


Recent Advances in the Theory of Low-pressure Discharges

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Outline

May you have the hindsight to know where you've been, the foresight to see where you're going and the insight to know when you're going too far...

- Introduction to low-pressure discharges.
- Nonlocal electron kinetics in low-pressure discharges.
- Nonlinear transport of negative ions in plasma sources.

Outline

- Introduction to low-pressure discharges.
- Nonlocal electron kinetics in low-pressure discharges..
- Nonlinear transport of negative ions in plasma sources.

Applications of Glow Discharges

- Plasma processing of materials
- Lighting
- Gas discharge lasers
- Plasmas for electric propulsion
- Plasmas for pollution control and reduction
- Plasma isotope separation

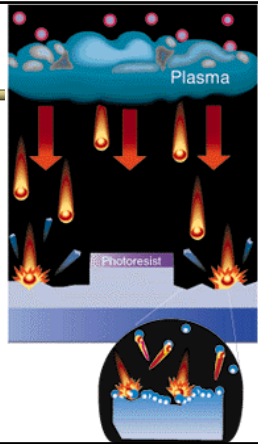
Plasma Parameters

- Plasma density $10^8 - 10^{12} \text{ cm}^{-3}$
- Gas pressure few mTorr – atmosphere
- Small degree of ionization $< 10^{-4}$
- Electron temperature T_e - few eV
- Ion temperature T_i - 0.03 eV
- Spatial scale mm- m

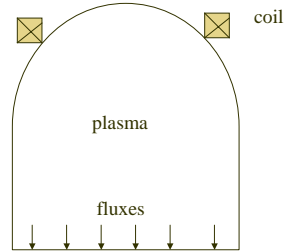
Motivation

- *Low temperature plasmas* are popular for technology.
 - Most remote from thermodynamic equilibrium.
 - $T_e(3\text{eV}) \gg T_i(0.03 \text{ eV})$.
- Parts of the EDF are very flexible and almost independent.
 - EDF = several weakly connected populations.
 - Small degree of ionization $< 10^{-4} \Rightarrow v_{ee} \ll v_e$.

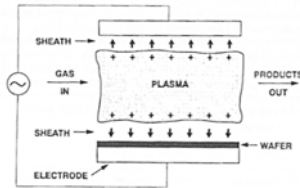
Plasma is Needed for the Etch Process



Plasma Can Produce Uniform Fluxes



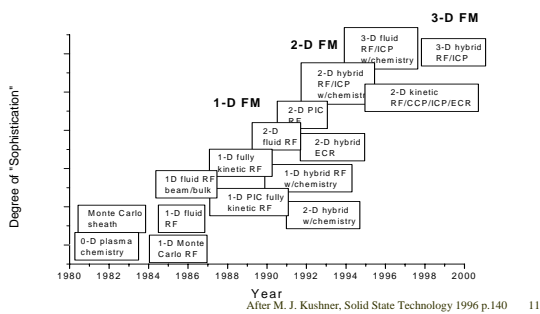
Schematic of Capacitive Discharge Plasma Reactor



Needed Fluxes of Radicals and Ions

- Composition
- Energy and angular distributions
- Uniformity
- Influence of external discharge parameters

Timeline for Evolution of Plasma Equipment Models



Limitations in Numerical Procedures

Disparity of time scales

- Etching 100s
- gas residence 0.1s
- ion residence 10^{-5} s
- ion residence 10^{-7} s in the sheath
- discharge voltage period 10^{-8} s
- electron residence 10^{-9} s in the sheath

Limitations in Numerical Procedures

Electric fields

Sheath ~ 1 kV/cm

Plasma ~ 1 V/cm

Spatial scales

Debye radius $\sim 10^{-3}$ cm

Plasma slab ~ 10 cm

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Is There Any
Interesting Physics
to Discuss



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Is There Any Interesting
Physics to Discuss?

