

Why Should I Believe My Code?

The Quest for Verification & Validation

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Outline

- I. **Introduction**
- II. **DEGAS 2 Verification**
 - A. **Code Verification**
 - B. **Solution Verification**
- III. **DEGAS 2 Validation**
- IV. **Dedicated Validation Experiments**

Introduction

- **Scientists are supposed to be skeptical!**
 - Treat the code as if it were a perpetual motion machine.
 - [Hatton 97]: “...*the results of scientific calculations carried out by many software packages should be treated with the same measure of disbelief researchers have traditionally attached to results of unconfirmed physical experiments.*”
 - Verification & validation methodologies facilitate this process.
 - These are ongoing efforts ⇒ a quest!
- **Where are we going to get enough manpower & funding to do this?**
 - Effort expended should be commensurate with risk associated with wrong solutions.
 - For most present fusion applications risks are not high,
 - **Possible exception: ITER PFC decisions [Skinner, Edge & Pedestal II].**
 - ⇒ Might be able to get “good enough” with available resources.
 - But, should always keep in mind how we could do better.
 - Describe V&V of DEGAS 2 as an example,
 - Provide throughout ideas for further discussion.

DEGAS 2 Uses Monte Carlo Algorithm to Solve Boltzmann Equation for Neutral Species [Stotler 94]

- **More precisely, compute phase space integrals of form:**

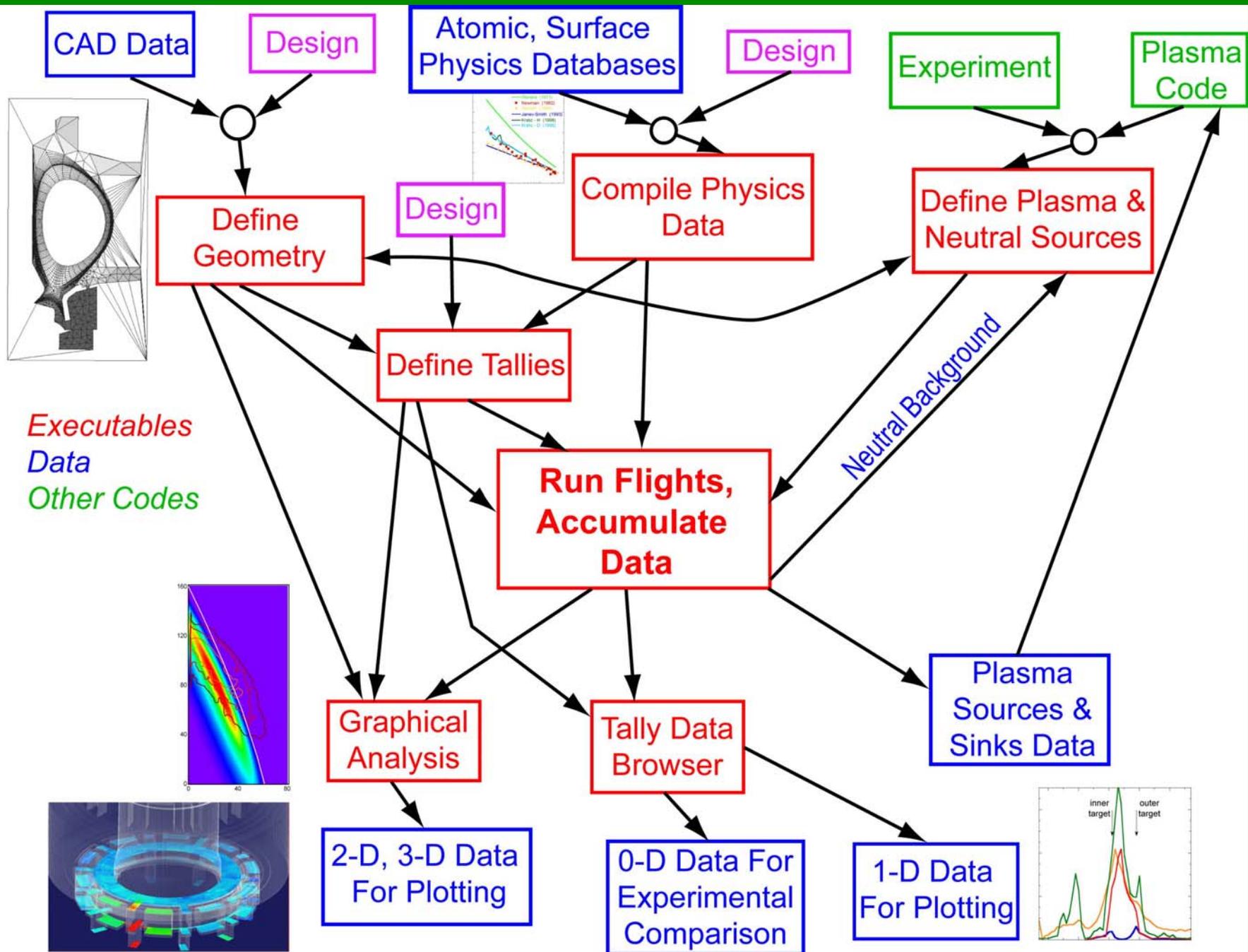
$$I(g) = \int_{\Delta\vec{x}} d^3x \int_{\Delta\vec{v}} d^3v f(\vec{x}, \vec{v}) g(\vec{x}, \vec{v})$$

- **Two good features:**

- Treat complex geometry & processes,
- Most aspects of code operation can be understood in analog terms,
 - But, have mathematical basis in central limit theorem, etc.
 - Needed also for non-analog techniques (variance reduction)

- **Drawbacks:**

- Accuracy of solution scales like $N^{0.5}$,
 - Mitigated by natural parallelism.
- Comparisons of solutions must be done statistically,
 - I.e., using a mean and a variance.



Approach to V&V Dictated by Nature of Code Easier for MC?

- **Modularity simplifies testing of components.**
- **MC code will always converge,**
 - Only question is how fast.
- **MC method naturally provides statistical error,**
 - But, this is only 1 part of total simulation uncertainty!
- **Flexibility facilitates simulating variety of verification problems & experimental situations,**
 - In as much detail as needed.
 - Simulating diagnostic signals straightforward.

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Code Verification Is About Preventing & Eliminating Bugs – DEGAS 2's Exterminator

- Use CVS to track code versions & branches.
- Document all non-trivial code.
- `implicit none` – use it, love it.
- Use “assertions” liberally.
- Let the computer do the grungy coding.
- Use a variety of platforms & compilers.
- Check every code change in a debugger.

What Did You Break This Time?

