

# **Hybrid Simulations of Alpha Particle Effects on MHD Modes in ITER**

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The 2005 American Physics Society meeting, DPP, Nov. 24-28, 2005

# Outline

- Introduction
- M3D code: hybrid model
- Recent highlights
- Internal kink, fishbone and TAE in ITER
- Summary

# Introduction

- We investigate stability of internal kink, fishbone and TAE in ITER by particle/MHD hybrid simulations;
- Our main tool, M3D, is a 3D global nonlinear extended MHD code.

# M3D code

M3D is an extended-MHD (XMHD) code which has multi-level of physics:

Resistive MHD;

Two fluids;

Particle/MHD hybrid;

# M3D XMHD Model

$$\rho \frac{d\mathbf{v}}{dt} + \rho(\mathbf{v}_i^* \cdot \nabla)\mathbf{v}_\perp = -\nabla P - \nabla \cdot \mathbf{P}_h + \mathbf{J} \times \mathbf{B} - \mathbf{b} \cdot \nabla \cdot \Pi_i$$

$$\mathbf{J} = \nabla \times \mathbf{B}, \quad \frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} = \eta \mathbf{J} - \nabla_{\parallel} P_e / en - \mathbf{b} \cdot \nabla \cdot \Pi_e$$

$$\partial P / \partial t + \mathbf{v} \cdot \nabla P = -\gamma P \nabla \cdot \mathbf{v} + \dots$$

$$\partial P_e / \partial t + \mathbf{v} \cdot \nabla P_e = -\gamma P_e \nabla \cdot \mathbf{v} + \dots$$

- Pressure tensor

$$\mathbf{P}_h = P_{\perp} \mathbf{I} + (P_{\parallel} - P_{\perp}) \mathbf{b}\mathbf{b}$$

$$f = \sum_i \delta(\mathbf{R} - \mathbf{R}_i) \delta(v_{\parallel} - v_{\parallel,i}) \delta(\mu - \mu_i)$$

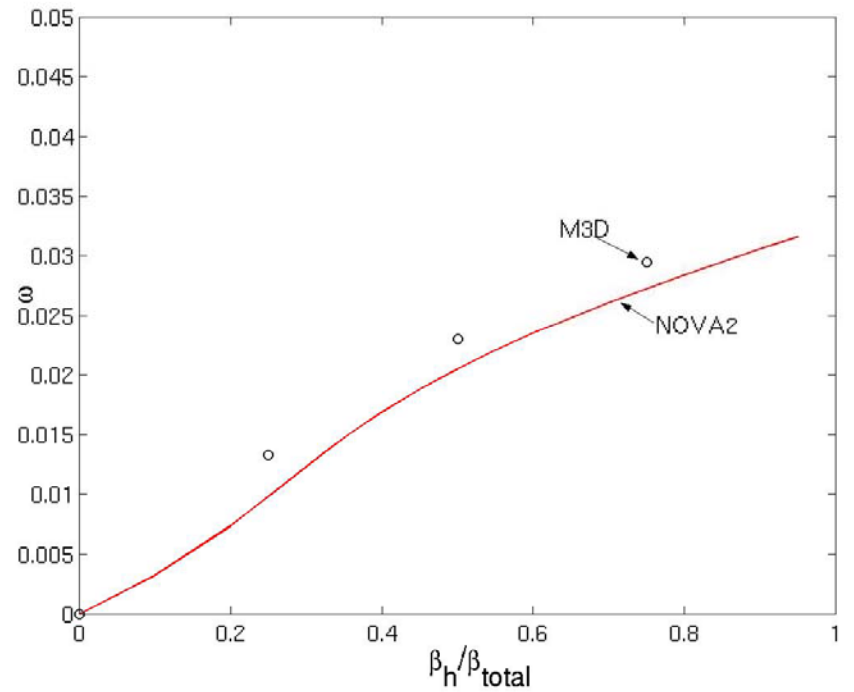
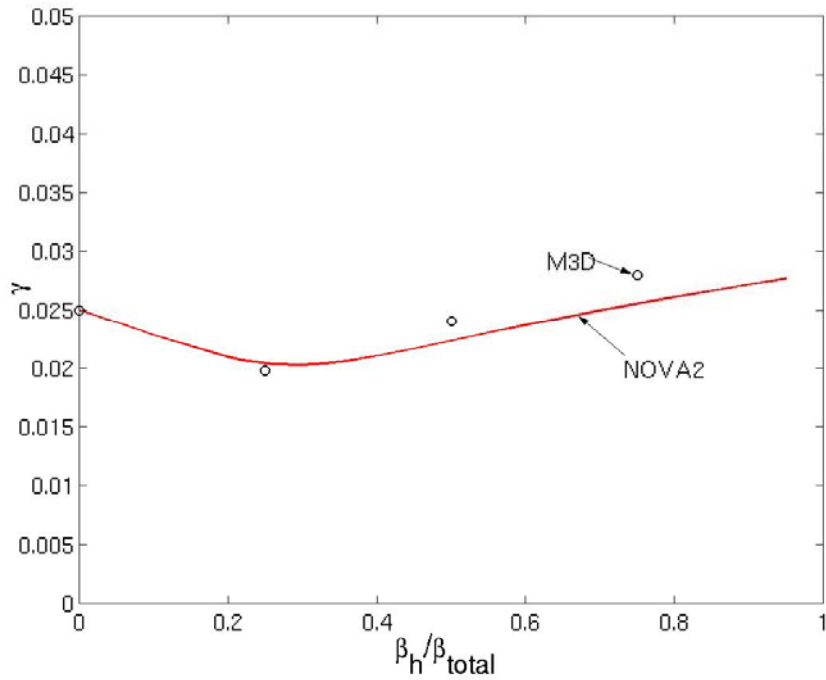
- Gyrokinetic Equations

$$\frac{d\mathbf{R}}{dt} = \frac{1}{B^{**}} \left[ v_{\parallel} (\mathbf{B}^* - \mathbf{b}_0 \times (\langle \mathbf{E} \rangle - \frac{1}{q} \mu \nabla (B_0 + \langle \delta B \rangle))) \right]$$

