



Scaling Properties of the M3D Code From CDX to ITER

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FDM3D Workshop, Princeton

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Background: Large scale sparse linear systems

¹1N: $\Delta^\perp u = f^\perp$, Neumann boundary condition

²1D: $\Delta^\perp u = f^\perp$, Dirichlet boundary condition

³2D: $\Delta^* u = f^*$, Dirichlet boundary condition

⁴3D: $\Delta^\dagger u = f^\dagger$, Dirichlet boundary condition

⁵4N: $(\Delta^\perp - \eta)u = f_g^\perp$, Neumann boundary condition

⁶4D: $(\Delta^\perp - \eta)u = f_g^\perp$, Dirichlet boundary condition

⁷4I: $(\Delta^\perp - \eta)u = f_g^\perp$, semi-implicit advancing of thermal conduction

⁸5D: $(\Delta^* - \eta)u = f_g^*$, Dirichlet boundary condition

⁹6D: $(\Delta^\dagger - \eta)u = f_g^\dagger$, Dirichlet boundary condition

Zero eigenvalue, Ill conditioned,
Null-space,
CG/ICC, Slow convergence, CG/AMG

$$\begin{aligned}\Delta^\perp &\equiv \frac{\partial^2}{\partial R^2} + \frac{\partial^2}{\partial Z^2} \\ \Delta^* &\equiv \Delta^\perp - \frac{1}{R} \frac{\partial}{\partial R} \quad \text{unsymmetric} \\ \Delta^\dagger &\equiv \Delta^\perp + \frac{1}{R} \frac{\partial}{\partial R} \\ &\Downarrow \\ &\text{Conserved form} \\ \Delta^\perp &\equiv \nabla \cdot \nabla \\ \Delta^* &\equiv \nabla \cdot \frac{1}{R} \nabla \quad \text{symmetric} \\ \Delta^\dagger &\equiv \nabla \cdot R \nabla\end{aligned}$$

Majority of the code time spent in these Linear Elliptic solvers:

~80%, GMRES/ILU

~33%, CG/AMG

significant speedup was observed for large problems, very scalabe.

Motivation: WHY

To optimize the code and prepare for petascale calculations.

M3D time can be broken down to 3 major parts:



Their efficiencies are critical for optimization on petascale computers.

An Example: Total M3D Time = 726 sec

- Physics = 240
- Linear Solver = 274 (optimized, otherwise >80%.)
- Data copy = 206

Outline: HOW

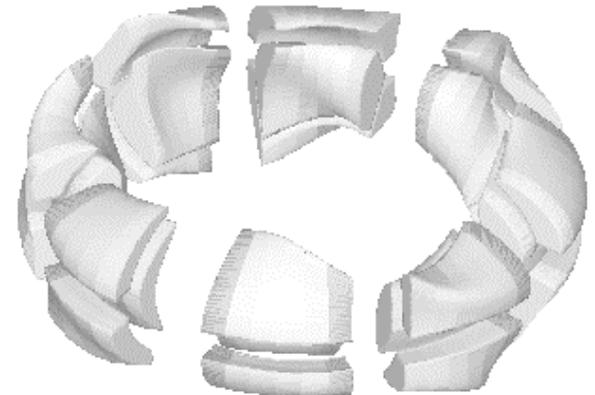
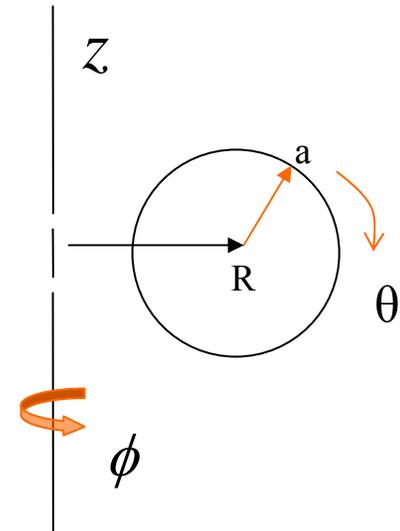
1. 3D (r, θ, ϕ) *strong* scaling
2. 3D (r, θ, ϕ) *weak* scaling
3. 1D (ϕ) *weak* scaling
4. 2D (r, θ) *weak* scaling

A, B, C, D, E, F

A geometry in in toroidal ϕ direction;
B CPUs in toroidal ϕ direction.

C geometry in minor radial r direction;
D CPUs in radial r direction.

E geometrt in poloidal θ direction;
F CPUs in poloidal θ direction.



Definitions

Physics grid: **A C E**

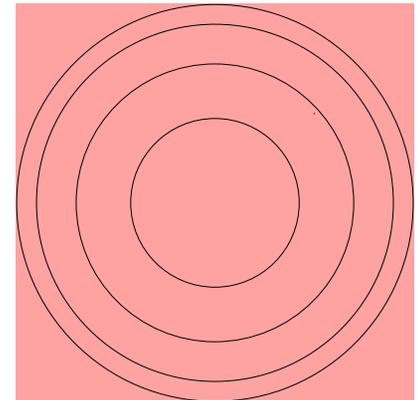
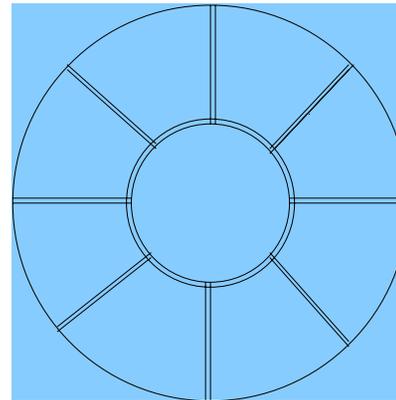
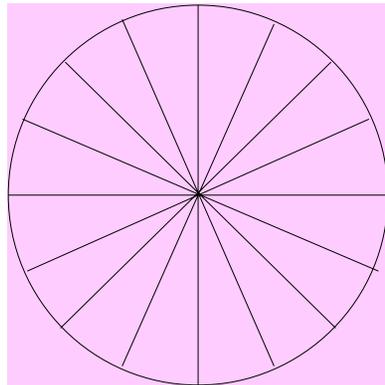
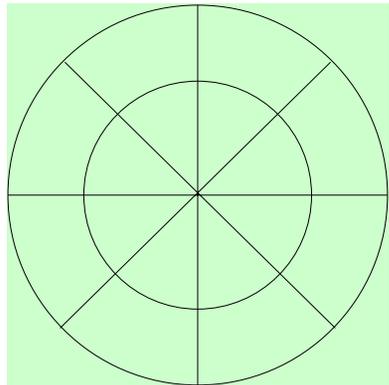
CPU grid: **B D F**

