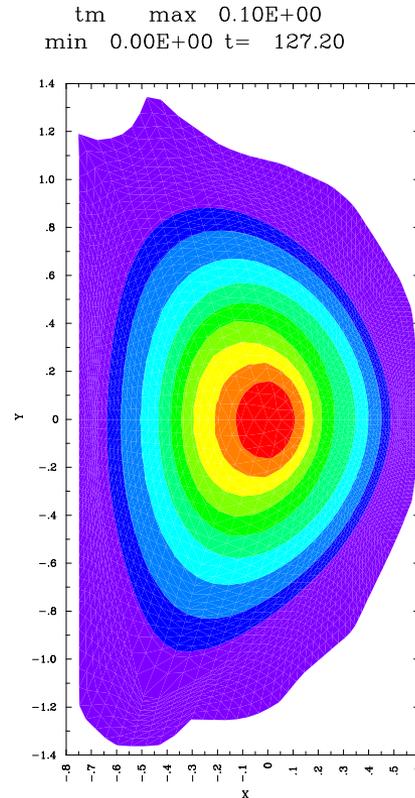
# scaling of critical rotation

- The growth of the resistive mode appears to scale as the  $\frac{1}{2}$  power of resistivity
  - In the simulations a Spitzer – like self consistent resistivity is used which varies at temperature to the  $-3/2$  power
  - Starting from the same initial state, the maximum amplitude of the  $n=3$  perturbation out of phase with the vacuum RMP is measured at  $t=52$
  - Critical rotation should have same scaling to shield RMP and suppress mode

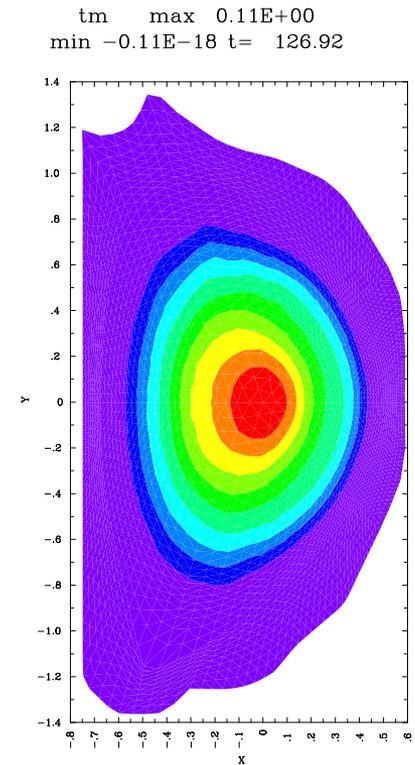


# Effects of rotation on temperature

- Rotation shrinks magnetic islands so there is less island overlap
  - A relatively thin stochastic layer remains at the separatrix
  - This causes some cooling at the edge
- Two rotating cases are compared: with and without RMP
  - The rotation in this case is purely toroidal, but the rotation profile is taken from g126006 equilibrium reconstruction
  - The rotation amplitude is larger in order to produce enough screening numerically
  - Show at time  $t=126$