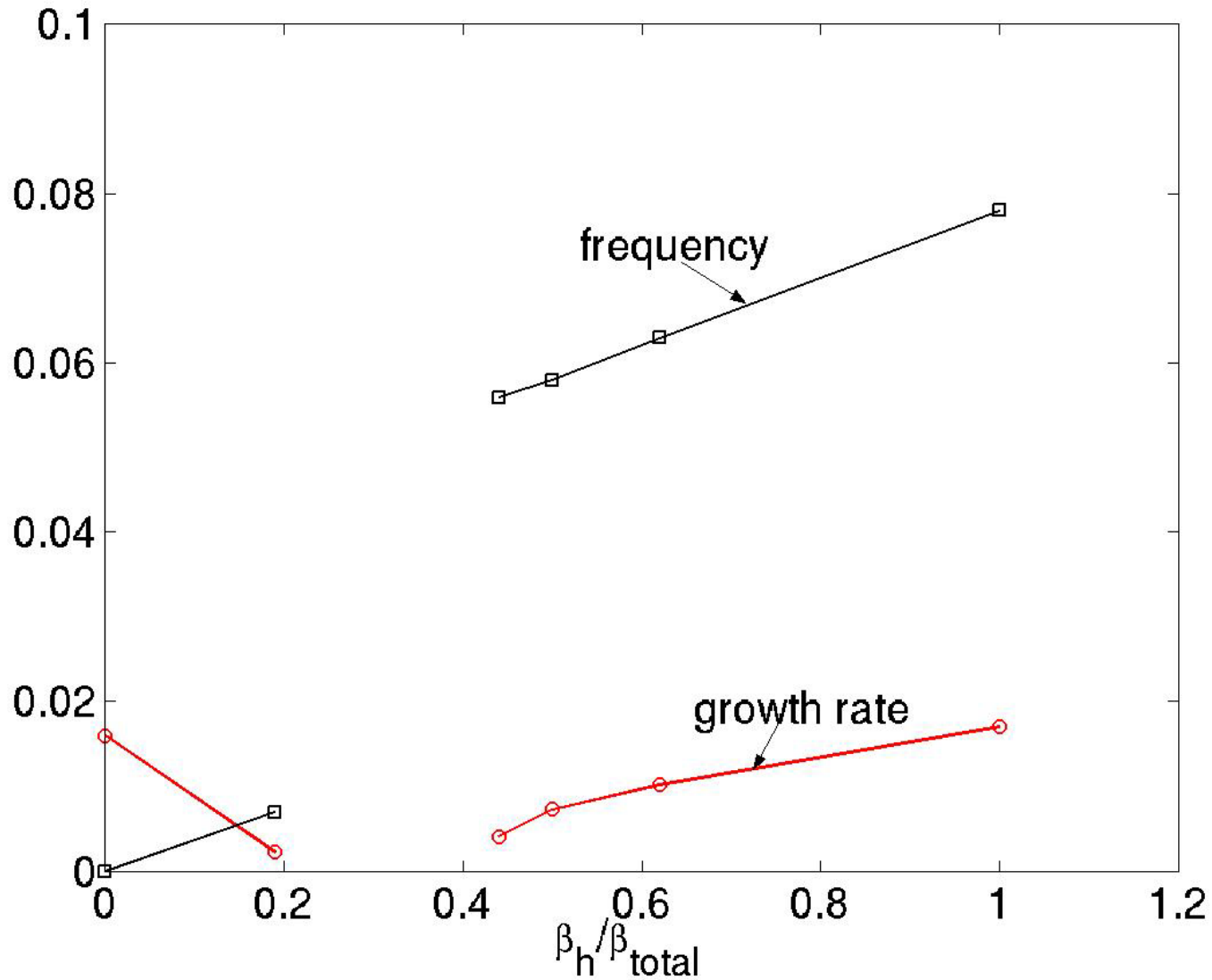
$$m \frac{dv_{\parallel}}{dt} = \frac{q}{B^{**}} \mathbf{B}^* \cdot (\langle \mathbf{E} \rangle - \frac{1}{q} \mu \nabla (B_0 + \langle \delta B \rangle))$$

$$\mathbf{B}^* = \mathbf{B}_0 + \langle \delta \mathbf{B} \rangle + \frac{mv_{\parallel}}{q} \nabla \times \mathbf{b}_0, \quad B^{**} = \mathbf{B}^* \cdot \mathbf{b}_0$$