Regression Testing

- **Regression test suite: set of runs performed after code changes to identify problems caused by those changes,**
 - Require results to match previous ones “exactly”,
 - Or that deviations are the ones expected from code modifications.
- **Ideally, would test all aspects of code functionality.**
- **DEGAS 2 has 8 examples,**
 - Most derived from test cases discussed here.
 - Not comprehensive, but do try to add one with each new code capability.
- **matchout code used to compare output files,**
 - Checks every array, printing largest absolute and relative difference,
 - In most cases, this is 0 (to 15 digits).
 - Does statistical comparison, using relative standard deviations in files, for cases in which only statistical agreement is expected.
- **DEGAS 2 examples not ready for automation,**
 - Not quick or easy to run.

Code Verification

Ideas for Going Further

1. Static deep-flow analysis tools,

- Imagine a compiler in a really bad mood.
- Source of Hatton's "12 serious faults / 1000 executable FORTRAN lines" [Hatton 97].
- Commercial: **QA C, QA FORTRAN**. Looks for:
 - Coding defects not found by compiler,
 - Non-portable code,
 - Code likely to be difficult to maintain,
 - & Standards violations.
 - Outputs software metrics.
- Freeware: **ftnchek**.

2. Dynamic testing,

- Includes regression testing.
- Coverage analysis – which lines of code are executed?
 - Appear to be commercial & freeware packages available.
 - Including Lahey-Fujitsu F95!
 - Can design test cases to hit certain sections of code: glass box testing.
- Black-box testing: have someone else run the code!

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Checking Code Components Separately Speeds & Simplifies Testing

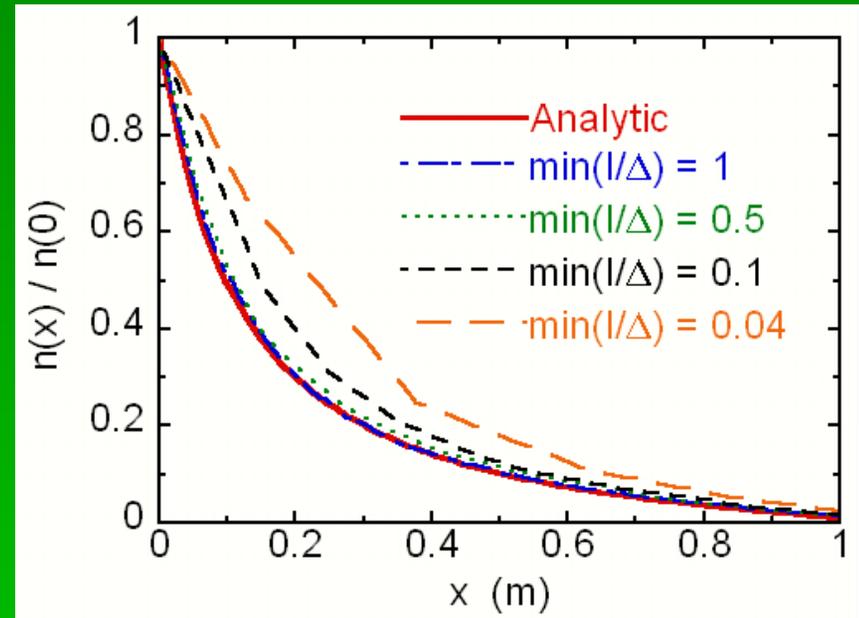
- Test code modifications or new atomic physics / PMI data in isolation,
- Check input data for new problems at each stage of workflow,
- DEGAS 2 has test routines for:
 - System-dependent routines,
 - Random number generator,
 - Atomic physics reactions,
 - Plasma-material interactions,
 - Geometry,
 - Sources.

Integrated Tests of DEGAS 2

- **Against analytic solutions,**
 - Escape probability,
 - **1-D analytic fluid model,**
 - Couette flow.
- **Against other codes, aka “benchmarks”,**
 - DEGAS, **EIRENE**, KN1D
 - Checks numerical methods used in both codes,
 - And, gives some idea of impact of different approaches.
- **Some of these are suitable for inclusion in a public collection of test cases,**
 - Certainly for Monte Carlo neutral transport codes,
 - Some are in fluid limit \Rightarrow test fluid neutral transport codes.
- **Conservation checks are also legitimate verification tests,**
 - Not yet automated in DEGAS 2, but moving towards that.
 - Also symmetry tests.
- **Many simpler checks carried out, but not well documented,**
 - Whenever I see a viable test, I try it!
 - Going forward: compile a record of these.

Analytic Fluid Neutral Model

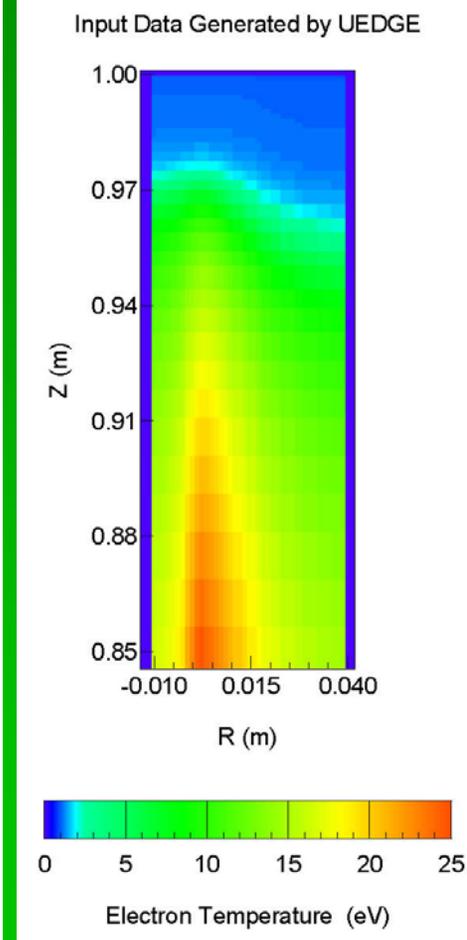
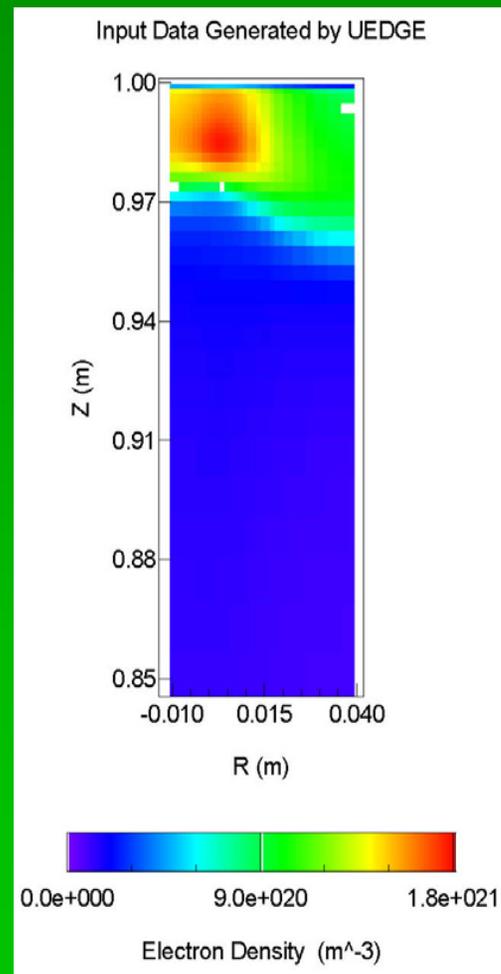
- 1-D fluid neutral momentum balance with constant CX cross section, linearly increasing T_i [Stotler 97] (courtesy S. Krasheninnikov),
- ~40 cases with DEGAS & DEGAS 2,
- Conclude:
 - Max(mfp/system size) < 0.1 for fluid model to be valid,
 - Min(mfp/grid spacing) > 0.5 to resolve thermal force.
- Code runs fine even if these are not true,
 - But, problem being simulated differs physically from the one postulated!



