

VDE Modeling with M3D-C1

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New Resistive Wall Capability In M3D-C1 Includes Wall And Vacuum Regions In Simulation Domain

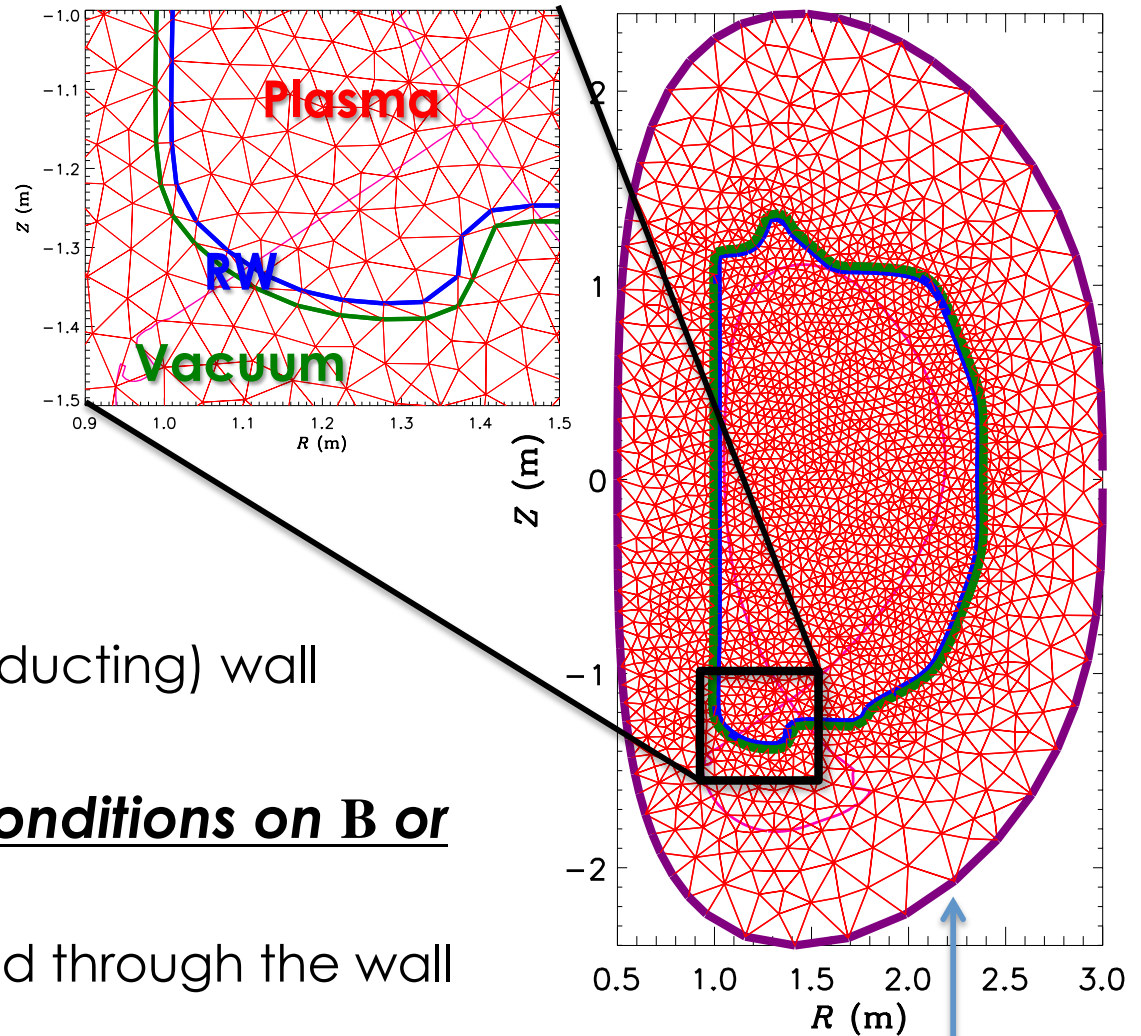
- **3 regions inside domain:**
 - Vacuum ($\mathbf{J} = 0$)
 - RW ($\mathbf{E} = \eta_w \mathbf{J}$)
 - Plasma (Extended MHD)

- **Boundary conditions:**

- v, p, n set at inner wall
- \mathbf{B} set at outer (superconducting) wall

- **There are no boundary conditions on \mathbf{B} or \mathbf{J} at the resistive wall**