<p>1D (φ) <i>weak</i> scaling</p> <table> <tr> <td>A</td> <td>B</td> <td>C</td> <td>D</td> <td>E</td> <td>F</td> </tr> <tr> <td>a1</td> <td>b1</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>a2</td> <td>b2</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>:</td> <td>:</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>an</td> <td>bn</td> <td></td> <td></td> <td></td> <td></td> </tr> </table>	A	B	C	D	E	F	a1	b1					a2	b2					:	:					an	bn					<p>2D (r,θ) <i>weak</i> scaling</p> <table> <tr> <td>A</td> <td>B</td> <td>C</td> <td>D</td> <td>E</td> <td>F</td> </tr> <tr> <td></td> <td></td> <td>c1</td> <td>d1</td> <td>e1</td> <td>f1</td> </tr> <tr> <td></td> <td></td> <td>c2</td> <td>d2</td> <td>e2</td> <td>f2</td> </tr> <tr> <td></td> <td></td> <td>:</td> <td>:</td> <td>:</td> <td>:</td> </tr> <tr> <td></td> <td></td> <td>cn</td> <td>dn</td> <td>en</td> <td>fn</td> </tr> </table>	A	B	C	D	E	F			c1	d1	e1	f1			c2	d2	e2	f2			:	:	:	:			cn	dn	en	fn
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Strategy to improve data copy

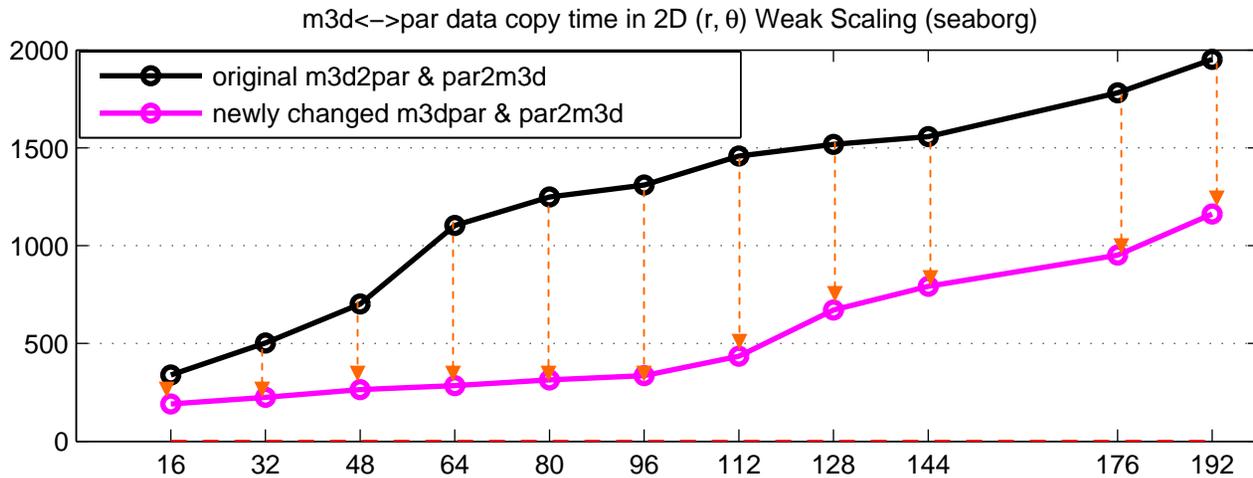
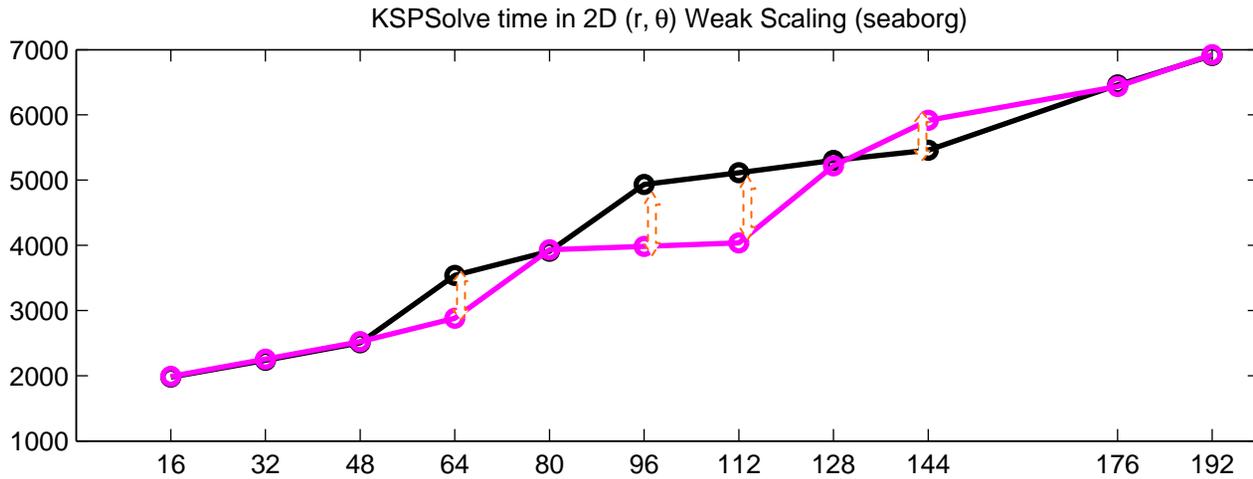
- a) Reduce toroidal ghost changes
- b) Reduce poloidal ghost changes:

2 times faster on seaborg



2D (r, θ) direction, C D E F

Strategy to improve data copy – II



Seaborg: NERSC IBM SP RS/6000.