# M3D agrees with NOVA2 code



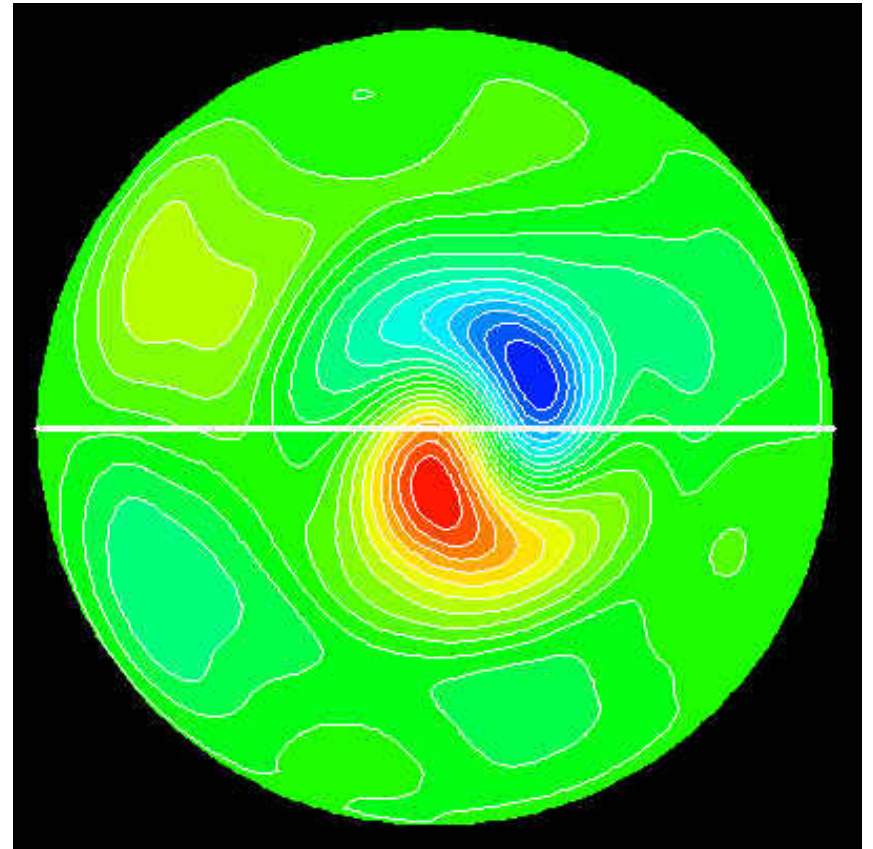
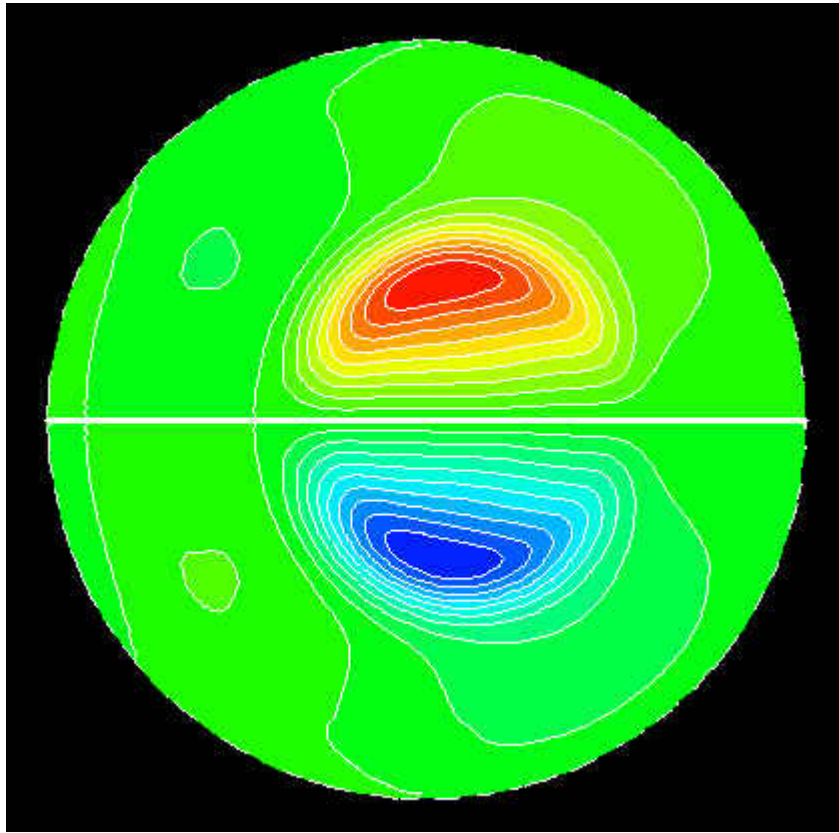
# Excitation of Fishbone at high $\beta_h$