Yes!
Electron Energy Distribution
Functions (EEDF)

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Outline

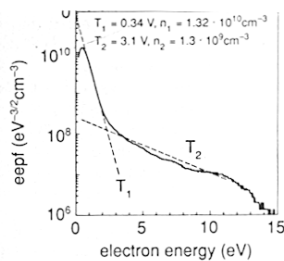
Introduction to low-pressure discharges.

● **Nonlocal electron kinetics in low-pressure discharges.**

Nonlinear transport of negative ions in plasma sources.

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Non-Maxwellian Electron Energy Distribution Functions



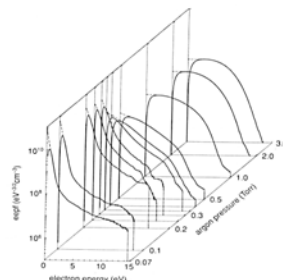
FOR MORE INFO

V.Godyak R.Piejak PRL 65 996
Argon 0.1 Torr, $f=13.56$ MHz, $L=2$ cm

2. The EEPF (lower) and normalized EEDF (upper),
obtained for $p=0.1$ Torr and $I_d=0.3$ A rms.

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EEDF Can Drastically Change for Different Discharge Conditions



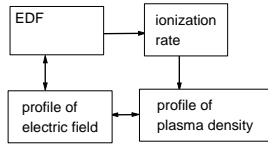
FOR MORE INFO

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Argon 0.1 Torr, $f=13.56$ MHz, $L=2$ cm

FIG. 3. The EEPF evolution with changing argon pressure,
 $I_d=0.3$ A rms.

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Why to Care About EEDF ?



“Heart-Body”=
EEDF-Discharge

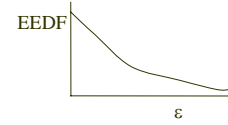
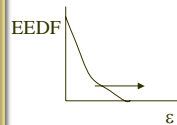
EEDF engineering = “Heart Surgery”

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Mechanism of EEDF formation: Heating



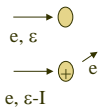
Elastic collisions with mean free path $\lambda \Rightarrow$
Random space diffusion yields \Rightarrow
Diffusion in energy with energy kick $eE\lambda$



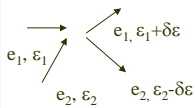
Diffusion in energy leads to heating

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Mechanism of EEDF formation: cooling and mixing



Cooling is due to energy losses in inelastic collisions.



Mixing is due to electron-electron collisions.

It is the only mechanism to make EEDF a Maxwellian!

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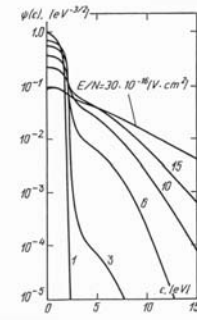
EEDF: stationary uniform E/P

1930 Druyvesteyn's EEDF
for λ constant.

$$f \sim \exp(-\varepsilon^2/\varepsilon_0^2)$$

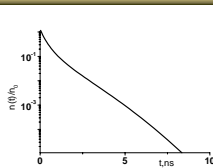
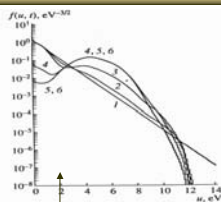
Real cross-sections in N_2

N.L. Alexandrev, et.al. Sov. J. Plasma Phys. 1978



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EEDF in decaying plasma



Strong energy losses

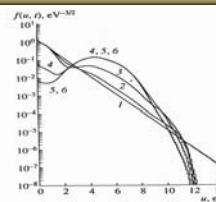
EDF afterglow Ar:NF₃, E/N=2 10⁻¹⁷Vcm²

- 1, 2, 3, 4, 5, 6.
- 0, 0.25, 1, 3, 5, 10 ns.

N.A. Dyatko, et.al. Plasma Phys.Rep. 1998

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Non-monotonic EEDF yields Negative Plasma Conductivity!