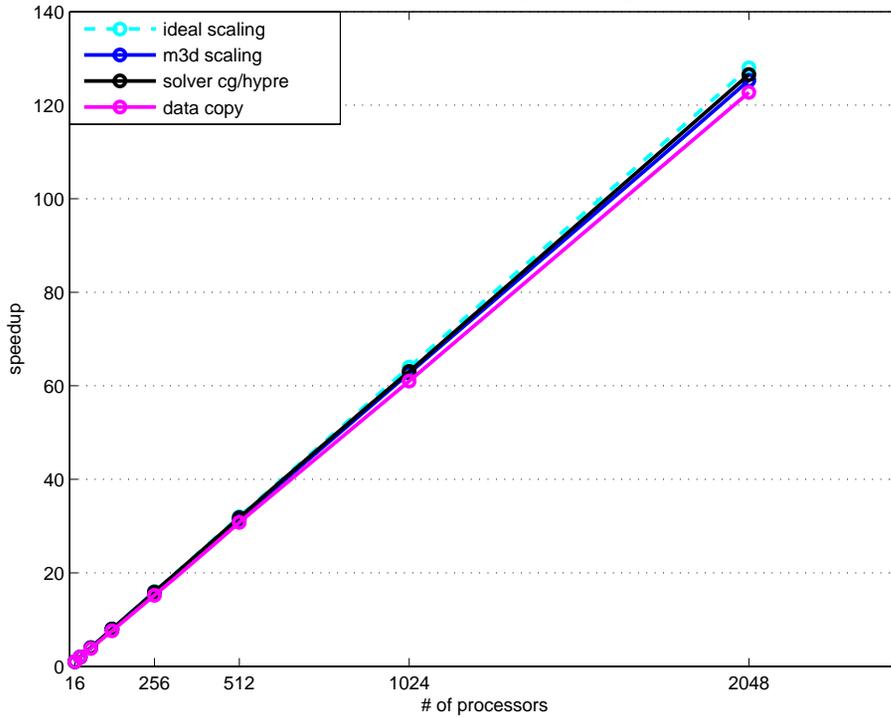


a distributed memory computer with 6,080 processors. Each processor has a peak performance of 1.5 GFlops. The processors are distributed among 380 compute *nodes* with 16 processors per node. Processors on each node have a shared memory pool of between 16 and 64 GBytes