Code-Code Comparisons

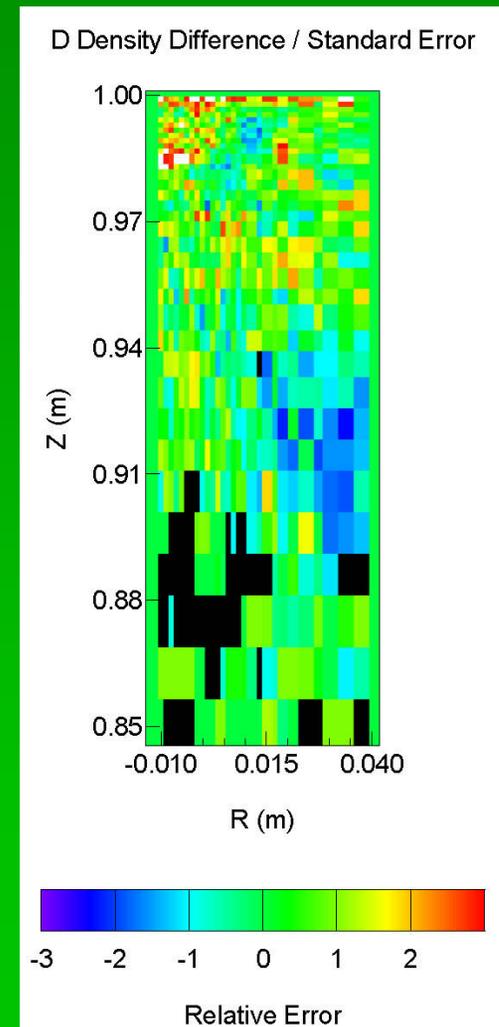
DEGAS 2 – EIRENE

- Details in User's Manual (36 pp.).
- Codes share same basic algorithm & some data,
 - Yet, this was a lengthy exercise.
 - Similar story for DEGAS,
 - Different for KN1D.
- Addressed subtleties in handling of atomic & surface physics, scoring, & interpolation,
 - Required knowledge of internal workings of both.



Code-Code Comparisons DEGAS 2 – EIRENE

- **Compiled histograms of differences normalized to Max(relative standard deviation, systematic error),**
 - Compare histogram with expected fractions to estimate systematic error,
 - Conclude that systematic error is ~5%.
- **Also did performance benchmark,**
 - ⇒ Initial optimization of DEGAS 2.



Solution Verification

Ideas for Going Further

- Establish database of verification test cases,
- Quantify accuracy of results [Oberkampf 02],
 - I.e., error trends in convergence studies,
 - Due to spatial and / or temporal discretization,
 - Iterative error,
 - Roundoff error.
 - Estimates will be useful in validation work!
- Analytic solutions
 - Undoubtedly many already exist & have been used,
 - Identify some for addition to test case database.
- Method of manufactured solutions [Roache 02],
 - Concoct solution that will exercise part or all of algorithm,
 - Analytically compute sources & boundary conditions associated with that solution,
 - Use these to set up run of code.
 - **Solution need not be physical!**
 - Useful solutions can be added to the test case database.
- Run metadata: record of details pertaining to particular run,
 - Code version,
 - Platform & compiler,
 - Location of input & output data files,
 - Else?

Outline

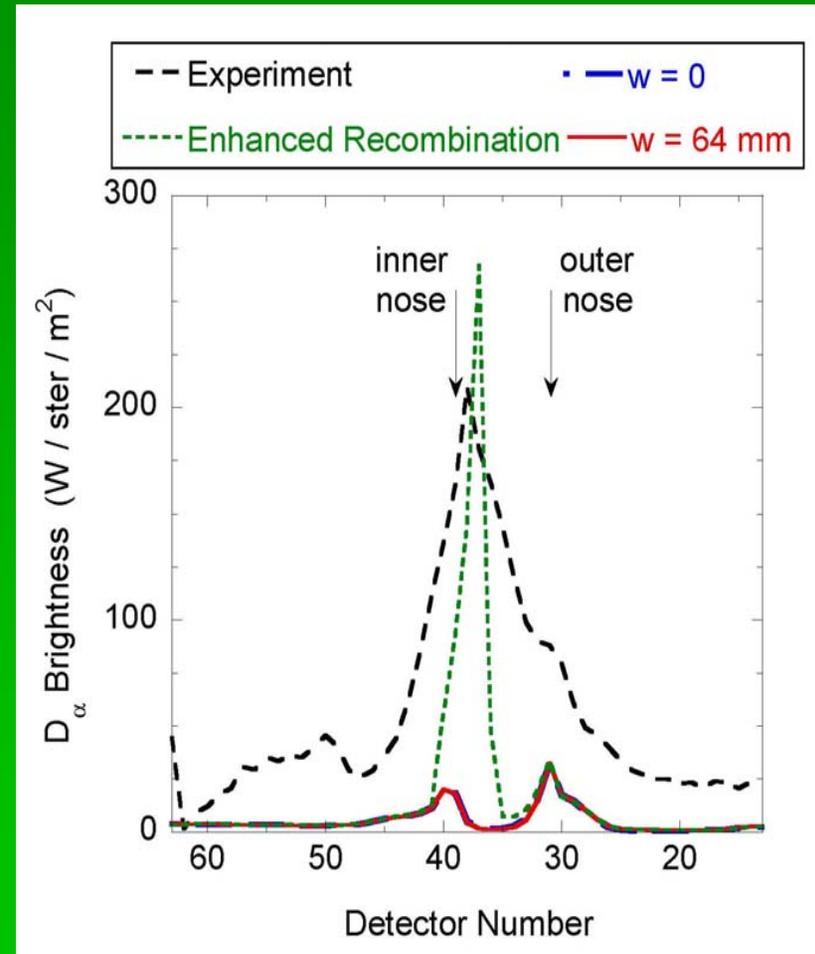
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DEGAS 2 Validation History