- Current can flow into and through the wall



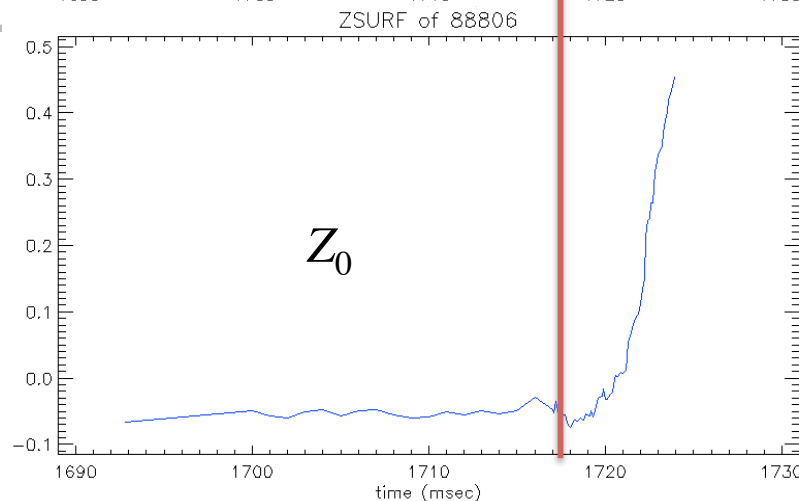
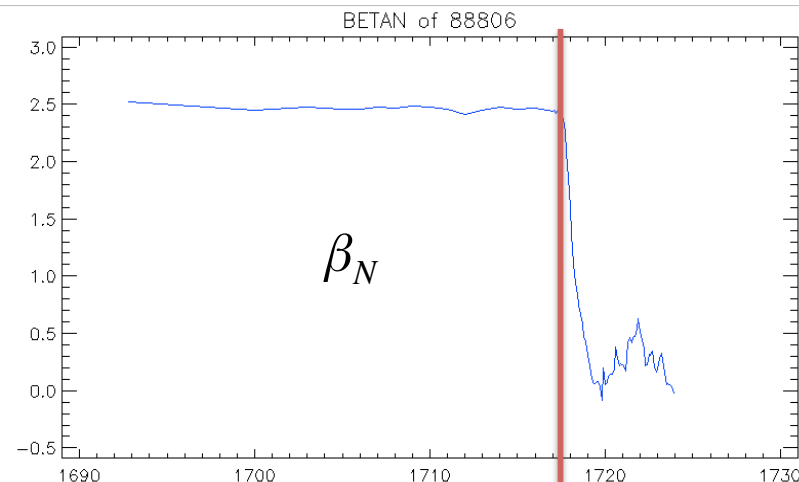
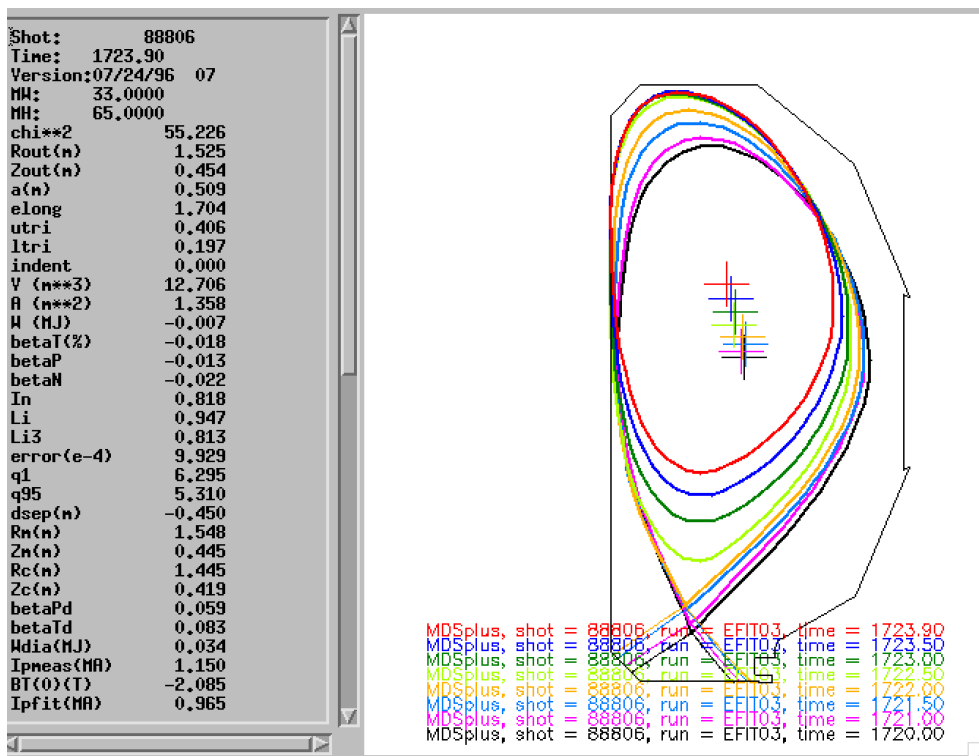
$$\mathbf{B} = \mathbf{B}_{plasma}(t) + \mathbf{B}_{coils}$$

$$\mathbf{J}_{coils} = 0$$

Superconducting Wall

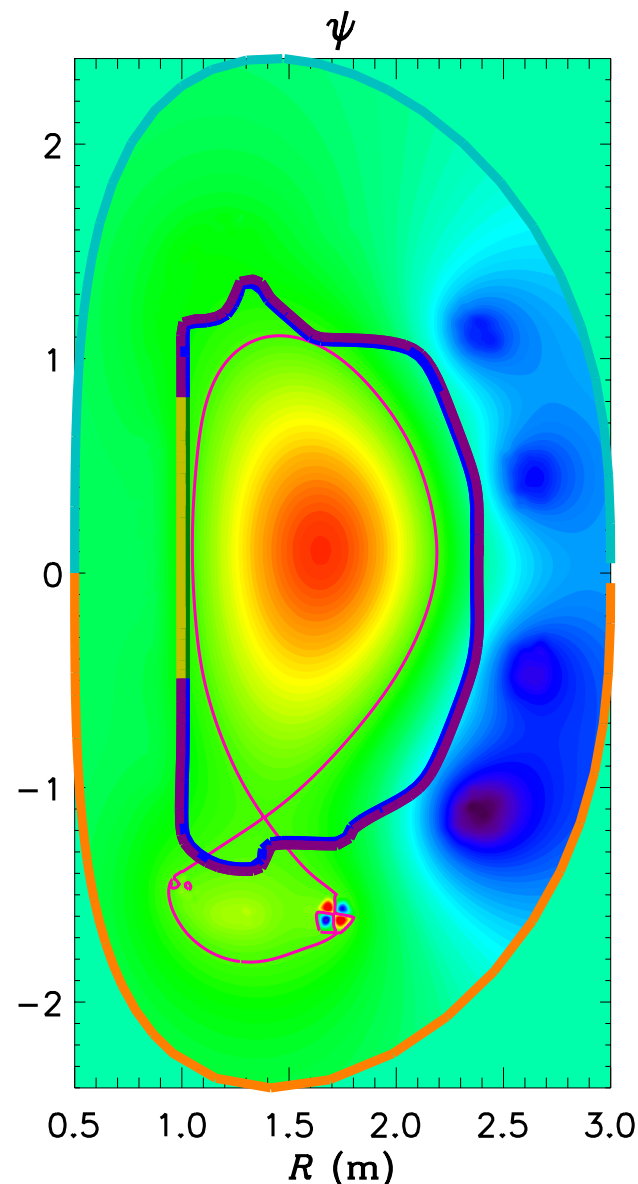
Nonlinear Calculation Recovers $n = 0$ Instability In DIII-D VDE Discharge