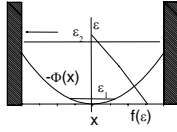


Total electron flux is against the electric field

$$\mu = -\frac{2e}{3m} \int u^{1/2} \lambda \frac{df(u)}{du} du < 0$$

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Evaporative Electron Cooling in Afterglow



In non-uniform plasmas
Low-energy electrons are trapped,
where as high-energy electrons can leave.

Electron temperature can cool to 30K! Biondi (1954)



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Evaporative Electron Cooling in Afterglow

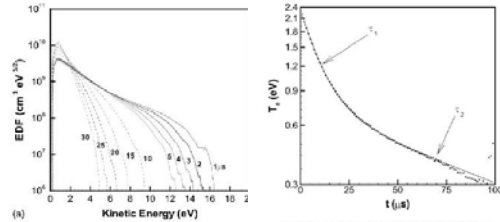


Fig. 7. Decay of the "electron temperature" at 15 nTorr.

Experiment: Kortshagen, et al. Appl. Surf. Sci. 192, 244 (2002)
Similar to Godyak's, but ID=14cm, L=10cm

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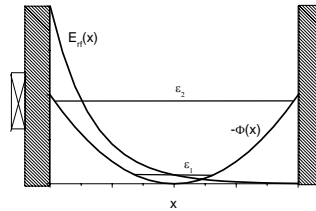
The Abrupt Formation of Large Population of Cold Electrons

- Large population of cold electrons is typical in various glow discharges.
- "Paradoxical" electron cooling with power increase.
- Plasma density jumps.

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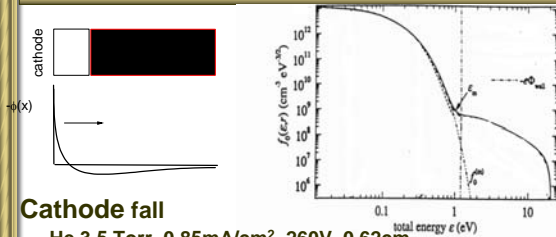
Cold Electrons: Explanation

- Necessary conditions:
 - Non-locality
 - Non-linearity



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Cold Electrons in DC Discharge

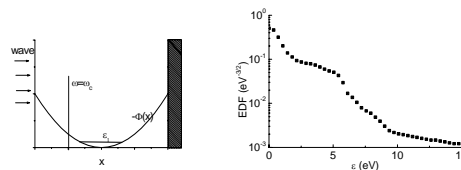


Cathode fall

He 3.5 Torr, 0.85mA/cm², 260V, 0.62cm
Exp.: $T_e=0.12\text{eV}$
E.A. Hartog et. al. PRL 1989
Model.: R.Araslanbekov, A.Kudryavtsev PRE 1998

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Cold Electrons in ECR discharge



Electron cyclotron resonance discharge

- N₂ 1mTorr, 0.14W/cm², 50cm
- Exp.: N. Bibinov et.al. Rev. Sci.Ins. 1998, 2004
- Model.: I. Kaganovich et.al. PRE 1999

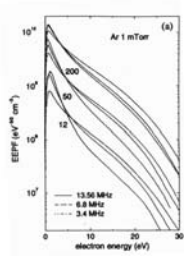
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Cold Electrons: ICP



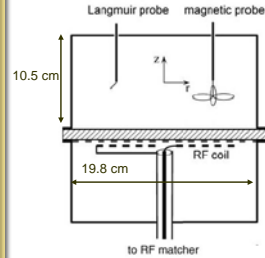
Inductively coupled discharge

- Argon 1mtor,
- Pancake geom. 20x10.5cm
- V A Godyak & V I Kolobov PRL 1998



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Godyak's Experiment is Benchmark.



The Inductively Coupled Plasmas (ICP) in a cylindrical stainless steel chamber as shown in Fig.1.

Measurements were made at

$f=0.45\text{-}13.56\text{ MHz}$

in argon gas pressures of 0.3-300 mTorr and

rf power dissipation in the plasma 6-400 W.

Figure 1. Experimental discharge chamber.