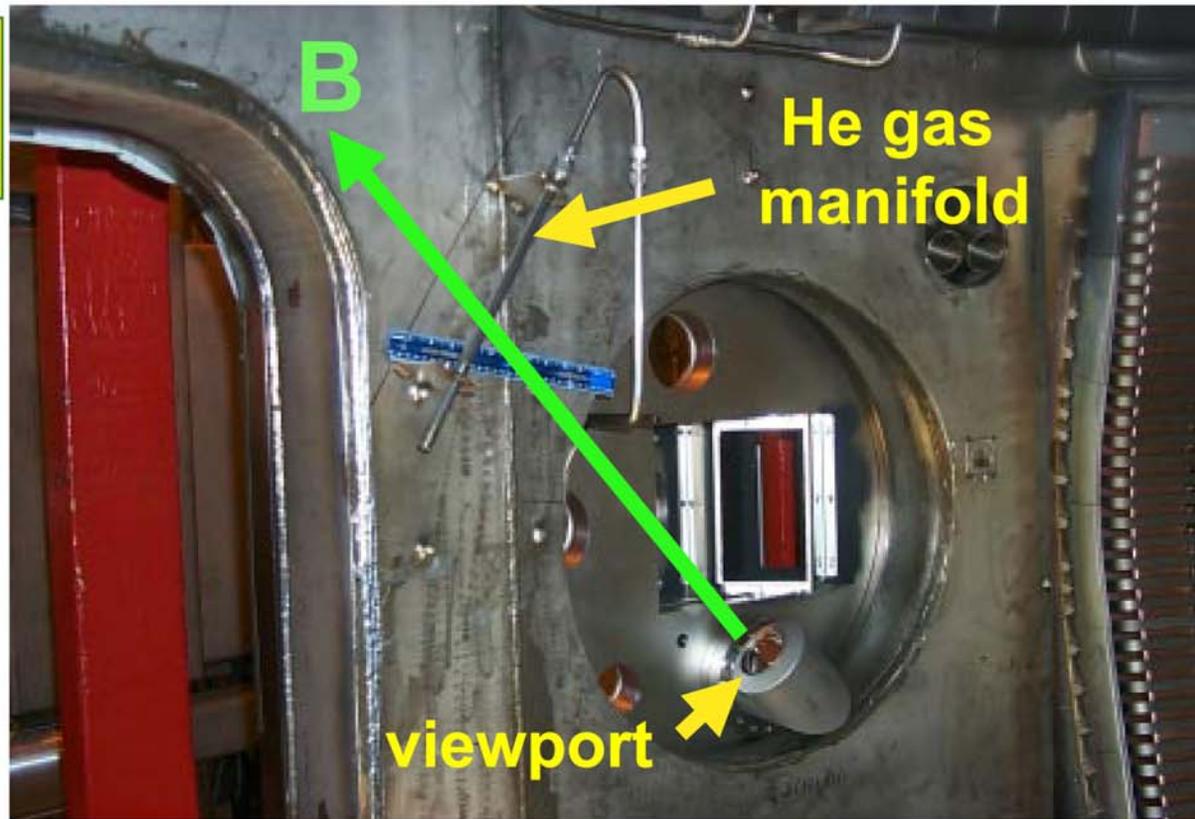
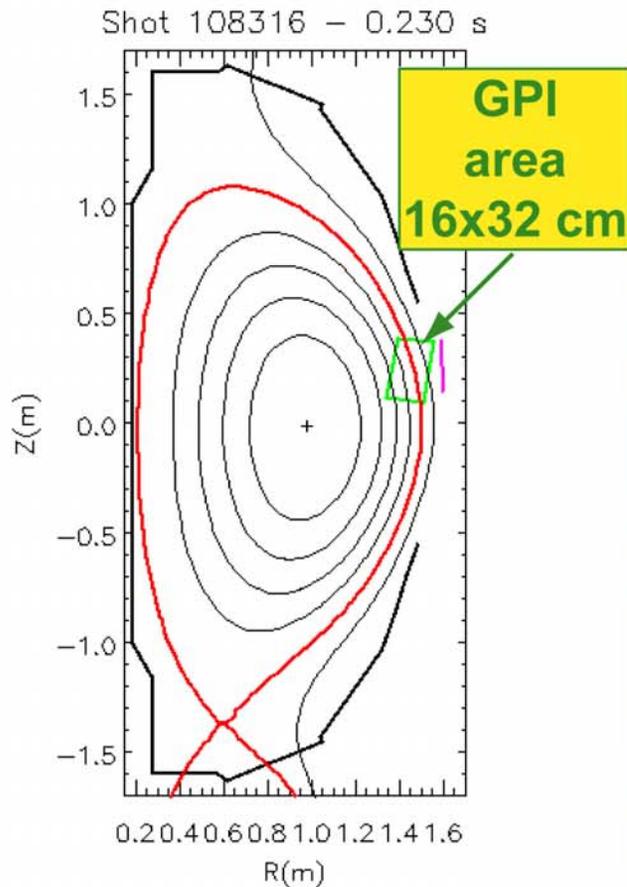
1. TFTR H_{α} Spectrum in D-T [Stotler 96]
 2. Alcator C-Mod Divertor Baffling Experiments
 3. NSTX Gas Puff Imaging Experiments
 4. C-Mod Gas Conductance Measurements
- None is an ideal validation in which code is run “blind”,
 - All code runs done after experiment,
 - Some code input based on experimental data.
 - Error analysis could be more rigorous.
 - But, trend over the 4 cases is towards that ideal,
 - Not a conscious effort!
 - Physics content progressively simpler.
 - All cases involved close interaction with experimentalists,
 - Acquire needed details about machine & experiment,
 - Understand subtleties & limitations of diagnostics.

Alcator C-Mod Divertor Baffling Experiments [Stotler 01]

- Like TFTR case, simulate complex system,
 - Input to code again was experimental plasma data + model to fill in gaps,
 - Used 2-point model \Rightarrow no adjustable parameters,
 - Assumed divertor neutral pressure dominated by recycling on outer target.
- Found neutral pressures too low by ~ 10 ,
 - Divertor D_α also off.
 - Concluded that assumed plasma model was inadequate.
- [Lisgo 05] has found that PFR recombination dominates both,
 - Divertor pressure still off by 2 & error bars do not overlap.
 - Photon trapping & 3-D effects matter,
 - Other phenomena may enter
 - \Rightarrow not done adding physics!
- We did learn something,
 - But, did this increase our confidence in the code?