- DIII-D discharge 088806 disrupted due to “killer pellet”
 - Vertical stability was lost shortly after thermal quench
 - VDE timescale ~ 3 ms



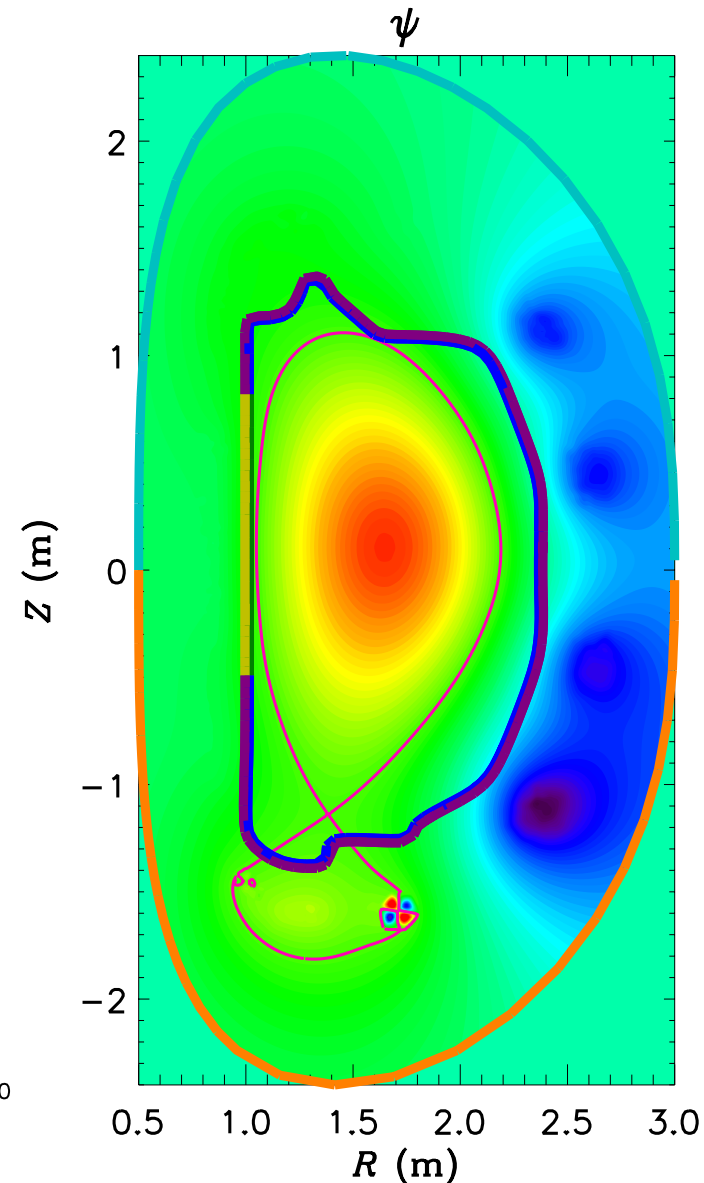
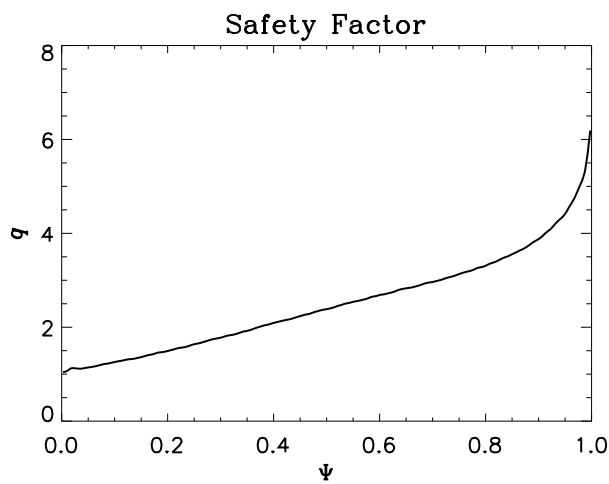
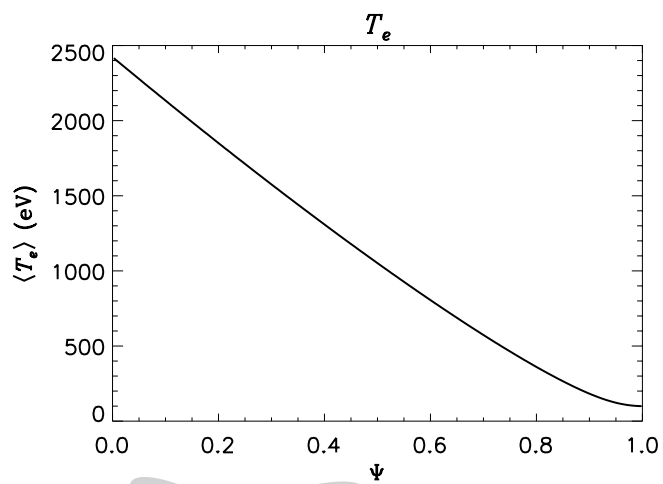
Nonlinear Calculation Initialized From EFIT Reconstruction