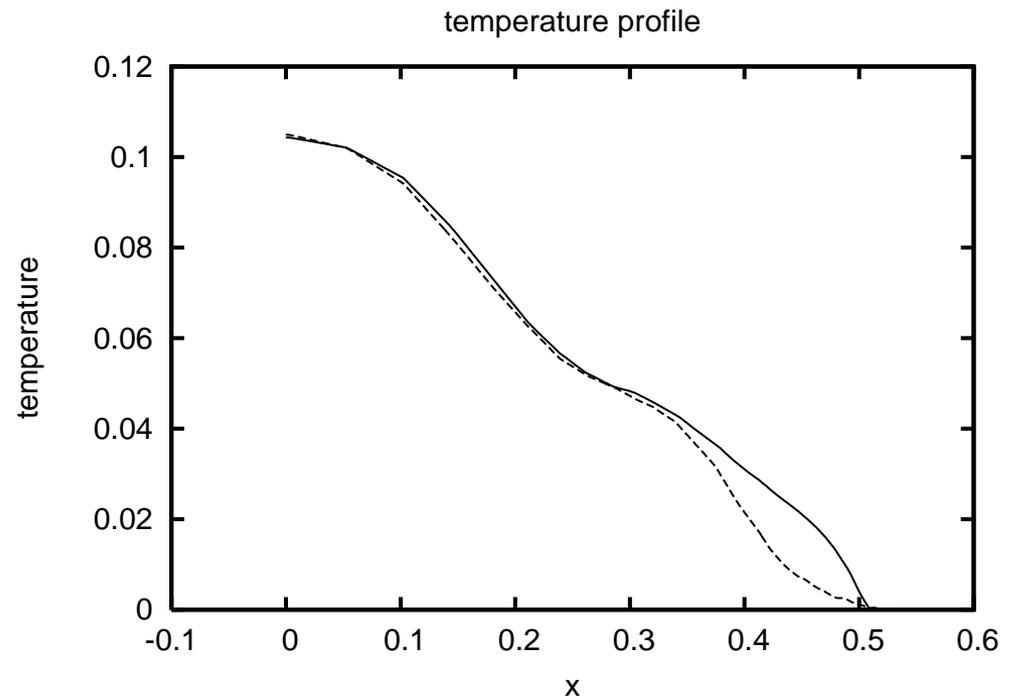
Temperature,  
No RMP



Temperature  
With RMP

# Effect of RMP and rotation on temperature profile

- The cooling region penetrates into the plasma
  - Profiles of temperature along midplane as a function of  $R - R_{\text{axis}}$
  - Solid line: no RMP, dashed line: with RMP
  - small effect on the plasma core

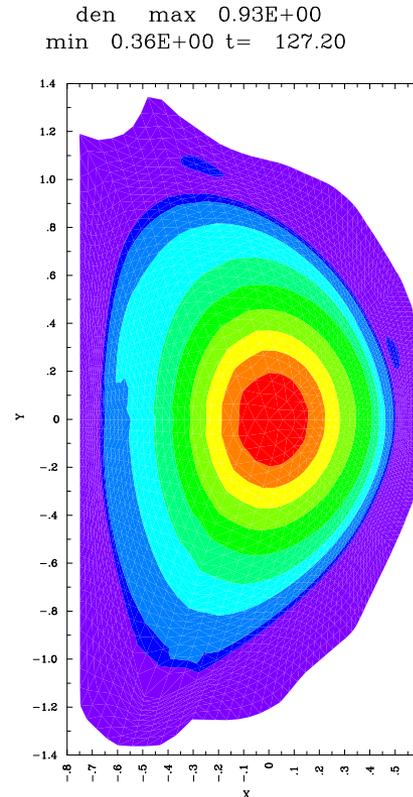


# Effect of rotation on density

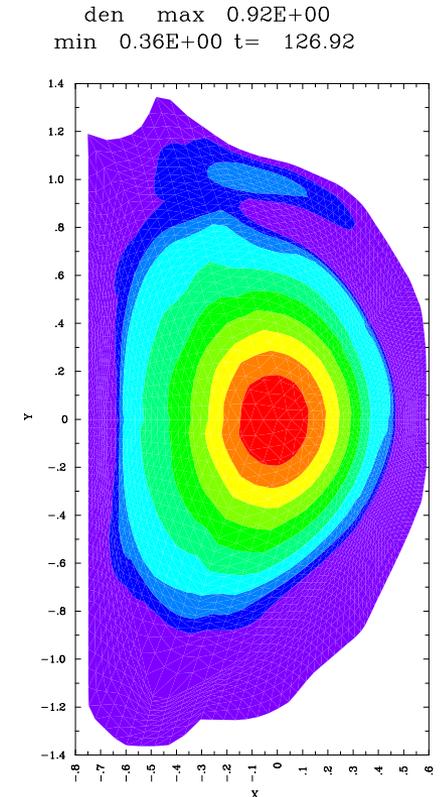
- The effect of rotation on the density is more complicated and more problematic numerically
  - Rotation causes density and pressure to deviate from magnetic flux surfaces
  - Temperature is a flux function because of high parallel thermal conduction
  - Toroidal rotation is more straightforward
  - Poloidal rotation can cause a density pedestal (MHD H mode) and shocks (Betti and Friedberg, PoP 2000)
    - Flux surface averaged sound speed vanishes at separatrix
    - Poloidal rotation at the separatrix is supersonic

# Density with toroidal rotation and RMP

- With toroidal rotation there is density loss even without the RMP. With the RMP the loss is enhanced. Density perturbations on open field lines tend to flow to an x-point
  - In this case there is an x-point at the top, outside the boundary, as well as at the bottom