NSTX Gas Puff Imaging Experiments [Zweben 03, poster PI-18]



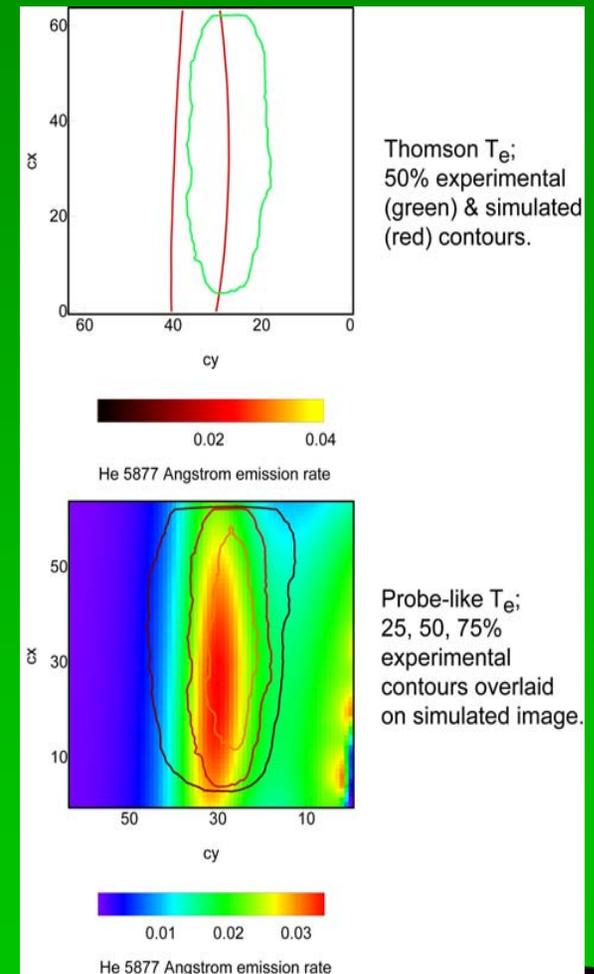
NSTX Gas Puff Imaging Experiments

[Stotler 04]

- **Our standard list of objectives for DEGAS 2 modeling:**
 1. Demonstrate that we understand physics underlying GPI \leftrightarrow validation,
 2. Use 3-D model to clarify spatial relationships of physical objects,
 3. Provide neutral density profiles that can be used to unfold 2-D n_e , T_e from camera images. [Myra, Edge & Pedestal I]
- **Still need data from experiment as input:**
 - Equilibrium,
 - Plasma n_e , T_e radial profiles.
- **But, only “model” needed for plasma parameters is that they are constant on flux surface,**
 - GPI experiment poloidally close to Thomson & probe locations.
- **Simulated physics also simpler:**
 - Only neutral source is gas puff,
 - Plasma recycling negligible,
 - Material interactions not significant.
 - Focused only on neutral transport & resulting light emission due to electron excitation,
 - Use of He as puffed gas reduces required atomic physics.
- **Another example of direct simulation of diagnostic, the 64x64 pixel camera view,**
 - Able to compare directly with experimental images,
 - Yielded 2-D, effective neutral density data used by Lodestar.

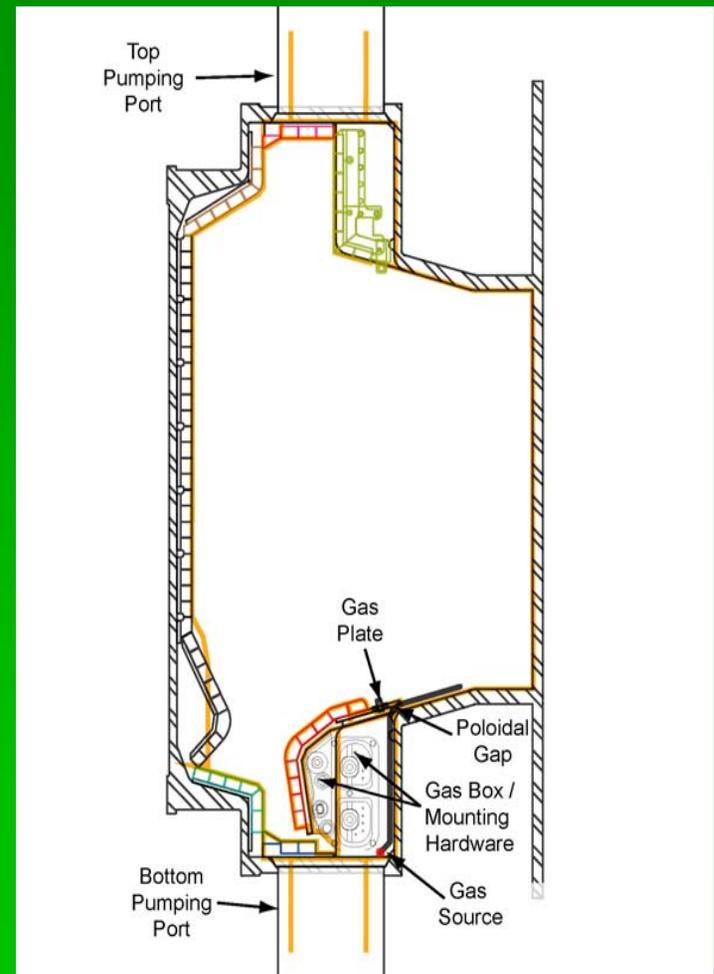
Could This Be A “Slam Dunk”?

- **1st complication: doing steady-state simulation, with constant on flux surface plasma, of time-varying, 3-D plasma,**
 - Only have 1 or 2 TS profiles near GPI time.
 - Assume TS profile \leftrightarrow equilibrium,
 - & Compare with “median” experimental image computed from entire movie.
- **2nd complication: far SOL probe $T_e \gg$ TS T_e ,**
 - Discrepancy not surprising given large blobs there.
- **Within error bars (not shown), simulated & experimental image peak locations agree.**
- **But, to really understand would need to account for impact of 3-D & time variation on TS & probe data as well as on emission cloud!**



C-Mod Gas Conductance Measurements [LaBombard 03]

- Experiments were specifically designed to answer questions raised in modeling of divertor baffling experiments,
 - I.e., to validate the simulation codes!
- Focus here on measurements made without plasma,
 - Two cases: gas puff in open & closed divertor.
- ⇒ isolate physics components
 - Neutral viscosity,
 - 3-D representation of geometry.