- **M3D-C1 is initialized using the reconstructed equilibrium just before TQ ($t = 1720$ ms)**
 - Equilibrium is re-solved on M3D-C1 grid
- **Nonlinear $n = 0$ calculation uses fairly realistic plasma parameters**
 - Spitzer resistivity: $S_0 \approx 6.8 \times 10^7$
 - Anisotropic thermal conductivity: $\chi_{\parallel} / \chi_{\perp} = 10^6$
 - Anomalous perp. transport: $100 < \chi_{\perp} < 800 \text{ m}^2/\text{s}$
- **RW approximates first wall, not vacuum vessel here; using “modern” first wall, different from old experiment**



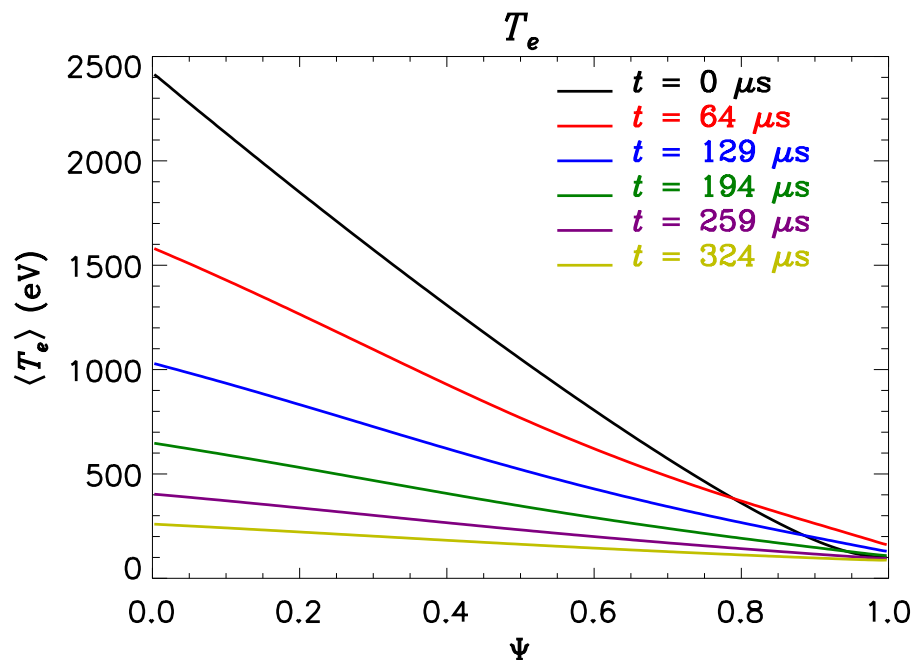
These Calculations Are A “First Try”; Not Suitable For Quantitative Validation

- **Simulations done at low resolution**
 - 5059 elements, ~320k DOFs
- $T_{SOL} \approx 100 \text{ eV} \rightarrow \eta_{SOL} \approx 1.6 \times 10^{-6} \Omega \text{ m}$
- **Single-Fluid, no sources**
- **Wall is uniform thickness (2 cm), resistivity**



Simulations Include Thermal Quench Stage

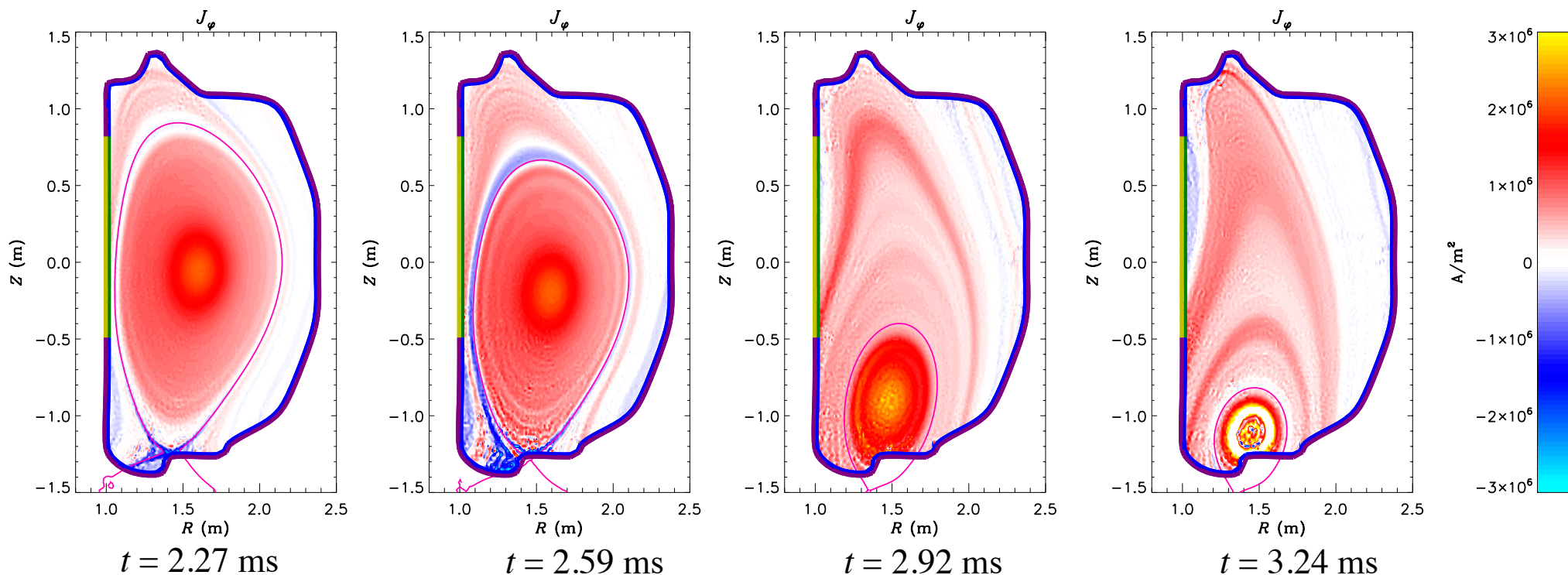
- A thermal collapse happens on $\sim 100 \mu\text{s}$ timescale, due to large perpendicular thermal conductivity
 - Not caused by any MHD activity or convective transport