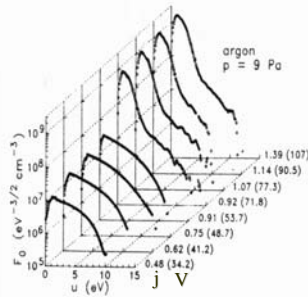
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Explosive Generation of Cold Electrons in Capacitive Discharge

EEDF evolution with discharge current

Argon, 13.56MHz, 6cm, 9Pa

U. Buddemeier et.al. APL (1996)



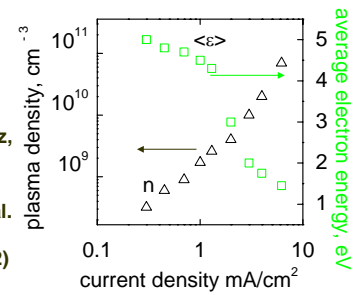
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"Electron Refrigerator"

Plasma evolution with current

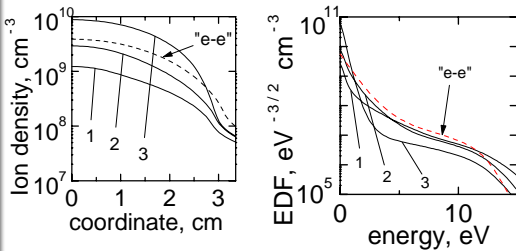
Argon, 13.56MHz, 6.7cm, 0.1torr

Symbols: exp. V.Godyak et. al. Plasma Sci. & Technol. (1992)



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Modeling: Absence of Steady State



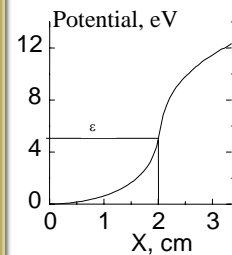
The EDFs and ion density profiles at three subsequent times

Solid lines: e-e collisions are ignored. 1 - $t = 0$ ms, 2 - $t = 0.34$ ms, 3 - $t = 2.24$ ms.

Dashed lines: with e-e collisions

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Nonlocal Approach -Averaging Over Fast Electron Bouncing



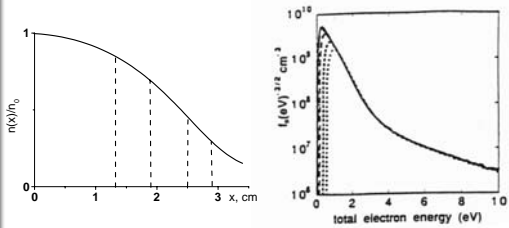
$$\epsilon = \frac{mv^2}{2} + e\Phi(\vec{r})$$

$$F(\epsilon)$$

I.B.Bernstein, T.Holstein. Phys. Rev. **94**, 1475 (1954).
L.D. Tsendin. Sov.Phys. - JETP, **39**, 805 (1974).

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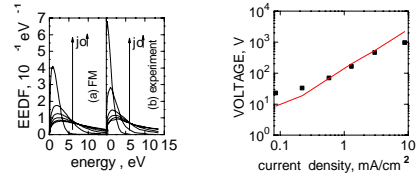
Nonlocal EEDF is a function of total energy $\varepsilon = mv^2/2 - e\phi(x)$



Experimental EEDF's at different positions
capacitively coupled RF discharge in argon 0.03 Torr, 13.56 MHz;
V A Godyak and R B Piejak, APL 1993

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Results of Fast Modeling



He, $p=0.1$ torr, $\omega=13.56$ MHz, $L_0=3.35$ cm.
Experimental data - filled squares, the FM results - solid line
 $j_0=0.085, 0.22, 0.58, 1.3, 6.0, 8.8$ mA/cm².

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Results of Fast Modeling

- Speed up ~100-1000 times
- Consistent with experimental data and full scale modelling CCP, ICP and ECR
- Discovery of new phenomena
 - Explosive generation of cold electrons

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