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Dedicated Validation Experiments

- “...validation experiments are indeed different from traditional experiments.” [Oberkampf 02],
 - Primary distinction is that the code & code developer are primary customers.
- Not incompatible with present modes of operation,
 - But, making real progress with validation will require shift in priorities.
- Revisit some guidelines in [Oberkampf 04]:
 - Should be designed jointly by experimentalists & simulation scientists,
 - Experiment should measure all quantities needed as input to code,
 - Exploit synergies between code & experiment,
 - E.g., design experiment to offset a code weakness,
 - Use exploratory code runs to identify needed measurements.
 - Keep experimental & code results independent, i.e., blind comparison.
- [Oberkampf 02] goes on to discuss validation metrics,
 - Involving experimental & simulation uncertainties,
 - Postpone consideration for now.

Opportunities for Validation Experiments

- **Comparing simulation results against tokamak discharges represents the top level of the validation hierarchy,**
 - If they don't match, how do you know where the model is going wrong?
 - Developing confidence in model requires going through entire hierarchy,
 - Focus here on lowest level(s).
- **My experience (this talk): even simplest benchmarks or experimental comparisons are worthwhile,**
 - Rarely as simple as they seemed,
 - Always learn something.
 - Even demonstrating that physics is different than in full system constitutes progress.
- **Plasma turbulence codes may be good place to start,**
 - At or close to “first principles” \Rightarrow no adjustable parameters,
 - **Universal character of edge turbulence [Zweben 04] \Rightarrow conceivably could make significant progress w/o tokamak experiments.**
- **Dedicated validation experiments ideal for university environment,**
 - Relatively small scale compatible with typical university funding,
 - Multiple diagnostics \Rightarrow opportunities for student involvement.
 - Requisite connection with code developers & theorists would keep university researchers & primary fusion labs closely coupled.
- **Ideas for possible validation experiments?**
 - Will need expertise of both experimentalists & simulation scientists,
 - **TTF is perfect forum for this!**

Conclusions / Discussion

- **Code verification**
 - Tools for improving software quality,
 - Static deep-flow analysis,
 - Dynamic testing.
- **Solution verification**
 - Database of accurate test cases from analytic results & MMS.
 - Code-code comparisons: may be tough!
 - Quantify accuracy of results.
 - Run metadata?
- **Code Validation**
 - Simulating full tokamak behavior may provide limited insight,
 - More constrained experiments can still be challenging.
- **Dedicated Validation Experiments**
 - Code is the primary customer!
 - Can we design experiments for lowest tier of hierarchy?
- **See also the V&V talks in the parallel sessions**
 - **Core Working Group II Thursday 10:10 – 11:30**
 - **Core Working Group V Friday 3:00 – 4:15**

References

- **[Hatton 97]** L. Hatton, “The T Experiments: Errors in Scientific Software”, *IEEE Comput. Sci. Eng.* **4**, 27 (1997).
- **[LaBombard 03]** B. LaBombard and C. J. Boswell, “In-Situ Gas Conductance and Flow Measurements Through Alcator C-Mod Divertor Structures With and Without Plasma Present”, MIT PSFC Tech. Report PSFC/RR-03-6 (2003).
- **[Lisgo 05]** S. Lisgo et al., *J. Nucl. Mater.* **337-339**, 139 (2005).
- **[Oberkampf 02]** W. L. Oberkampf and T. G. Trucano, “Verification and Validation in Computational Fluid Dynamics”, *Prog. in Aero. Sci.* **38**, 209 (2002).
- **[Oberkampf 04]** W. L. Oberkampf, “Verification and Validation in Computational Simulation”, Transport Task Force Meeting, Salt Lake City, Utah (April 2004).
- **[Post 05]** D. E. Post and L. G. Votta, “Computational Science Demands a New Paradigm”, *Physics Today* **58**, 35 (January 2005).
- **[Roache 98]** P. J. Roache, *Verification and Validation in Computational Science and Engineering* (Hermosa Publishers, Albuquerque, 1998).
- **[Roache 02]** P. J. Roache, “Code Verification by the Method of Manufactured Solutions”, *ASME J. Fluids Eng.* **124**, 4 (2002).

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- **[Stotler 94]** D. P. Stotler and C. F. F. Karney, “Neutral Gas Transport Modeling with DEGAS 2”, *Contrib. Plasma Phys.* **34**, 392 (1994). See also <http://w3.pppl.gov/degas2>
- **[Stotler 96]** D. P. Stotler et al., “Modeling of Neutral Hydrogen Velocities in the Tokamak Fusion Test Reactor”, *Phys. Plasmas* **3**, 4084 (1996).
- **[Stotler 97]** D. P. Stotler et al., “DEGAS 2 Neutral Transport Modeling of High Density, Low Temperature Plasmas”, 16th International Conference on Plasma Physics and Controlled Nuclear Fusion Research (Montreal, Canada, October 1996) (IAEA, Vienna, Austria, 1997), Vol. **2**, p. 633.
- **[Stotler 01]** D. P. Stotler et al., “Modeling of Alcator C-Mod Divertor Baffling Experiments”, *J. Nucl. Mater.* **290-293**, 967 (2001).
- **[Stotler 04]** D. P. Stotler et al., “Three-Dimensional Neutral Transport Simulations of Gas Puff Imaging Experiments”, *Contrib. Plasma Phys.* **44**, 294 (2004).
- **[Stotler 05]** D. P. Stotler and B. LaBombard, “Three-Dimensional Simulation of Gas Conductance Measurement Experiments on Alcator C-Mod”, *J. Nucl. Mater.* **337-339**, 510 (2005).
- **[Zweben 03]** S. J. Zweben et al., “High-Speed Imaging of Edge Turbulence in NSTX”, *Nucl. Fusion* **44**, 134 (2004).

Supplementary Slides

What is DEGAS 2?

- **A Monte Carlo neutral transport code [Stotler 94]**
 - **Fast, efficient**
 - Parallelization built in at the start
 - Most arrays allocated dynamically
 - **Portable**
 - Karney's parallel random number generator
 - Most data exchanges via netCDF files
 - **Easy to add new physics**
 - **Written in FWEB,**
 - Grungy tasks handled by macro preprocessor,
 - TeX documentation interwoven with code.
 - **Statistics:**
 - 31 executables:
 - Main code
 - 13 setup
 - 10 test
 - 7 post-processor
 - ~120 source files
 - Source code (including internal documentation): ~70K lines.
 - 85 atomic & surface physics data files

Does CVS Stand for “Crummy, Vexing Software”?

- **Use CVS (Concurrent Version System) to maintain code versions,**
 - Including binary data & output files!
 - “Tags” keep track of code releases & branches.
 - CVS has no “undo” ⇒ be careful!

I Don't Have Time to Write Documentation!