- At some point during the TQ, the plasma becomes vertically unstable

Calculation Shows Vertical Displacement Into Lower Divertor

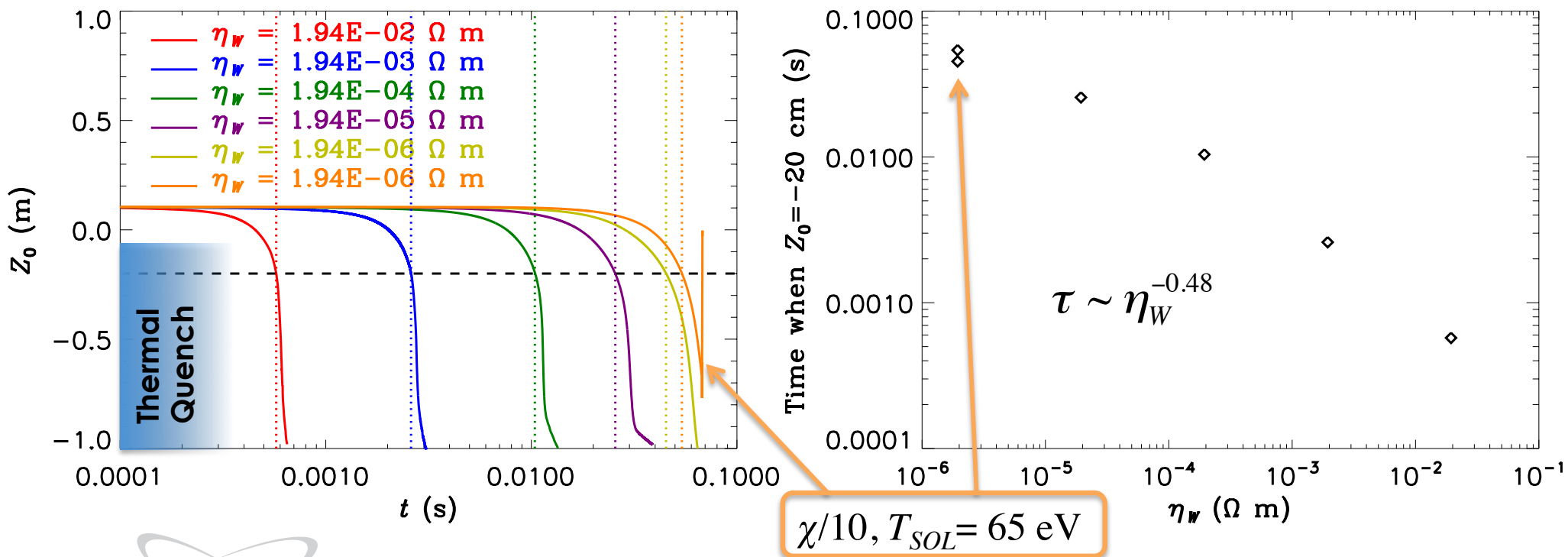
- Both **co- I_p** and **counter- I_p** currents are seen in the open field-line region
- **Plasma always moves to lower divertor, unlike in experiment**
 - Maybe due to different wall configuration?



Timescale of VDE Scales Inversely with $(\eta_w)^{1/2}$

- Given wall thickness $\delta = 2$ cm and a poloidal scale length $d = 50$ cm, resistive wall diffusion times range from ~ 6.5 ms to ~ 0.65 μ s
- VDE timescale is longer than resistive wall time
 - Doesn't seem strongly affected by T_{SOL} ; need more cases