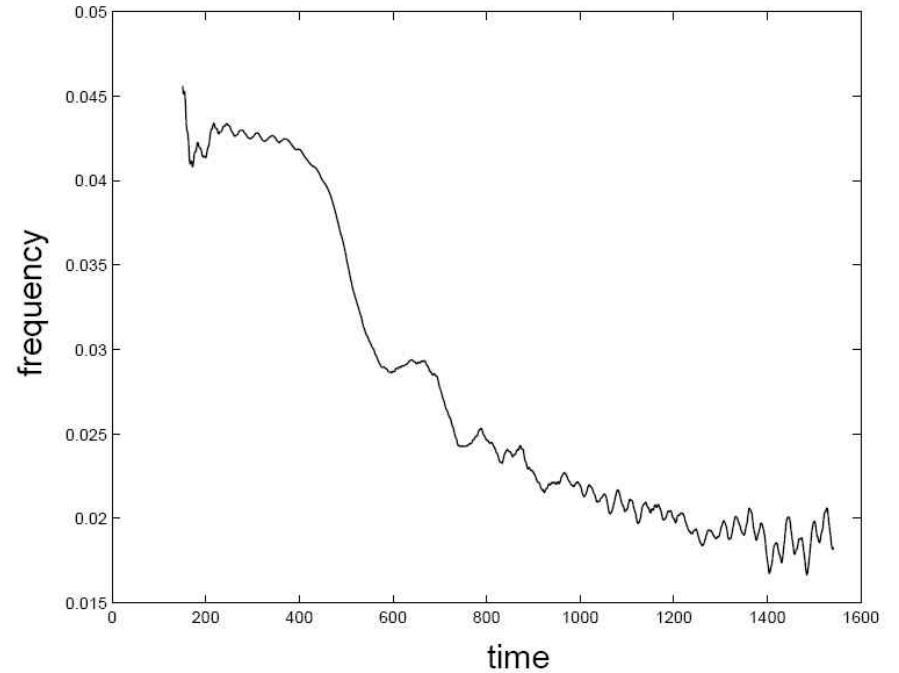
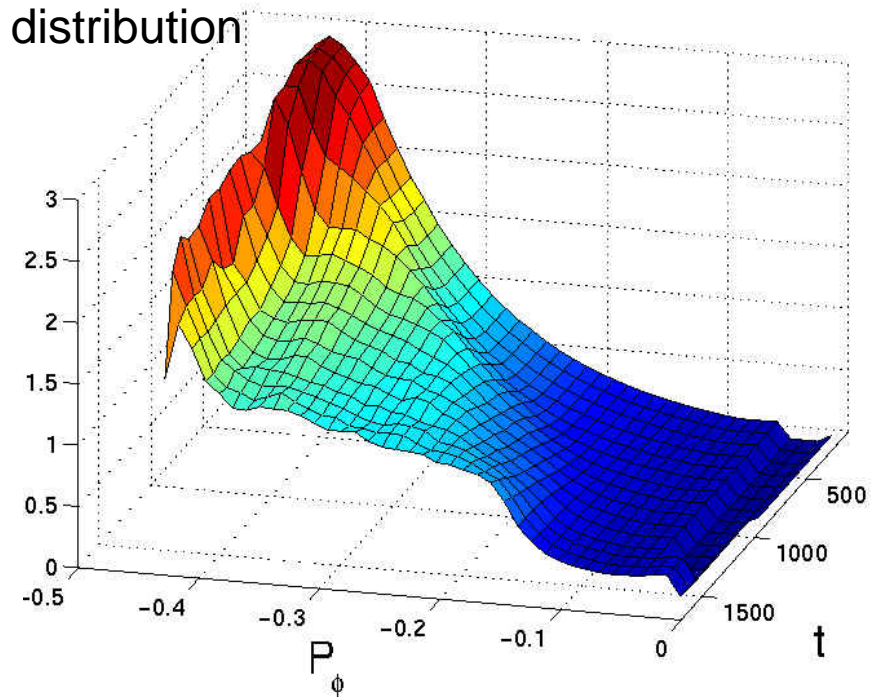
**Circular**  
 **$R/a=2.76$**   
 **$q(0)=0.9,$**   
 **$q(a)=2.5$**   
 **$\beta_-(0) = 5.7\%$**