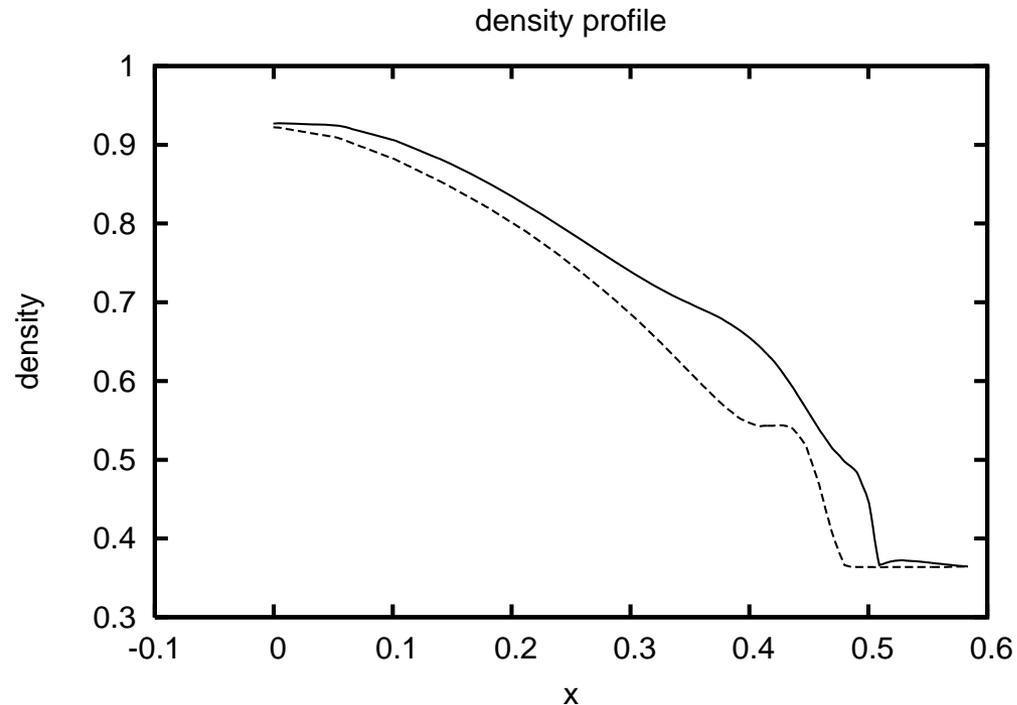
Density with  
No RMP



Density with  
RMP

# Density profiles with toroidal rotation and RMP

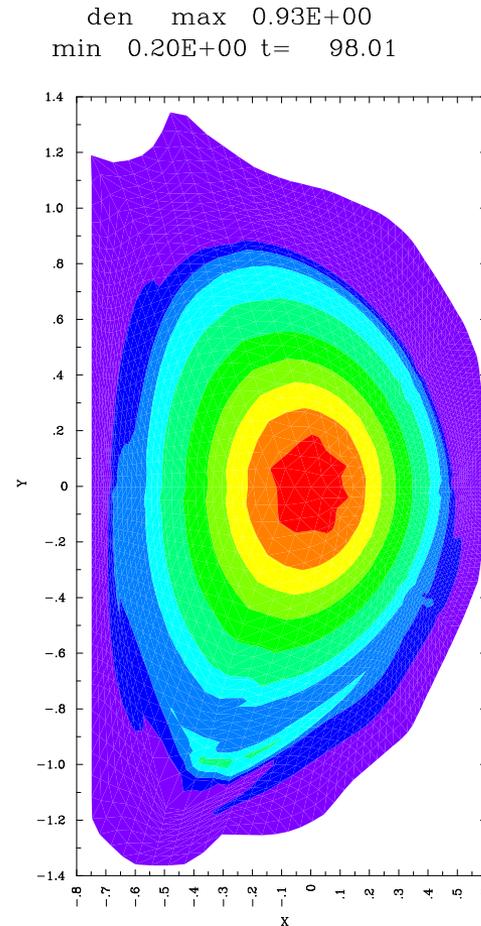
- Density profiles along the midplane are compared with toroidal rotation with and without the RMP. In comparison to the temperature perturbations, the density perturbations extend into the plasma core