- **Write documentation as code is being developed,**
 - Especially in source code,
 - Explain less-than-obvious code,
 - You'll be glad you did in ~3 years.
 - Be sure comments & source code agree!
 - Where applicable, refer to equations & expressions in published literature.
- **Compile a User's Manual,**
 - Writing comprehensive manual very time consuming,
 - Many sections of DEGAS 2 User's Manual were written first for posters or talks,
 - It is my reference of choice for these topics!
- **Document reference data files,**
 - E.g., DEGAS 2's atomic and plasma-surface interaction data files.
 - Have one file containing brief description of origin of each data file.
 - Atomic physics data generated by codes I run are also tracked by CVS.

```
if (Day.eq.'Thursday') then
  x = 2.
else
  x = 3.
end if
```

Implicit None: Use It, Love It

- **Primary value is to catch misspelled variable names.**
- **Much easier to have compiler point them out to you than to track down an obscure bug at run time.**
- **Strong typing (e.g., Java) would be even better.**

`assert(cell_intersect < geom_infinity)`

- An “assertion” checks conditions that ought to be true,
 - Print warning,
 - And / or stop code.
- If a line of code makes some assumption about a variable in it, check it! E.g.,
 - Array index \leq dimension,
 - Denominator $\neq 0$,
 - Particle is still in problem space.
- Very useful in catching memory corruption,
 - Memory corruption can make the “impossible” come true.
- In DEGAS 2, used in:
 - All setup, testing, and codes,
 - Some post-processing codes,
 - Initial runs of main program.
 - Disabled for production runs.

Let Computer Do Grungy Coding

- **DEGAS 2 uses FWEB based macros to:**
 - Handle dynamic memory allocation,
 - Specify common blocks, including with MPI,
 - Read & write netCDF files.
- E.g., the string `gi_ncread(fileid)` expands to ~280 lines of code I don't have to maintain.
- Represents “heroic” application of FWEB by Karney,
 - Not clear how to best do this in general.

Suns are From Venus, Linux Machines are From Mars

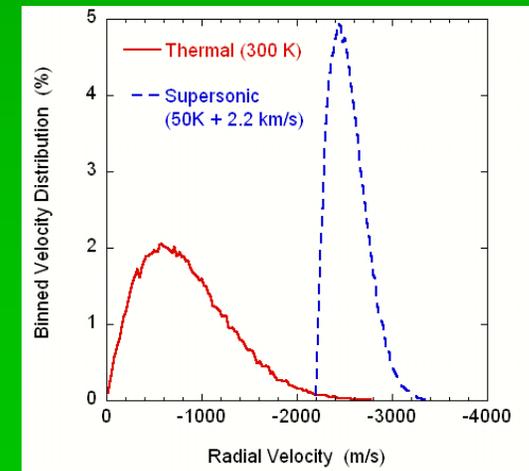
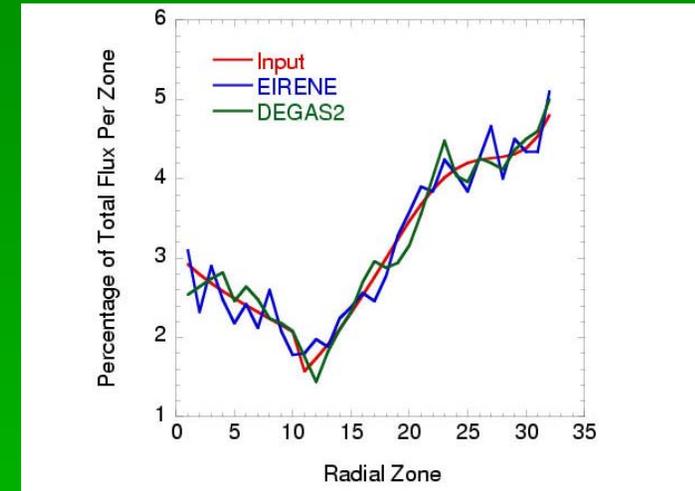
- **Trying different platforms & compilers ensures portability. Duh!!!**
 - Beneficial to do so before your users try it.
- **Some compilers picky about syntax,**
 - “Best” is NAG F95.
- **Compilers / platforms differ in subtle ways,**
 - E.g., handling of uninitialized variables,
 - ⇒ Comparing runs on different systems will help find such bugs.
- **For parallel codes, compare single & multiple processor runs.**

Testing of DEGAS 2 Geometry

- **Tracking flights through problem space is key component of MC algorithm,**
 - Code must always know where flight is!
- **Geometry problems very hard to catch at run time,**
 - E.g., might be very small volume of phase space entered only after $\sim 10^6$ flights.
- **\Rightarrow Essential to test thoroughly during problem development.**
- 1. **Basic consistency checks of geometry objects & connectivity information,**
 - E.g., a surface with something on one side, but nothing on other must be “outer” surface.
- 2. **Divide problem space into “pixels” & track through them,**
 - Same routine used to generate 2-D & 3-D plots.

Testing of Physical & Velocity Space Sampling of DEGAS 2 Sources

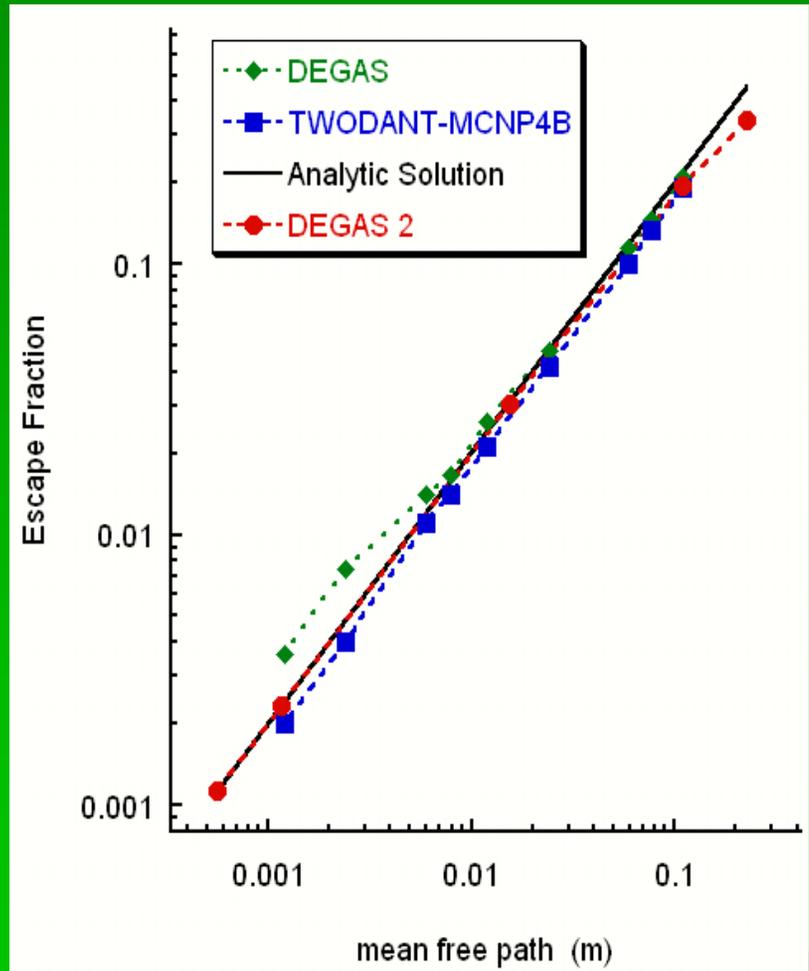
- Know distributions & expected sampling error \Rightarrow verify!
1. Compare sampled distribution of flights over source “segments” with requested distribution,
 - Check scaling of deviations with # flights,
 - Consistency quantified by χ^2 test.
 2. Compare sampled spatial & velocity distribution of source at given segment with expectations,
 - Exact same random number sequence as main code,
 - Dump out each flight x , v as well as averages,
 - Load flight data into KaleidaGraph to check higher moments or make scatter plots.