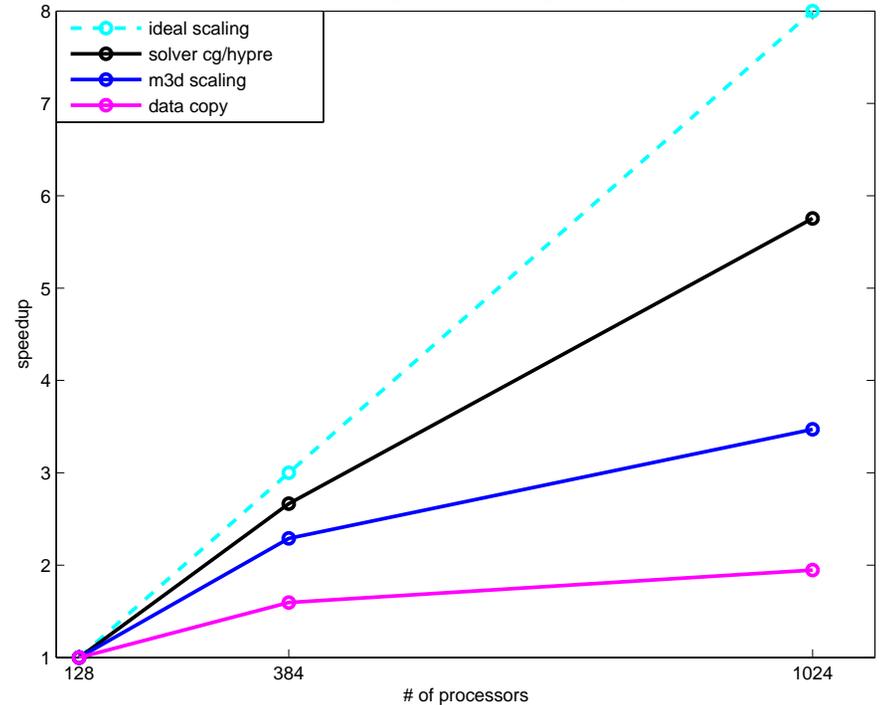


1D weak & 3D (r,θ,φ) strong scaling-till 10/29/2006

M3D weak 1D ϕ scaling on Seaborg



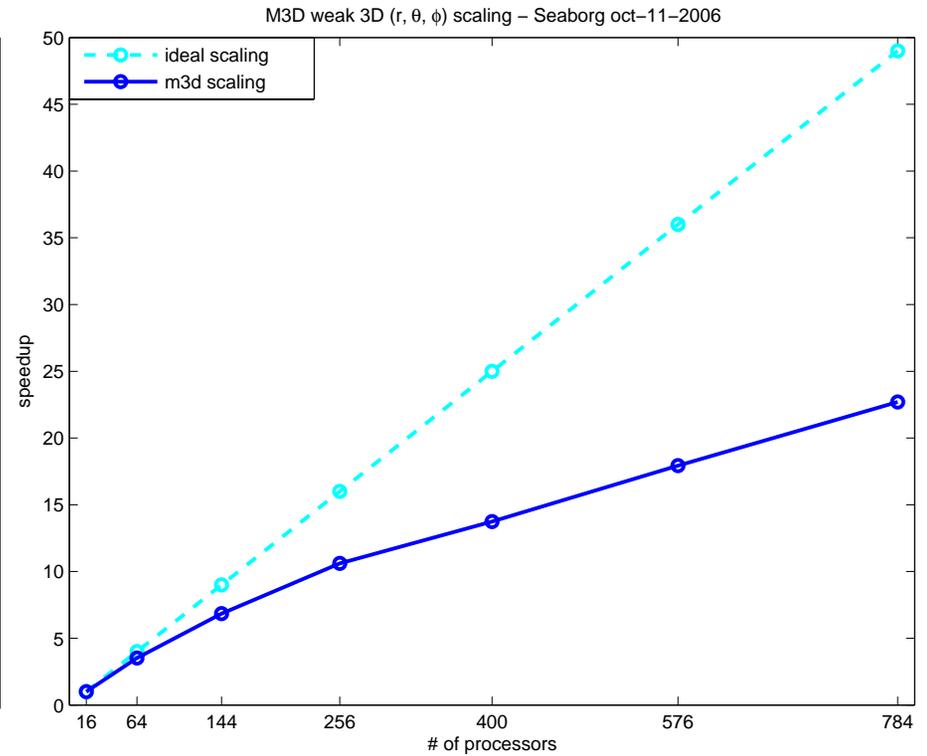
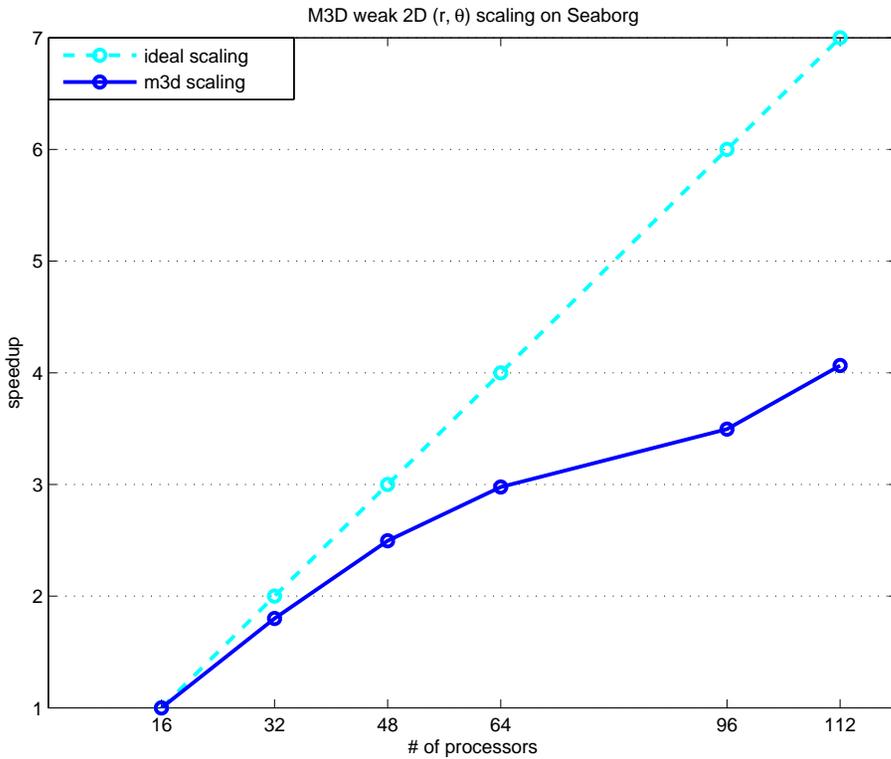
M3D strong 3D (r, θ, φ) scaling Seaborg



1D good; 3D not as good as 1D and can only go up to 1024 procs.



2D & 3D (r, θ, ϕ) weak scaling



2D and 3D not as good as 1D, and crashes beyond 112 or 784 procs.

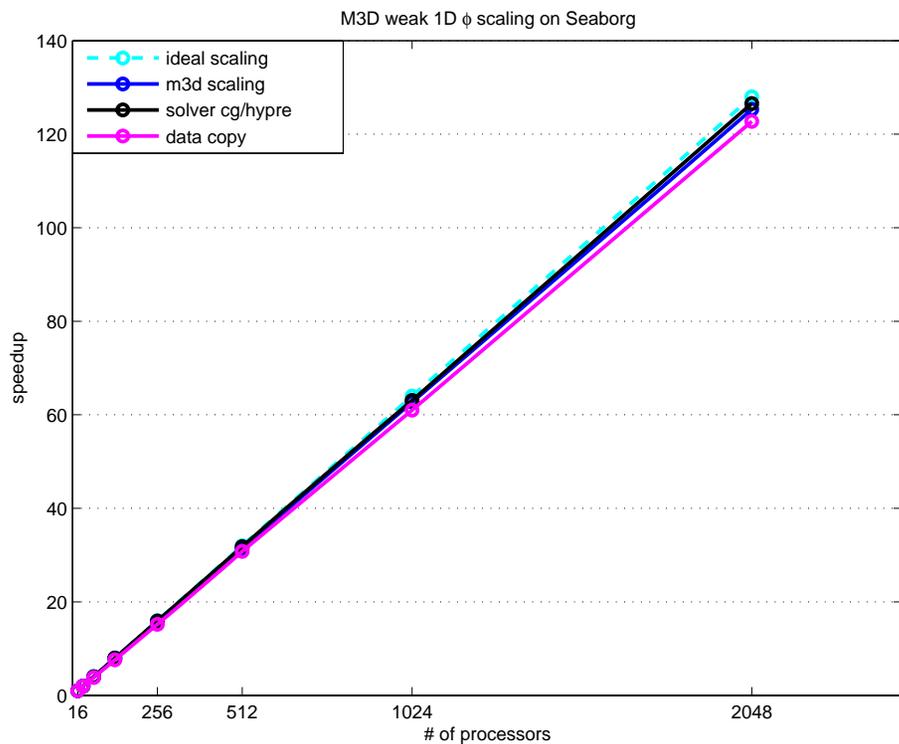
Jaguar: XT3



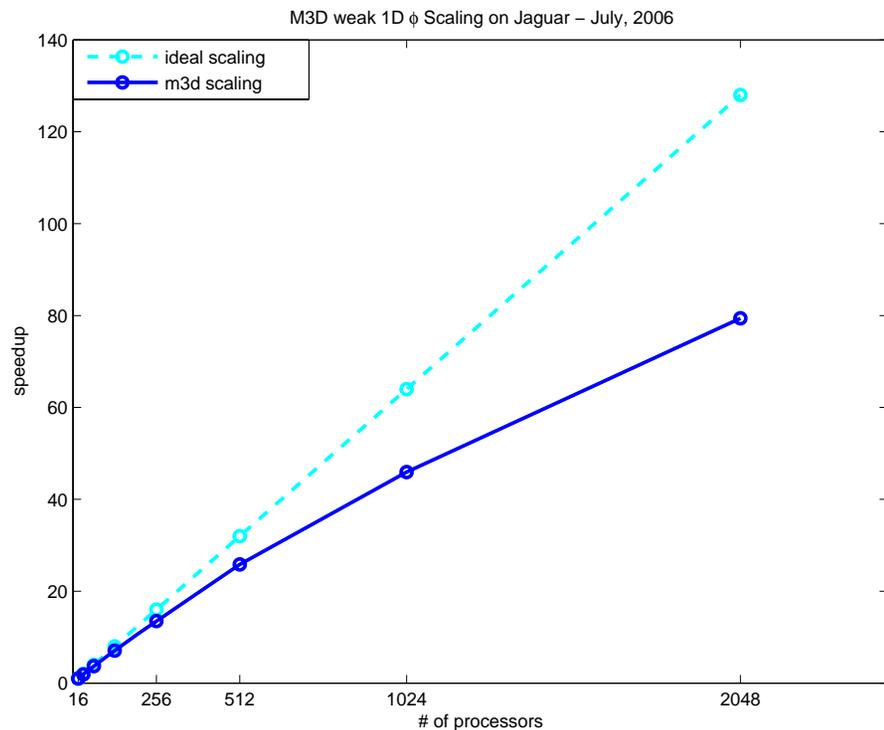
Compute-node processor count	10,424 cores <i>Note: 2 CPUs now share the memory and interconnect bandwidth of a single CPU before the upgrade</i>
Compute-node processor size	2.6 GHz dual core
Compute-node memory	4 GB <i>Maintaining 2 GB per core</i>
Lustre file system capacity	100 TB
Luster default stripe width	4 OSTs <i>The stripe size can be changed with the lfs stripesize command</i>
UNICOS/lc	Upgraded to 1.4.22 <i>Executables must be recompiled</i>
Interconnect	Full 3D torus