## Mode Structure: Ideal Kink v.s. Fishbone

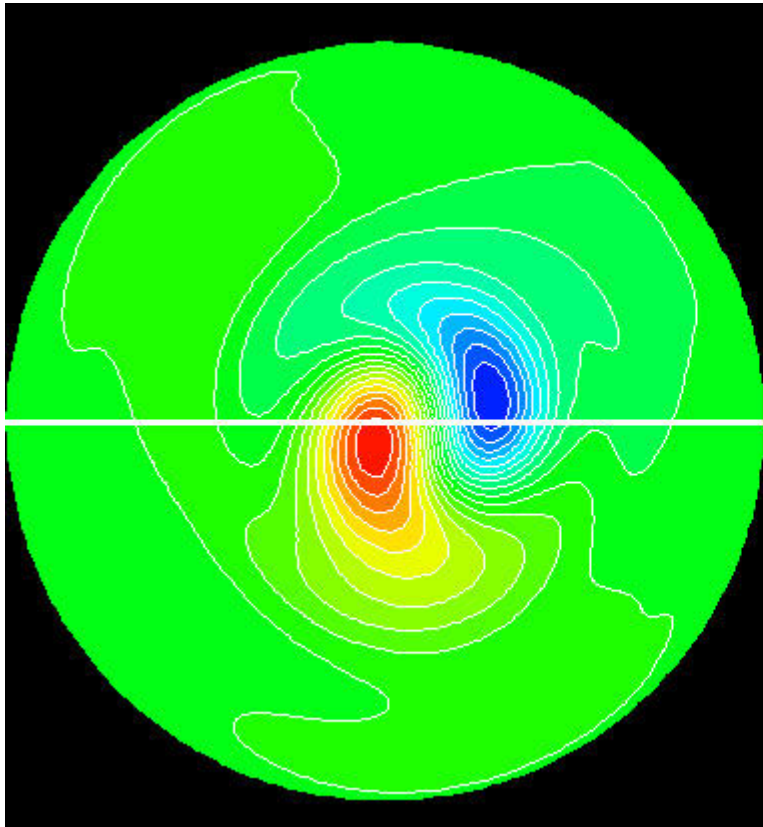


**As flattening region of distribution function increases, the mode frequency chirps down.**

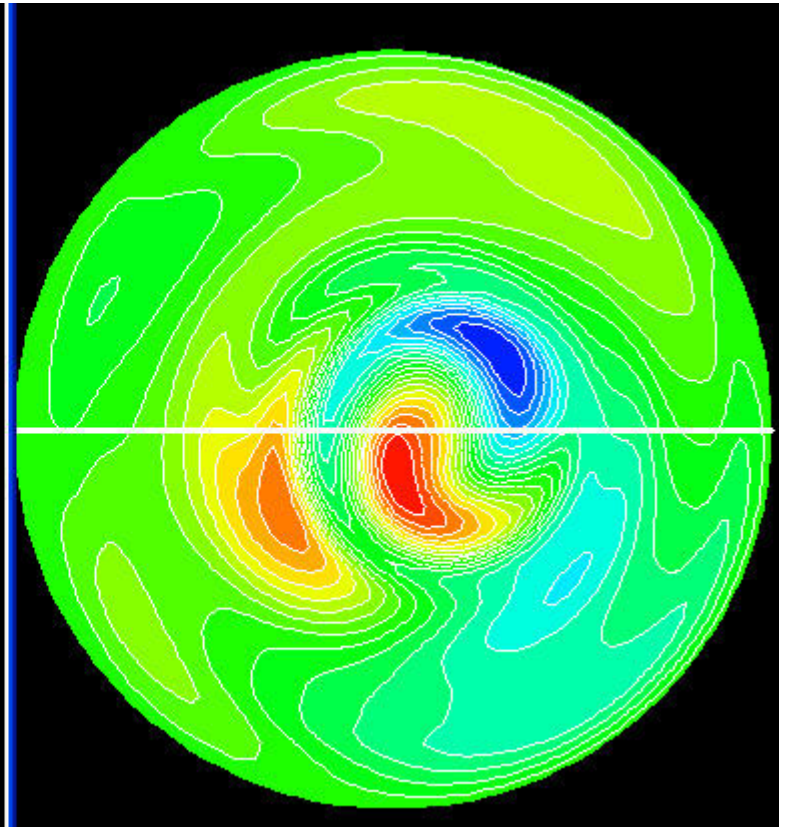


# MHD nonlinearity changes mode structure significantly

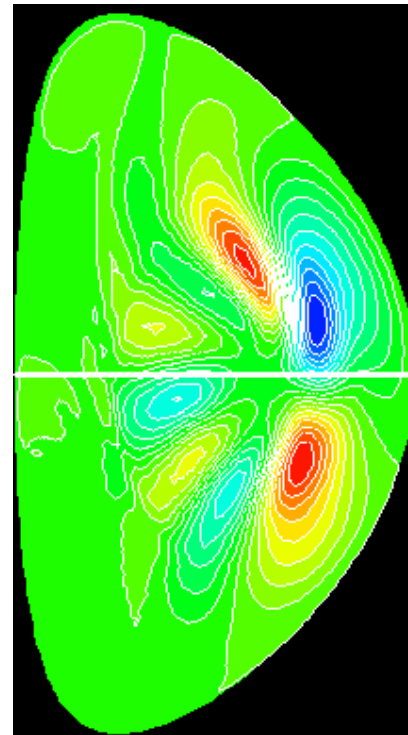
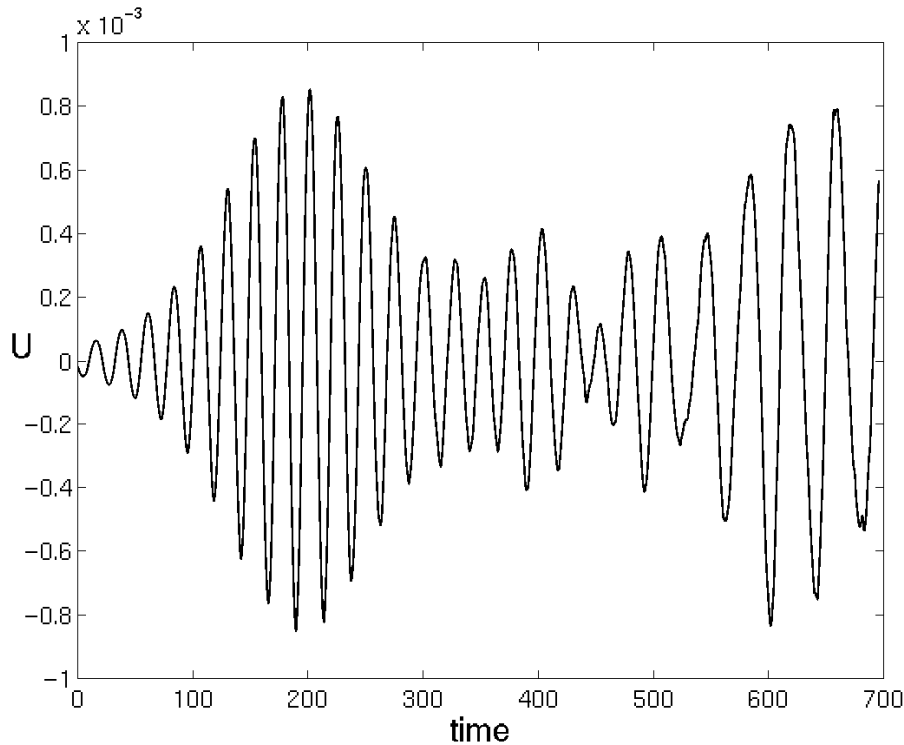
Linear MHD