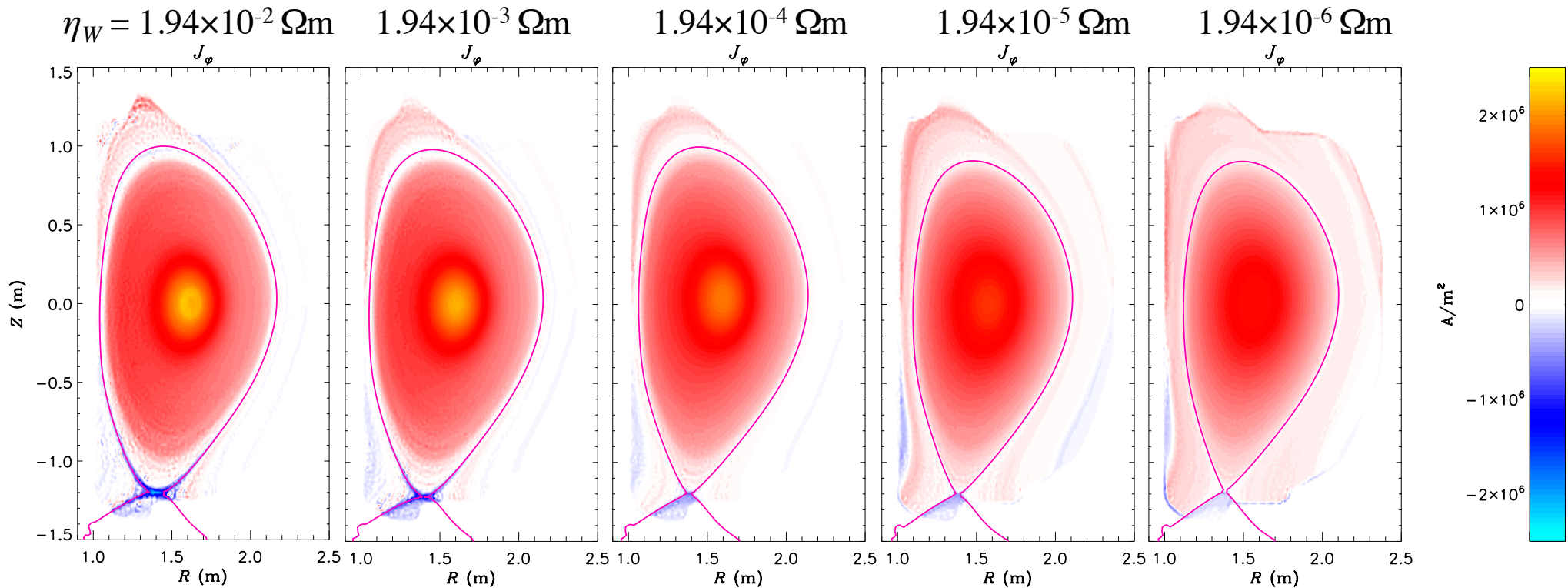
$$\tau_w = \frac{\mu_0 d \delta}{\eta_w}$$



$\chi/10, T_{SOL} = 65$ eV

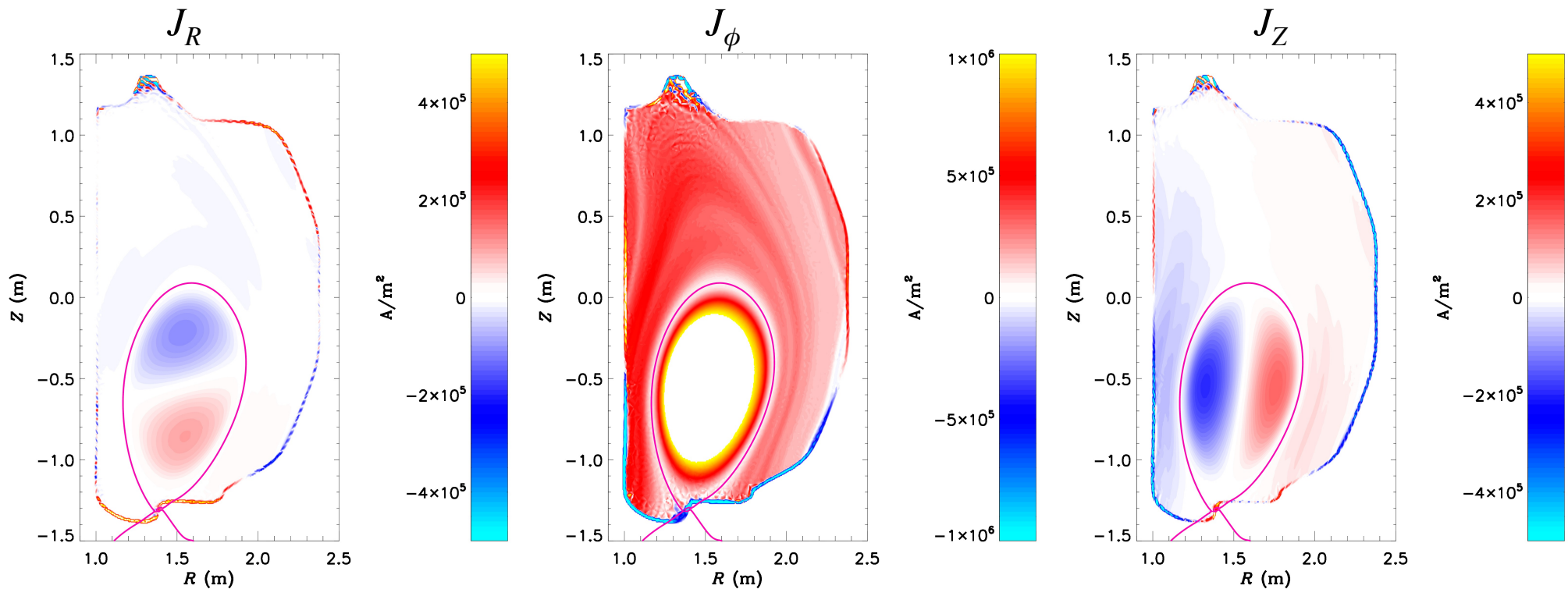
Currents in Wall and Open Field-Line Region Change with η_W

- At early stage of VDE, currents in the wall are stronger at lower η_W
- **Counter- I_p** currents are significantly stronger at higher η_W