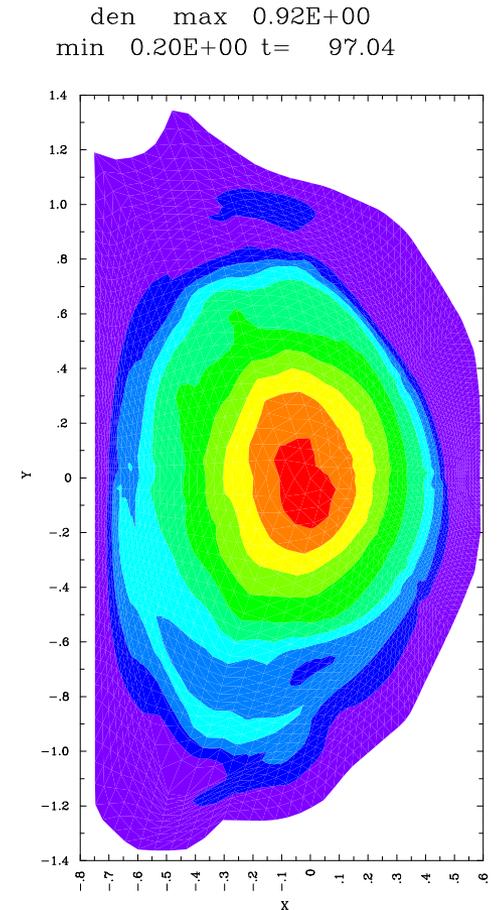
# Poloidal and toroidal rotation

- Poloidal and toroidal rotation were combined. This is more problematic numerically. To get cleaner results, a free boundary Grad Shafranov solver with flow is being developed.
- The initial poloidal velocity is of the form

$$\vec{v}_{pol} \propto \nabla T \times \nabla \varphi$$



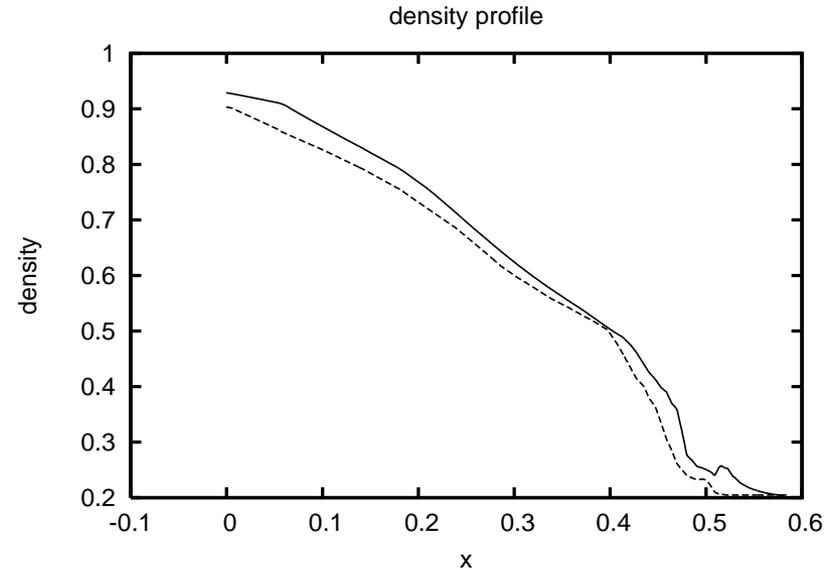
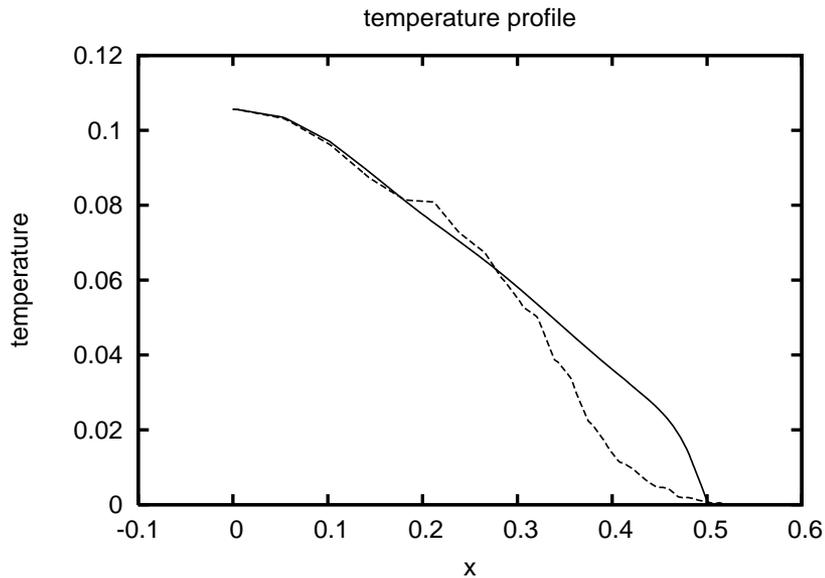
Density without  
RMP