1D (ϕ) weak scaling-till 7/15/2006



seaborg



Jaguar: not comparable to seaborg



Problems fixed on Jaguar

- Runtime memory limitation
 - Solution: use only 1 processor per node

```
yod -SN m3dp_fsymm_opt.x ...
```

- Code crashes when the number of processor increases from 2048 to 3076 or 4096:

```
module load gmalloc
```

```
link -gmalloc as the last library to build m3dp.x
```

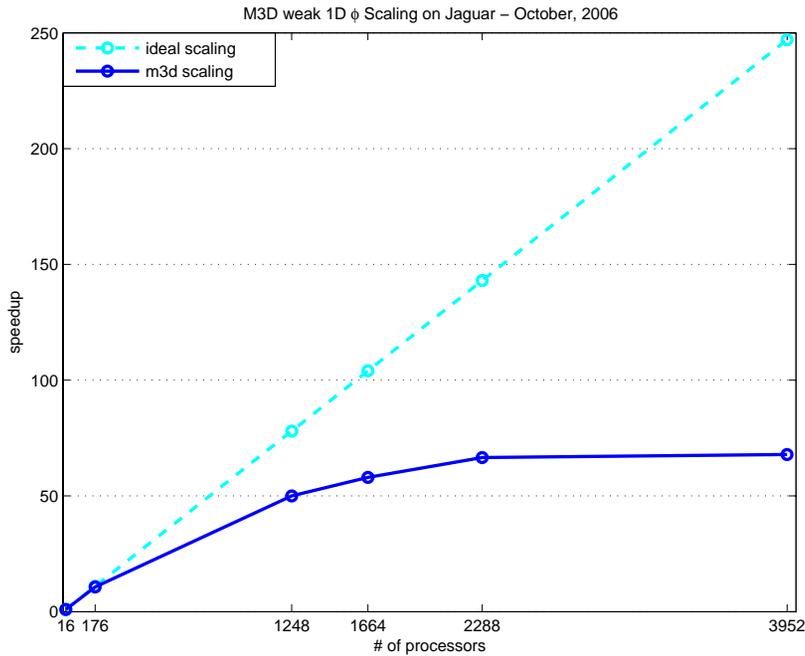
- Wait too long when debugging code
 - We need dedicated time to fix bugs only appeared on large number of processors.
- Fortran static array (stack)

```
yod -SN -stack 500M m3dp_fsymm_opt.x ...
```

All the problems were fixed after 9/15/06 upgrades.



1D (ϕ) weak scaling – till 10/26/2006



Communication:

	A	B	C	D	E	F
x	x	x	51	1	4	4
16						
176						
1248						
1664						
2288						
3952						

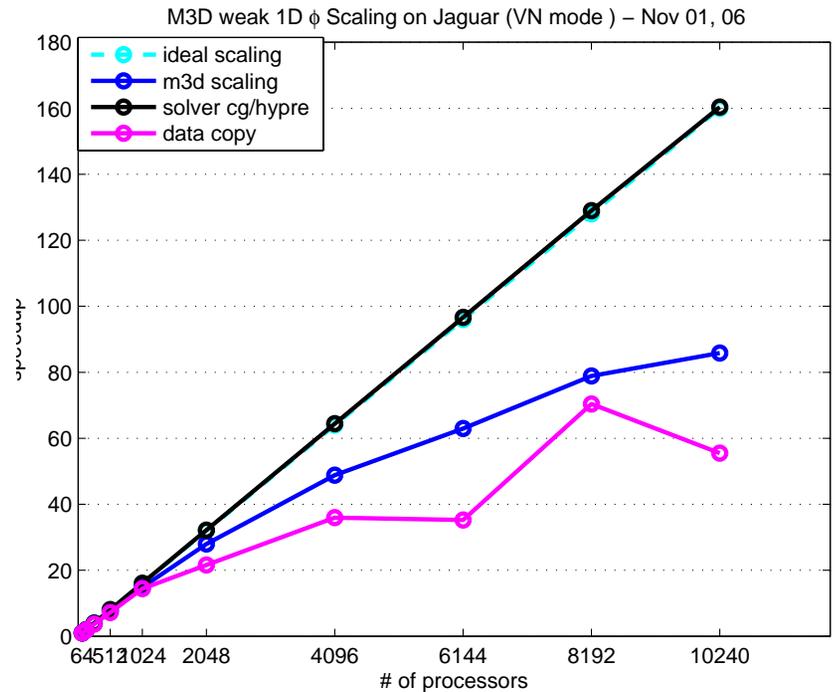
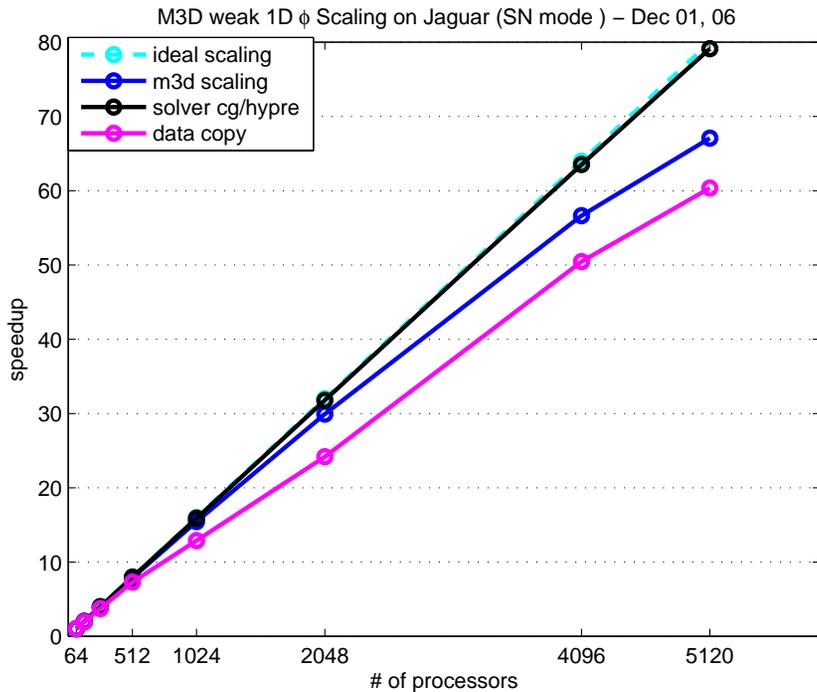
Heavy communication in ϕ direction compared to (r,θ) directions.