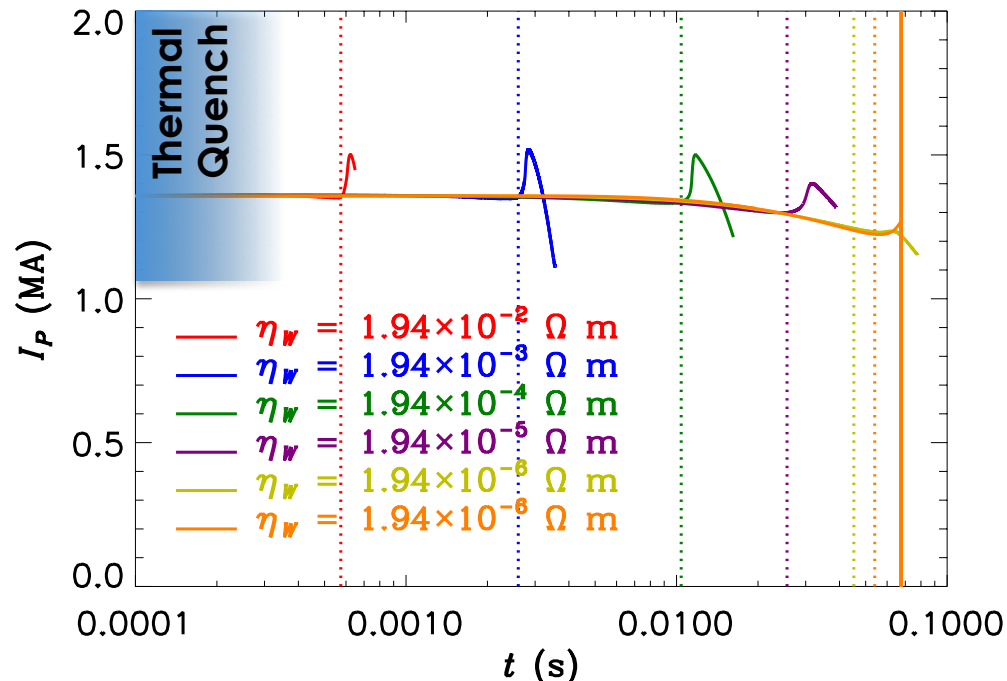
Wall Currents are Mostly Inductive

- **Currents are also present in the open field-line region**
 - Magnitude may be an artifact of high T_e in the open field-line region
 - Current flows from plasma to wall to ensure $\nabla \cdot \mathbf{J} = 0$
- **Wall currents are consistent with excluding poloidal flux**



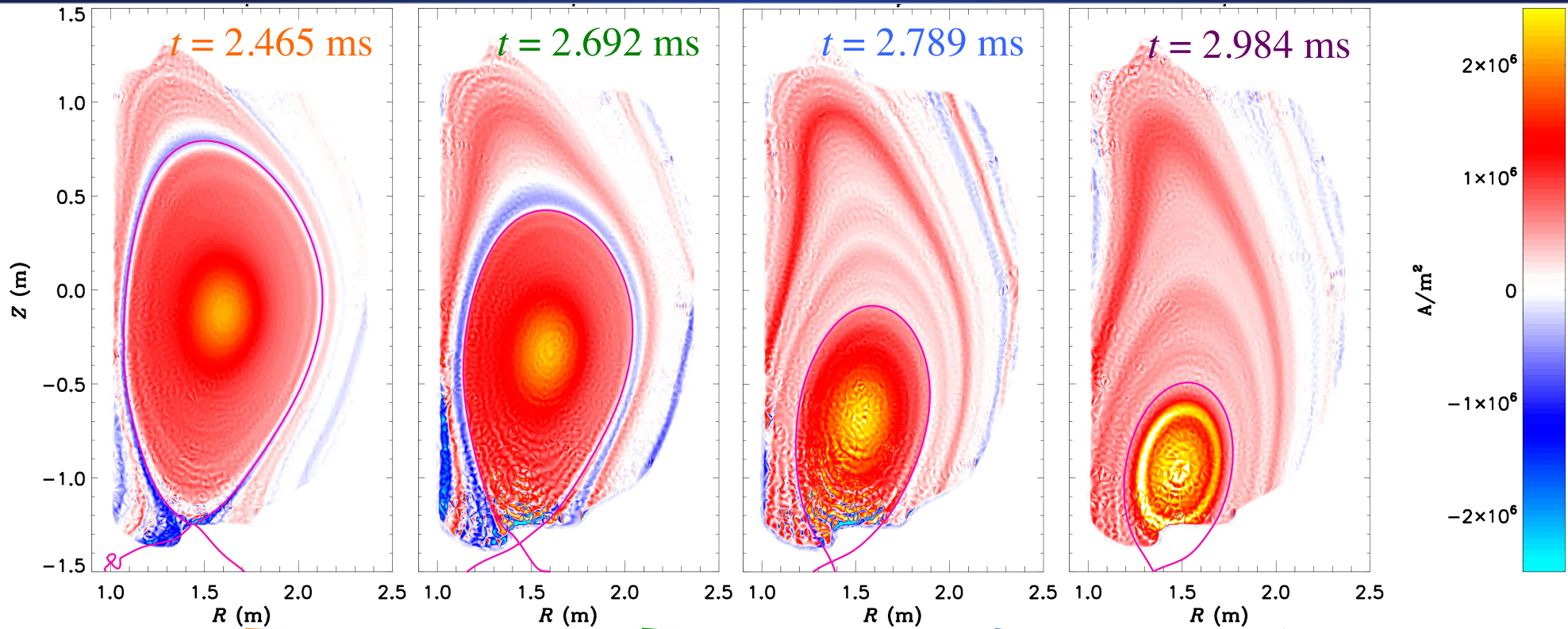
Current Spikes Observed Before Current Quench; Associated with Vertical Motion of Plasma