Density with  
RMP

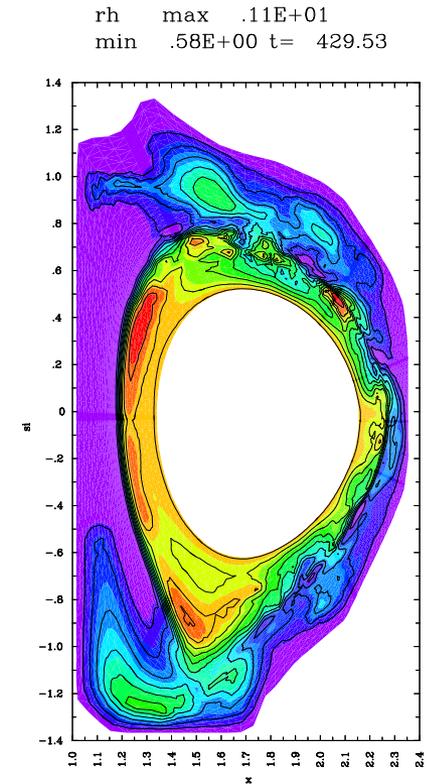
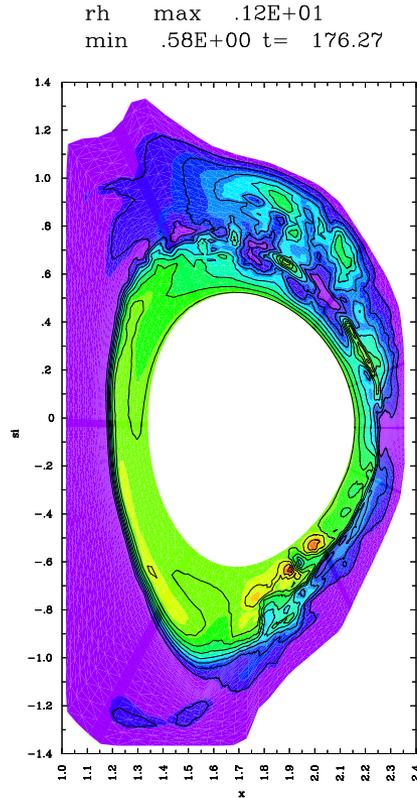
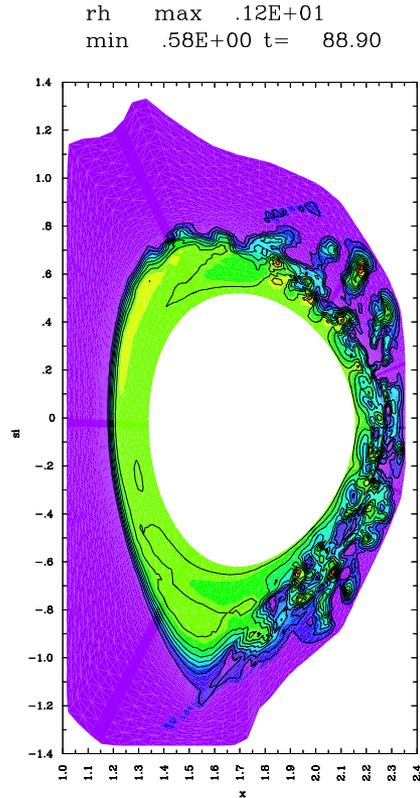
# profiles of temperature and density

- In this case the flows are smaller and the temperature perturbations are larger, although they do not extend to the core, while the density perturbations do.
  - Solid lines: no RMP, dashed lines: with RMP