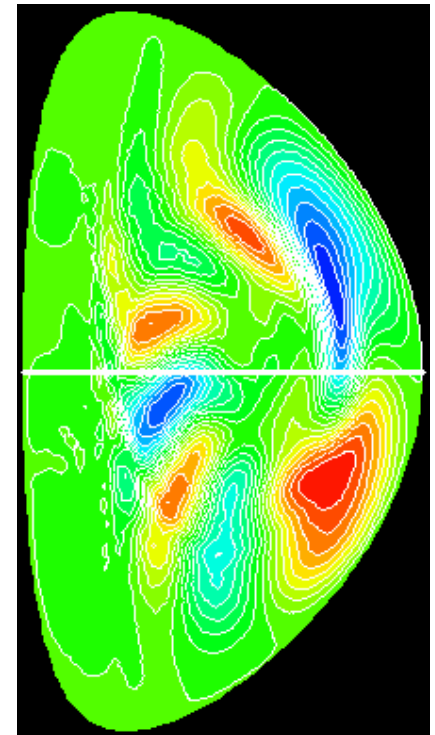
Nonlinear MHD



# M3D Nonlinear hybrid simulations of beam-driven modes in NSTX shows a bursting n=2 TAE as the mode moves out radially.



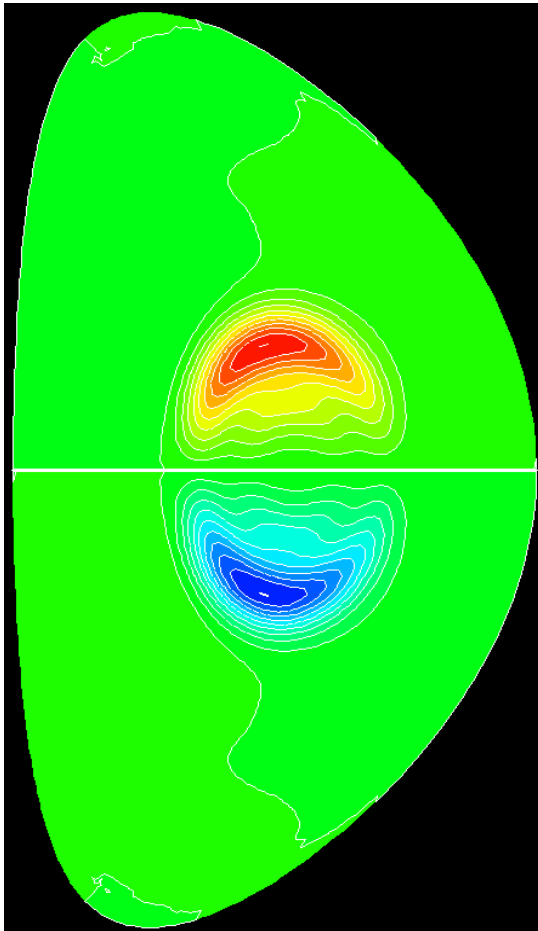
$t=0.0$



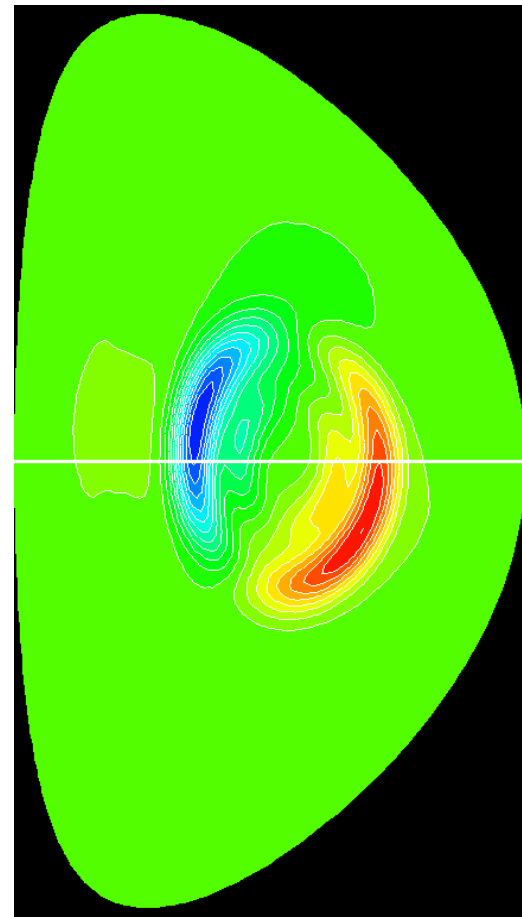
$t=336$

Alpha Particle Stabilization of Internal Kink Mode for ITER:  
**Internal Kink Mode Structure**