MPI I/O

Finally we can go up to 4000 procs by the end of October, 2006.



1D weak scale on the whole machine



Good up to 5000 processors; runs on > 10,000 proces, although not ideal.

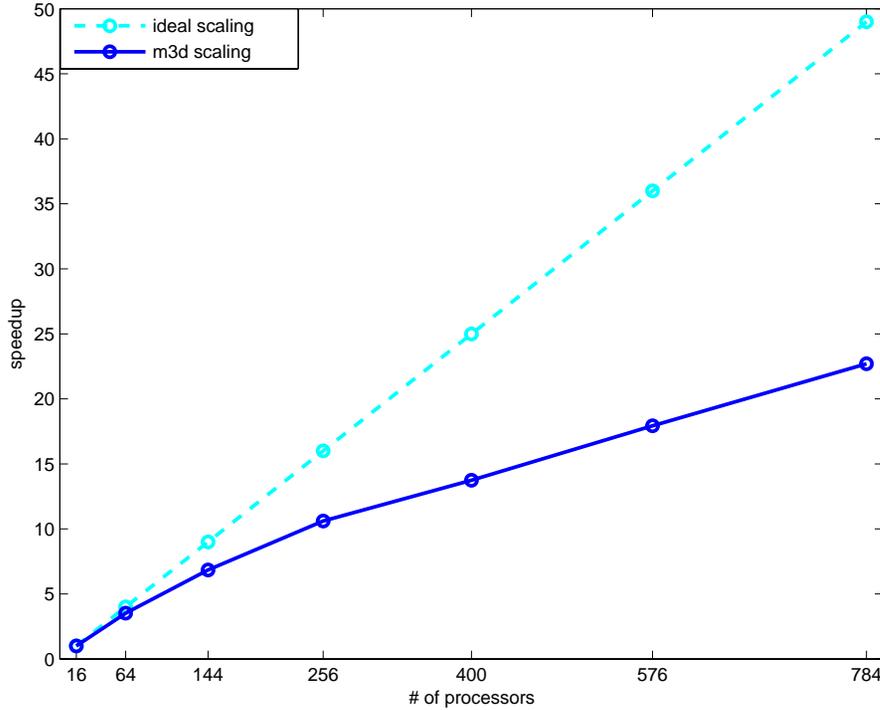
Problem size:

Vert= $C(C-1)/2 * E + 1 = 62,6081/\text{plane}$, total=(16, 32, 64, 128, 256, 512, 1024, 2048) times of Vert.