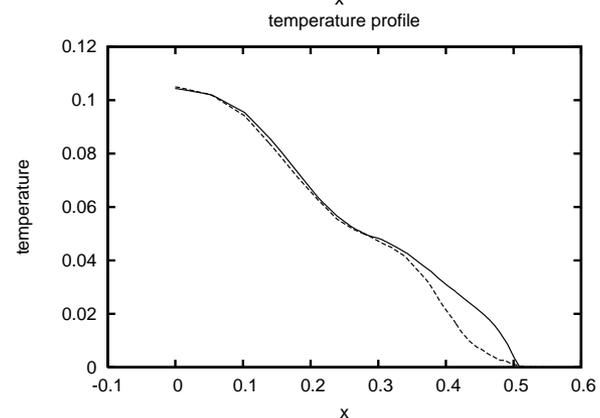
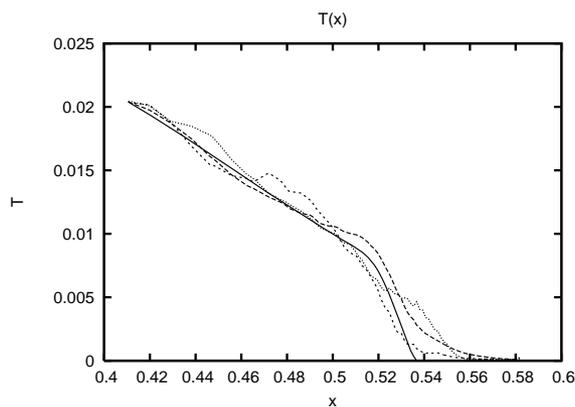
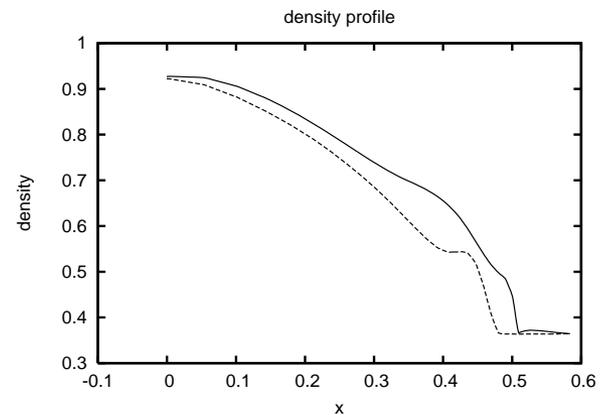
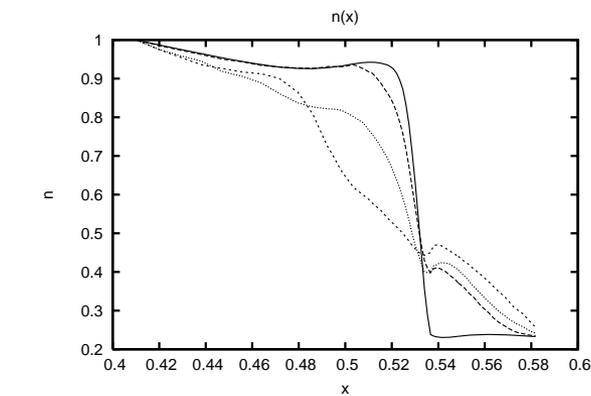
# Long time ELM simulations

- ELM simulations have been extended in time well beyond saturation
  - Methods: upwinding, nonlinear smoothing, dealiasing
- Resemblance to RMP
- Convergence criterion for coupling to XGC (CPES)



# ELM - RMP

- Density perturbations are larger than temperature perturbations
  - Temperature perturbations are localized to stochastic layer



ELM

RMP

# RMP summary

- RMP is affected by rotation
  - Plasma rotation screens the RMP from the plasma
    - Shrinks islands and reduces overlap to thin edge layer
    - stabilizes resistive mode excited by the RMP
  - RMP penetration profile depends on rotation profile
    - To get penetration as in GY Park model, need edge poloidal rotation
      - Free boundary G – S solver with flow will help
      - Need to stabilize resistive mode with less rotation
    - Present results like collisional RMP
- RMP resembles ELM
  - Temperature perturbations are local to edge
  - Density perturbations are non local
  - Density flows to x points