- Current spike onset is correlated with vertical motion of plasma, unlike TQ



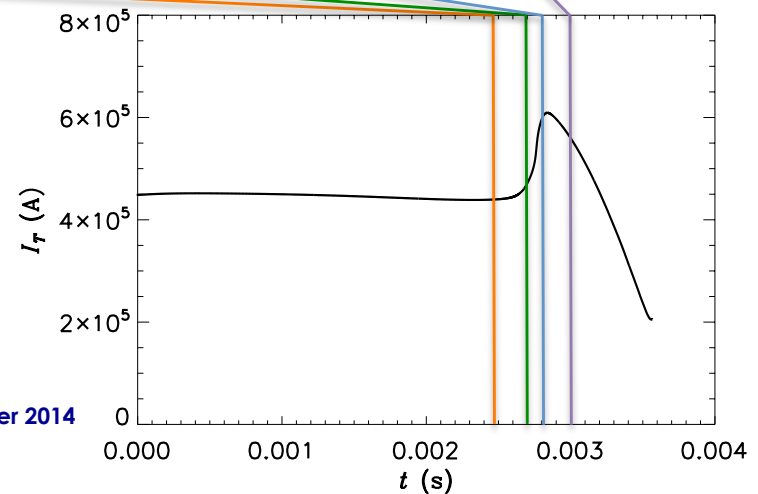
- “ I_P ” here only includes all toroidal current in the plasma region, but not in the resistive wall
- Spike is significantly diminished when $\eta_w < \eta_{SOL}$

Current Spike is Associated With Loss of Counter- I_p Current In Open Field-Line Region



$$\eta_W = 1.94 \times 10^{-3} \Omega \text{ m}$$

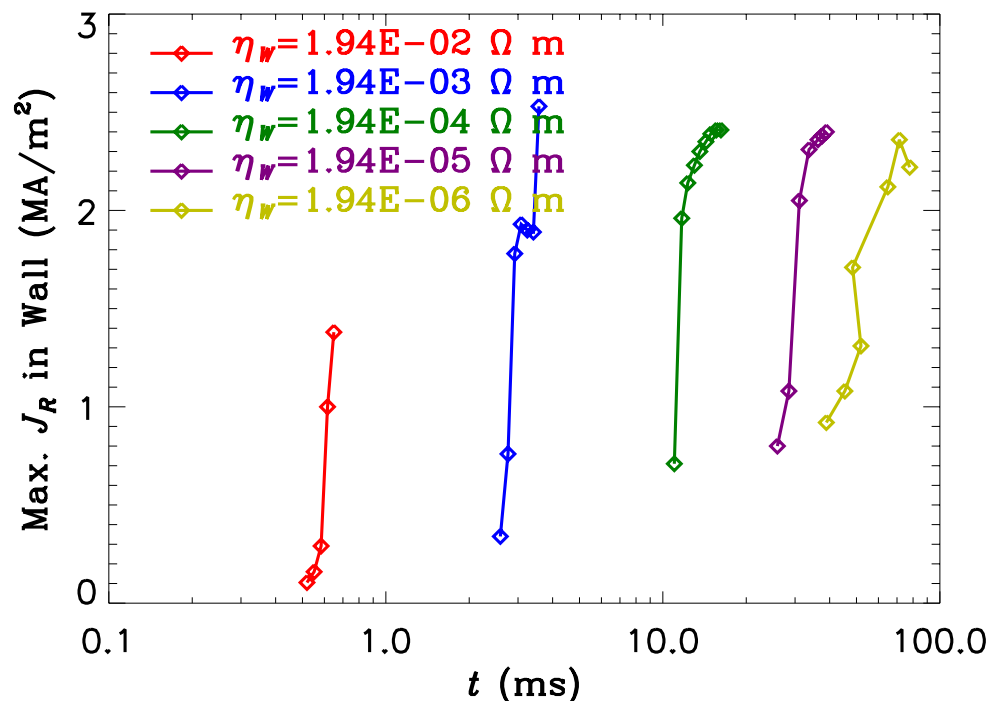
- Plasma undergoes rapid contraction during current spike



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Max Poloidal Current in Wall Depends Weakly on η_W

- Maximum J_R occurs during current quench, when plasma is limited by lower divertor
- Maximum J_R is roughly 2–2.5 MA/m² in this case
 - Corresponds to $F_Z \sim 500$ kN over ~ 50 cm of the lower divertor
- Impulse to vessel depends on η_W because time scale changes



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Summary

- **Resistive wall model in M3D-C1 seems to be working properly in 2D**
 - Axisymmetric nonlinear & complex linear
 - Realistic transport parameters and timescales
- **VDE calculations show how response currents flow in plasma and vessel**
 - Timescale of VDE scales roughly as $(\eta_W)^{1/2}$
 - Maximum current & force in vessel is weakly dependent on $\eta_W \rightarrow$ impulse decreases with η_W
 - A spike in the total current in the plasma region before the CQ is associated with the plasma contacting the wall; gets smaller when $\eta_W < \eta_{SOL}$
- **Next step: 3D**
 - Axisymmetric nonlinear, with periodic non-axisymmetric linear checks
 - Start 3D nonlinear calculation when non-axisymmetric instability found