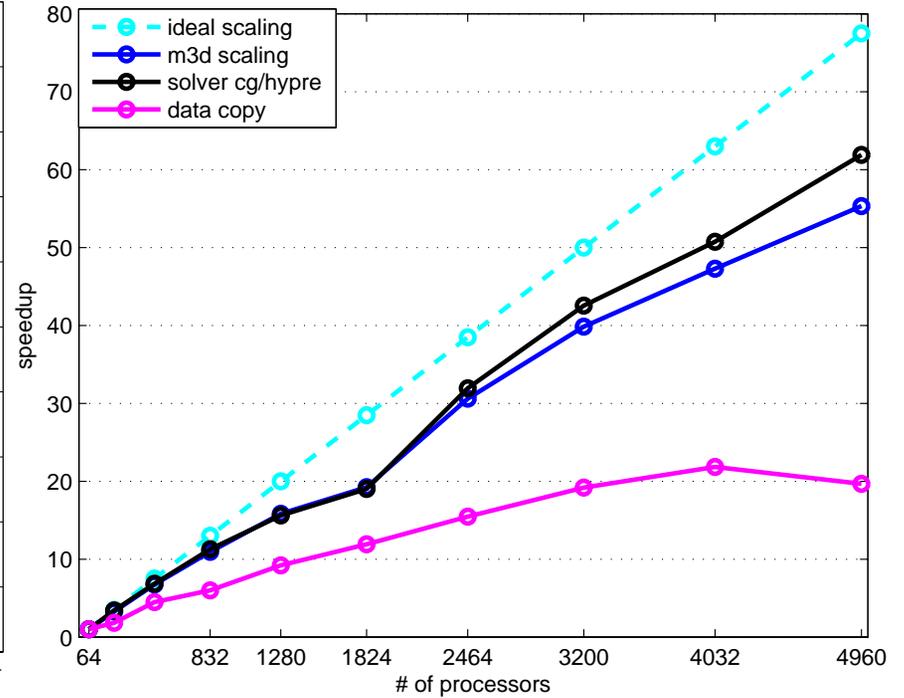
3D weak scale on the whole machine

M3D weak 3D (r, θ , ϕ) scaling – Seaborg oct-11-2006



Seaborg: ~800 procs

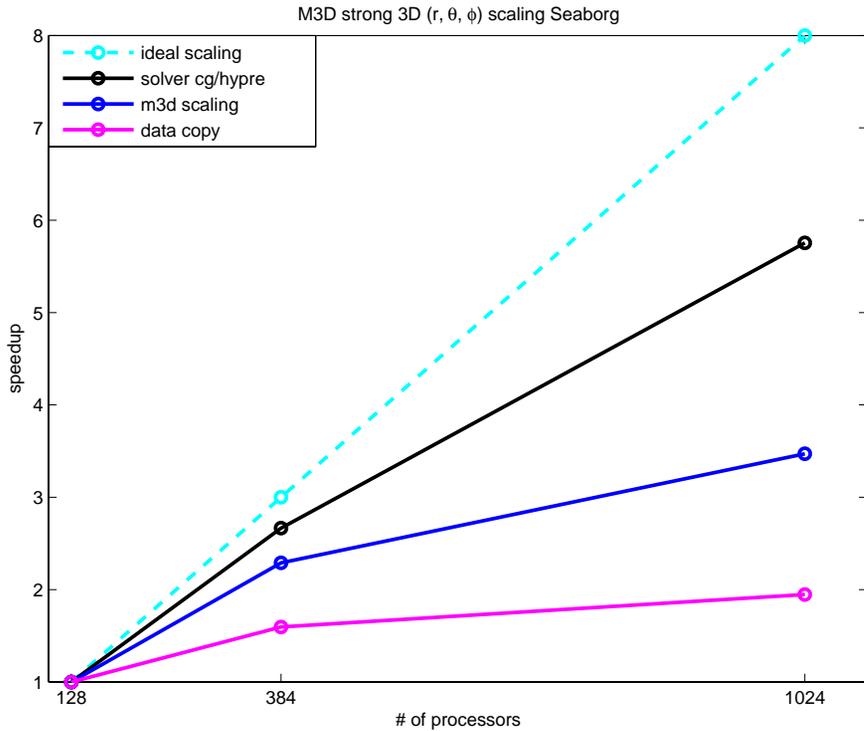
M3D weak 3D (r, θ , ϕ) Scaling on Jaguar (SN mode) – Jan 11 2007



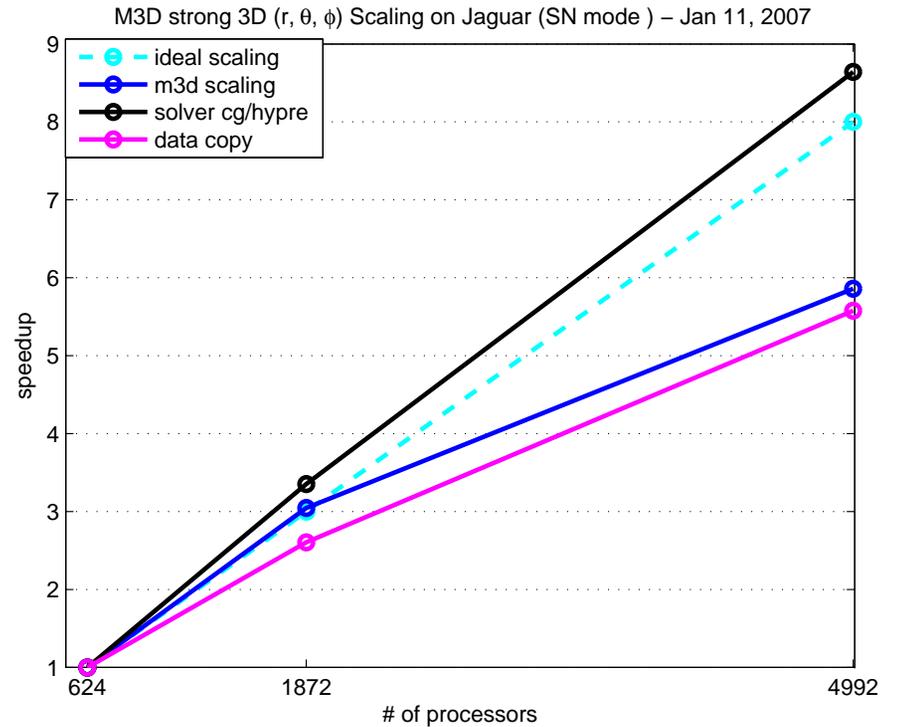
Jaguar: ~5000 procs



3D strong scale on the whole machine



Seaborg: 1024 procs



Jaguar: 5000 procs



MCS BGL Configuration

Compute - 1024 dual PowerPC 440 700MHz 512MB nodes

Storage - 14 TB of clusterwide disk (currently using the MCS Parallel Virtual File System (PVFS)) and 3.5TB of home directory filesystem.

Network - IBM BlueGene Torus, Global Tree and Global Interrupt

Running Jobs

`cqsub -t <time> -n <nodecount> -c <#processors> -m <mode> <exe> [arg1,arg2,...]`

<time> is in minutes (required)

<nodecount> is the number of nodes

<#processors> number of procs

<mode> is one of 'co' or 'vn'

<exe> is the full path name to the mpi executable
[arg1,arg2,...]

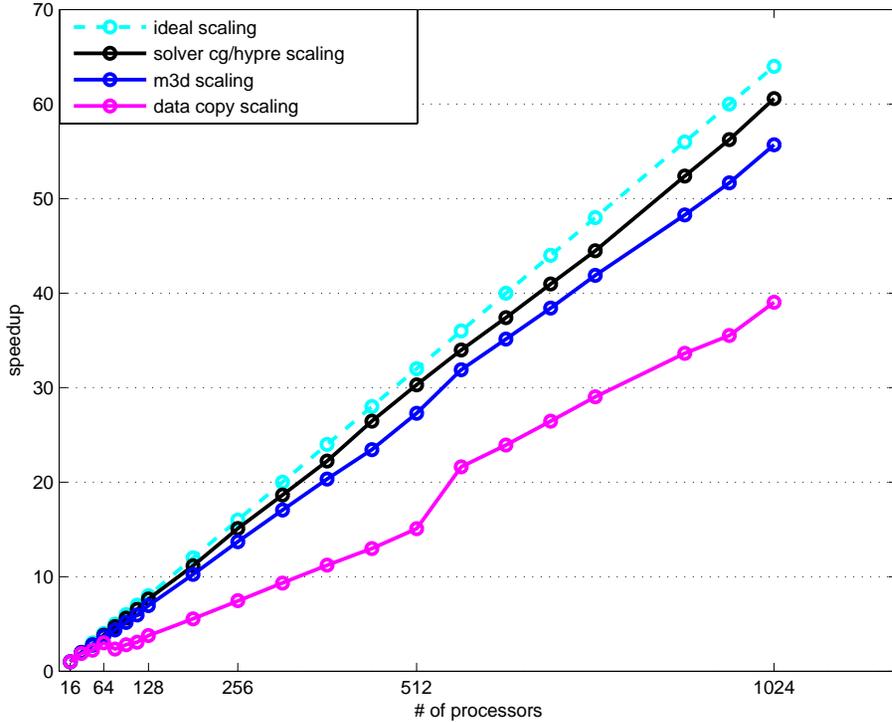
using a partition size smaller than 512, the code cannot use the [full Torus network](#). This will most likely cause the [performance to be very poor](#).