# M3D – XGC coupling

- Long time ELM simulations could reach relaxation stage
  - Convergence criterion introduced in M3D-MPP
    - Relative density fluctuation level below criterion, after ELM saturation
    - Variables averaged in toroidal angle and written out
    - M3D-OMP flux surface averages to get profiles
    - M3D-OMP computes new Grad Shafranov equilibrium
    - XGC computes new profiles
- Add rotation to G-S solver in M3D-OMP
  - XGC calculates radial electric field
  - Need free boundary equilibria with flow
- RMP
  - XGC with 3D magnetic field calculates profiles and radial E field
  - M3D calculates 3D magnetic field and 3D motion

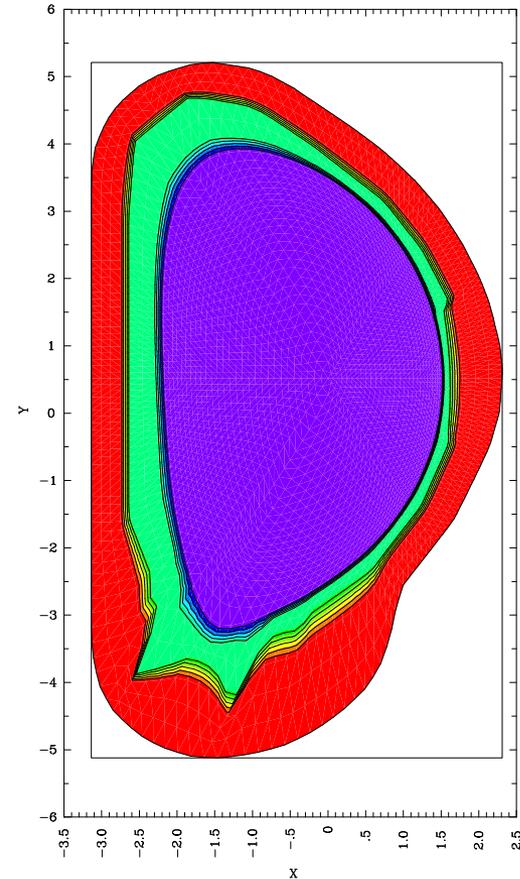
# Resistive Wall Modes

H. Strauss  
R. Paccagnella  
J. Breslau

# ITER resistive wall model

- ITER has 2 walls: 1<sup>st</sup> wall and vacuum vessel 2<sup>nd</sup> wall
- 2 models used in M3D
  - “no outer wall”: impenetrable resistive 1<sup>st</sup> wall
  - “outer resistive wall” : impenetrable 1<sup>st</sup> wall with continuous magnetic field, resistive 2<sup>nd</sup> wall, highly resistive region between 1<sup>st</sup> and 2<sup>nd</sup> walls