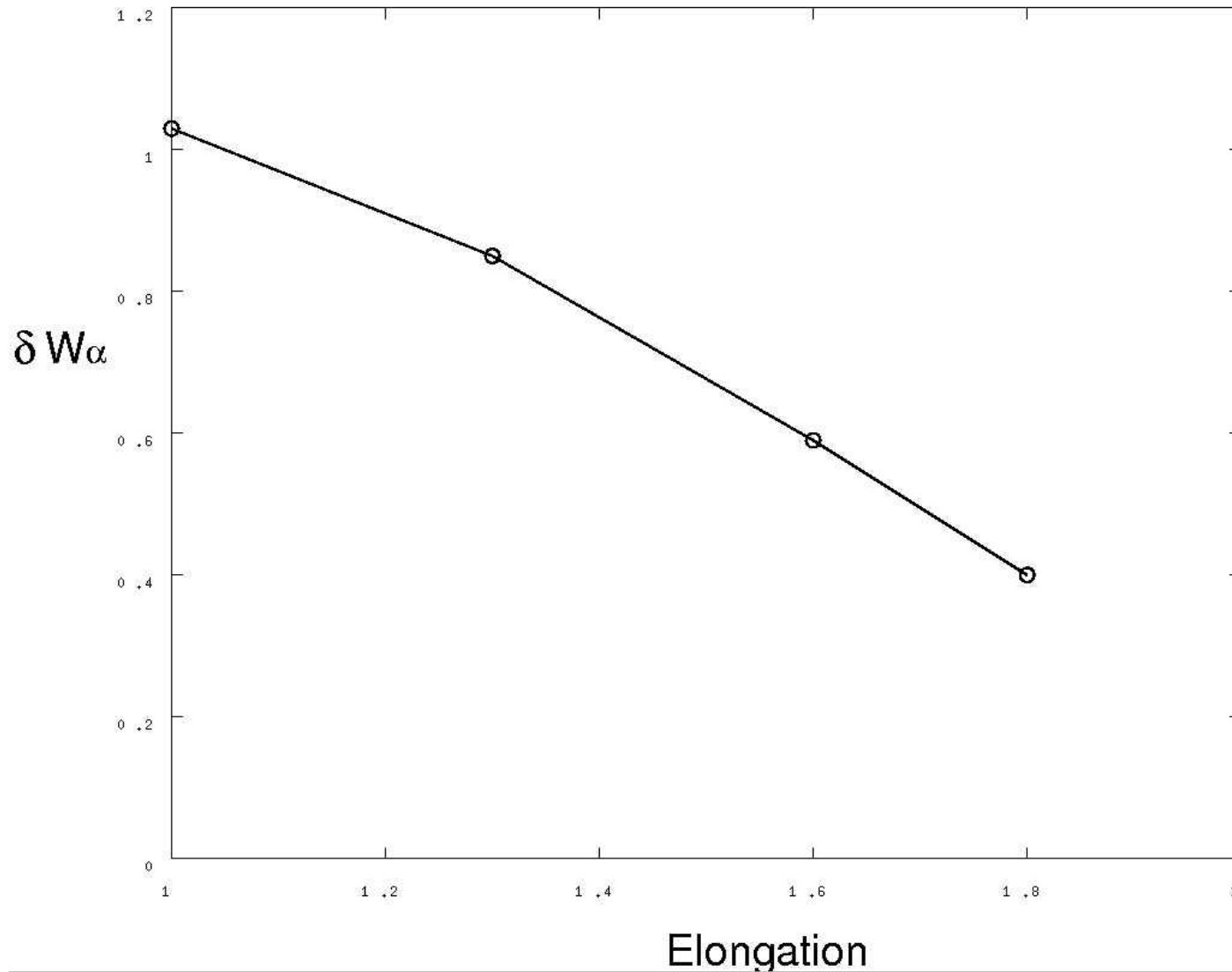
$\beta_\alpha=0.0$



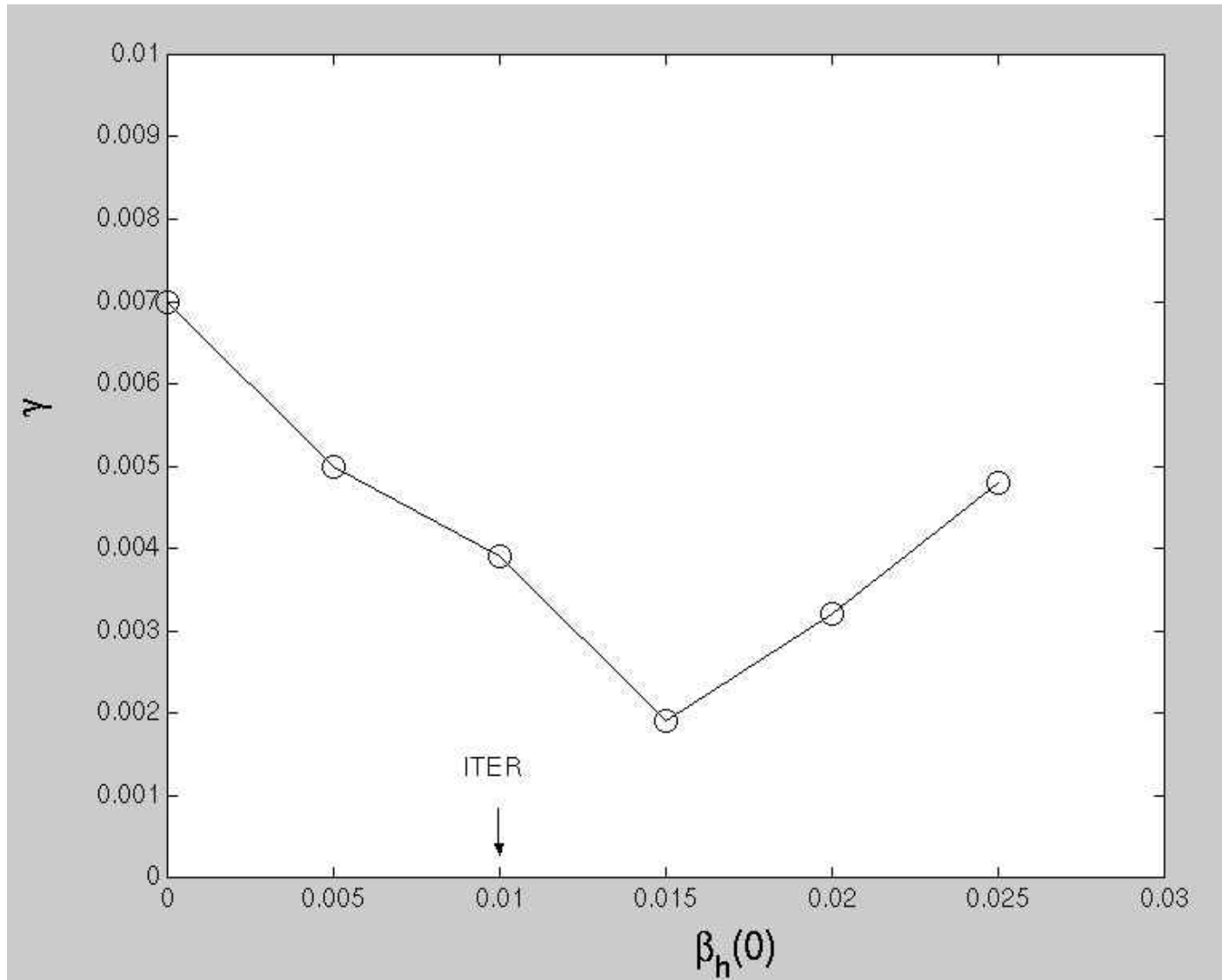
$\beta_\alpha=1.0\%$



# Plasma shaping reduces alpha particle stabilization significantly



# The fishbone mode is calculated to be stable in ITER



# **Thermal ion kinetic effects are stabilizing**

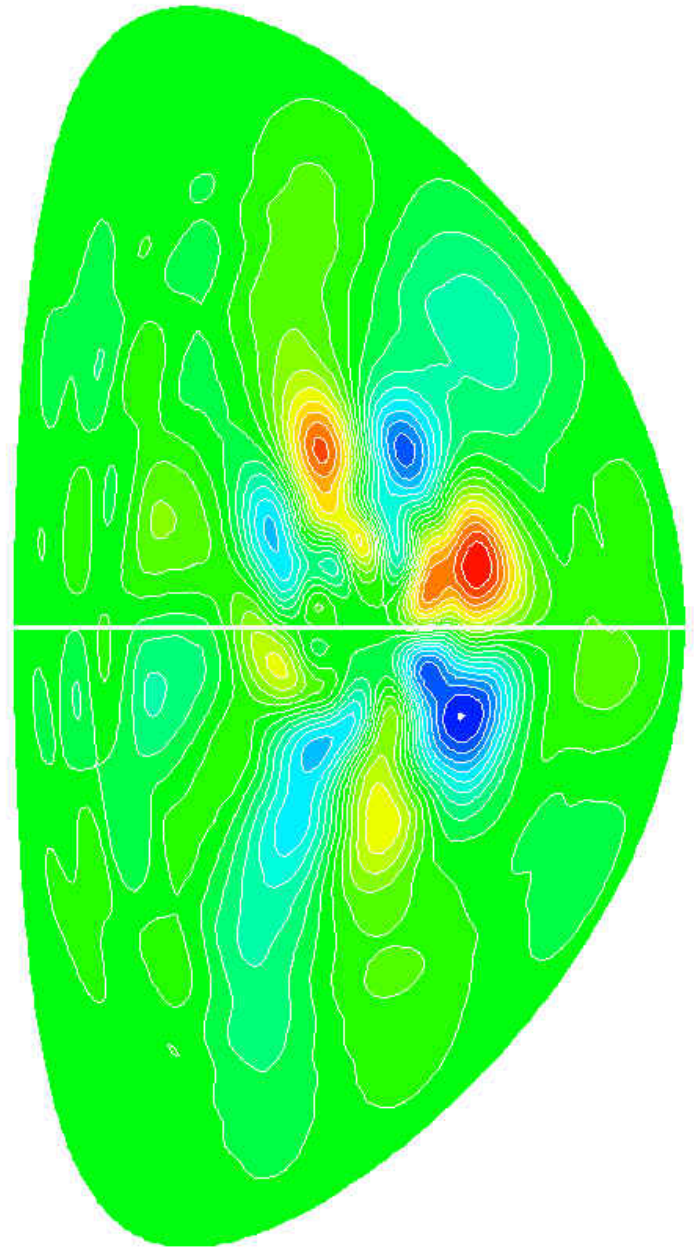
- M3D can also treat thermal ions as particles
- For an ITER case, the internal kink mode growth rate is reduced by half due to thermal ion kinetic effects.



# **n=3 TAE in ITER**

$$q(0)=1.4$$

mode peaks at  $q=1.5$



# Summary

- Comprehensive hybrid simulations have been carried out to investigate kinetic effects of alpha particles and thermal ions on internal kink and TAE.
- Elongation of ITER reduces the alpha particle stabilization of internal kink mode
- Thermal ion kinetic effects are strongly stabilizing for internal kink
- Fishbone is found to be stable in ITER.
- Initial results show an alpha-driven  $n=3$  TAE in ITER.