Desired Usage	Partition Size	# of processors
Development, Scaling	32	64
Development, Scaling	64	128
Development, Scaling	128	256
Development, Scaling	256	512
No Development	512	1024
No Development	1024	2048

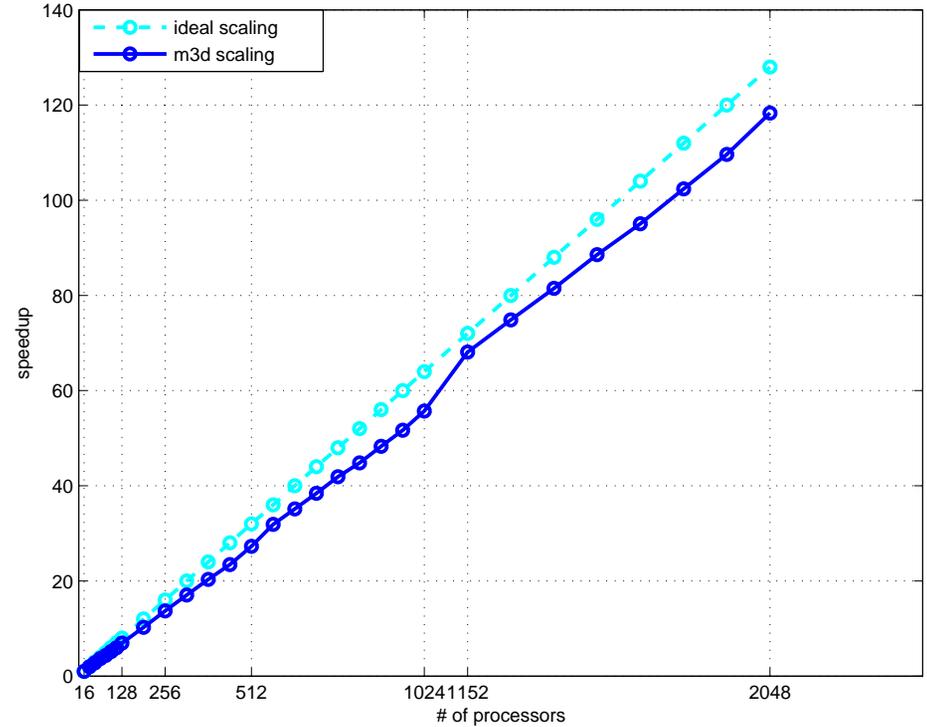


1D (ϕ) weak scaling

Weak 1D ϕ Scaling on BGL oct-25-2006, R=50



Weak 1D ϕ Scaling on BGL oct-31-2006, R=50



Doesn't have enough memory to push big runs.

As a result of scaling, code stretching ...

Meaningful,
Not nonsense!

- Fixed
 - physics bugs
 - memory bugs (not show up when using a small amount of memory)
 - coding bugs (not show up when Vert is small)
 - I/O bugs

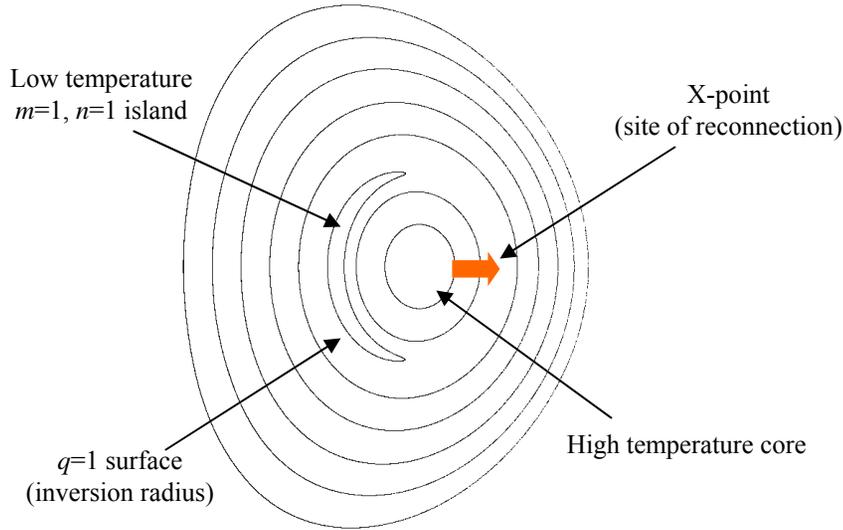
- Robust (ready to do comprehensive physics and get higher resolution)

$(A, B, C, D, E, F) = (32, 16, 51\sim 91, 1, 4, 4), \quad \text{Vert} = 5,100/(r,\theta) \text{ plane}$

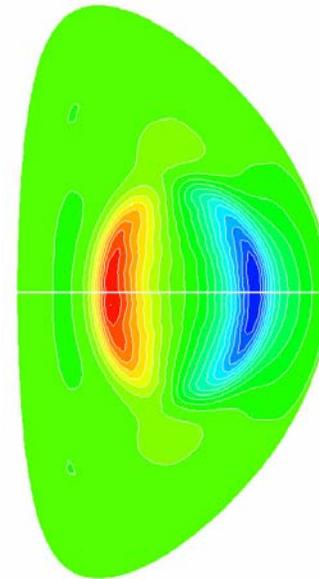
$(A, B, C, D, E, F) = (3952, 640, 560, 2, 13, 39), \quad \text{Vert} = 2,034,760/(r,\theta) \text{ plane}$

Franklin : Applications need high resolution

CDXU --> DIIIID --> ITER



Sawtooth Instability in CDXU



Nonlinear behavior of energetic particle modes in NSTX