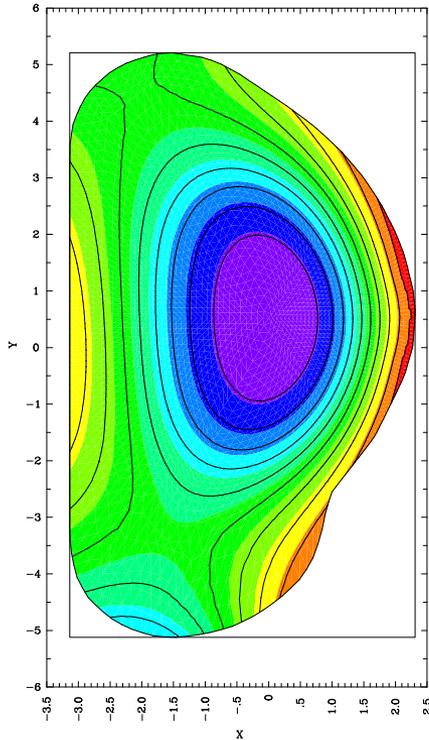
g max 0.20E+01  
min 0.00E+00 t= 97.13



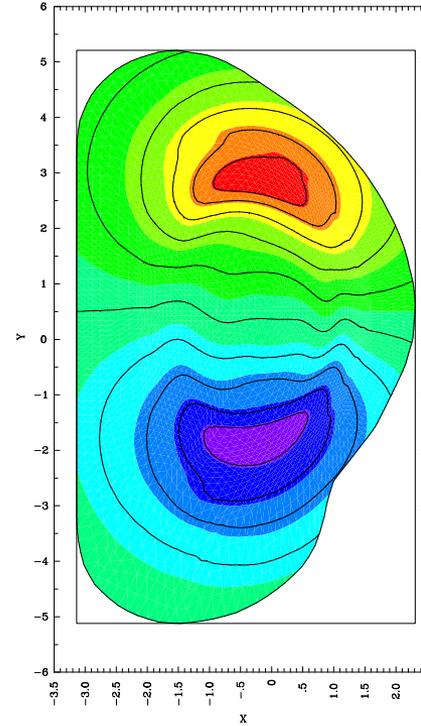
# 2 wall RWM

- Linear RWM calculated with 2 wall model
- AS Equilibrium and perturbed poloidal magnetic flux

a max 0.50E+00  
min -0.18E+01 t= 48.56

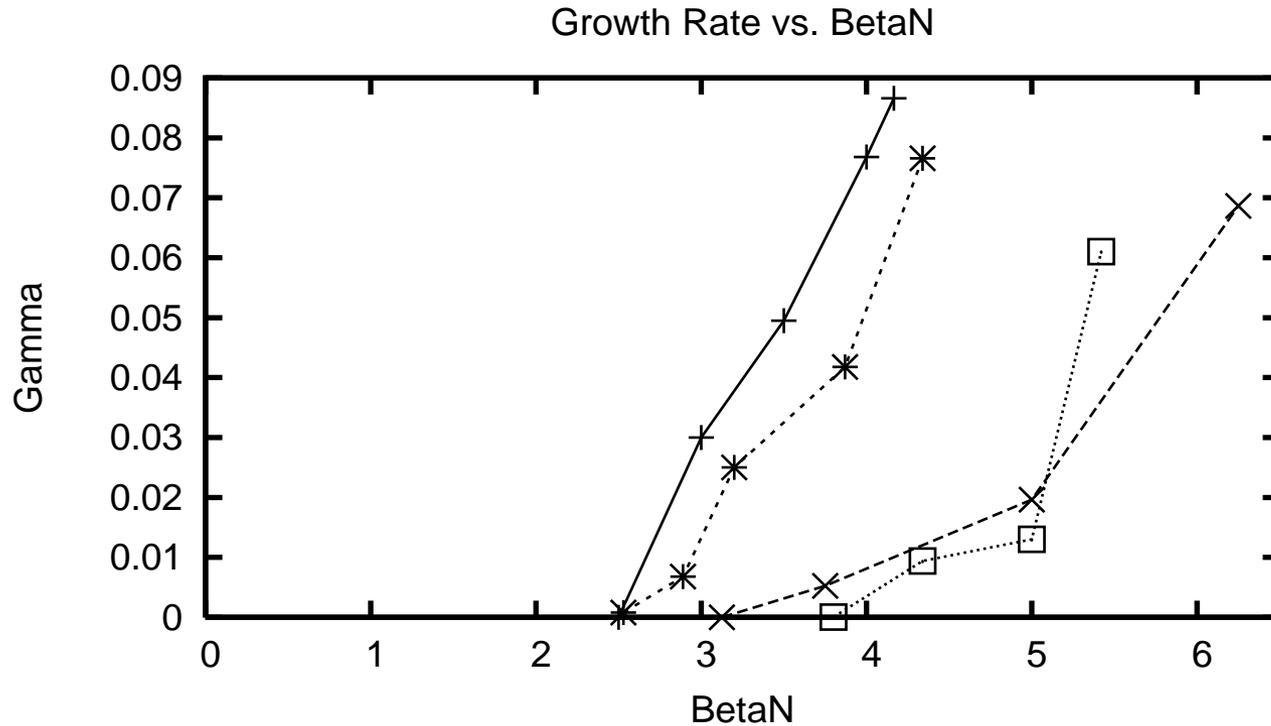


a prt max 0.14E-04  
min -0.13E-04 t= 97.13



# M3D – MARS comparison

- “no outer wall” and 2 wall linear growth rates were compared
- MARS: curves marked with + and boxes
- M3D: curves marked with \* and x



# M3D RWM status

- M3D-MPP 1 wall model is implemented
  - Used for linear simulations in MARS comparison
- 2 wall model
  - Implemented in M3D-OMP
  - Also implemented in M3D-MPP, but has some problems
- Green's function method for 2 walls is preferable