Tests Against Analytic Solutions

Escape Probability

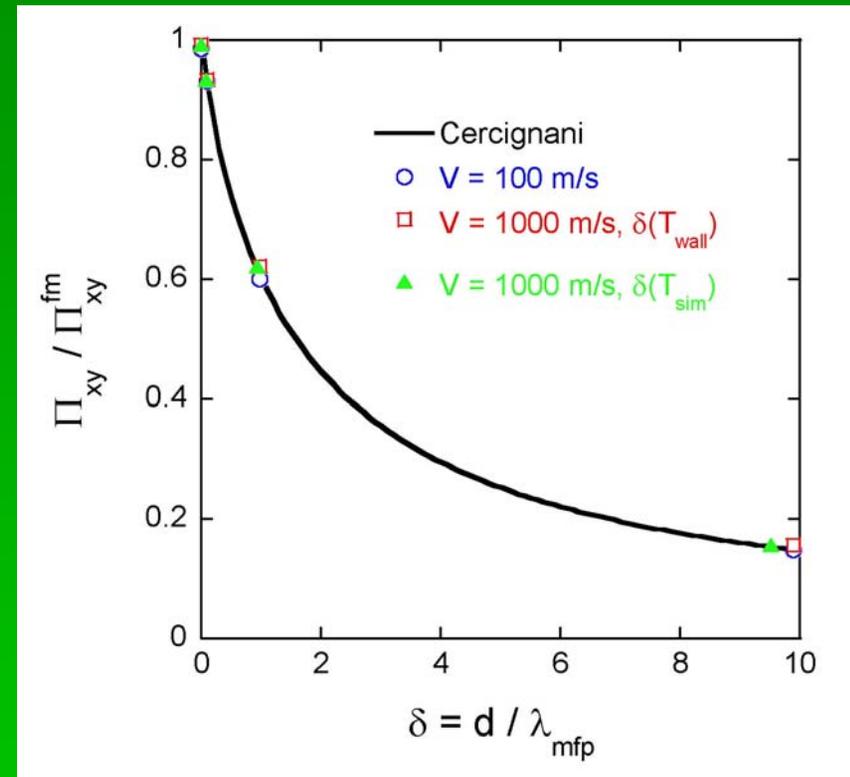
- Volume source in box \gg ionization mfp (courtesy R. Rubilar, ca. 1998)
 - \rightarrow $\text{mfp} * \text{Area} / (4 * \text{Volume})$.
- Old DEGAS had problems due to overlap between “external” & “tracking” meshes.
- Low mfp TWODANT & MCNP data lacked precision.
- What’s missing?
 - Error bars!
 - On analytic expression,
 - & on MC results.



Couette Flow

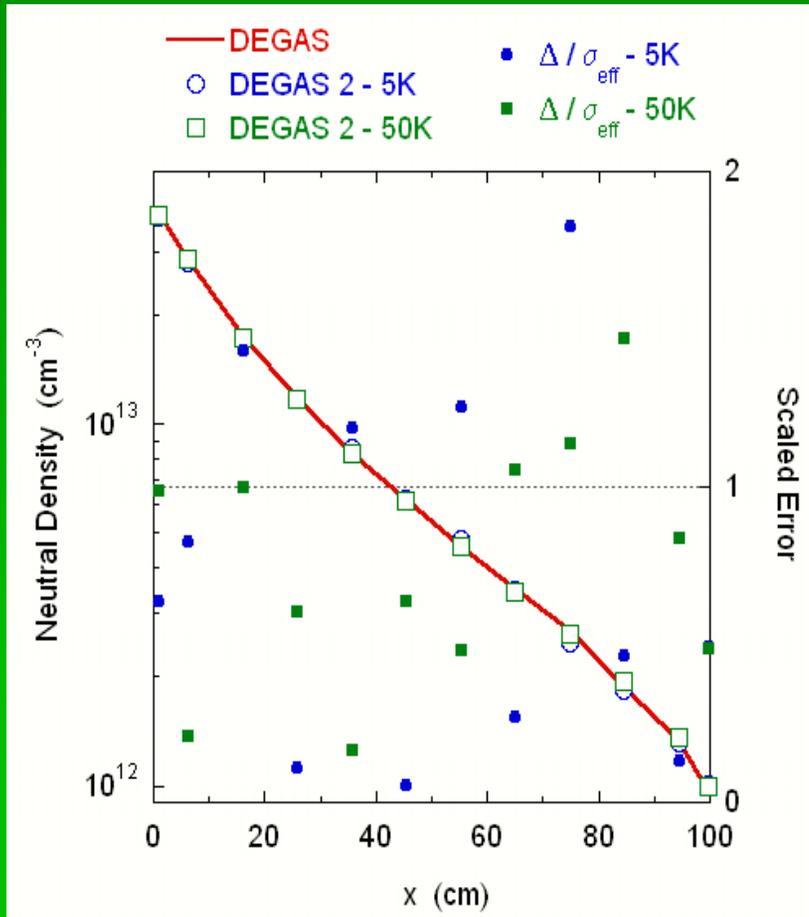
Test of Neutral Viscosity

- Fluid flow between sliding plates, d apart, relative velocity V (courtesy D. Reiter, Chr. May).
- Getting free molecular (kinetic) limit right requires “Maxwell flux” distribution \Rightarrow flux leaving wall = flux hitting wall.
- Still missing error bars,
 - Now have statistical + iterative errors.
- Also have from Reiter & May, 1 & 2 component equilibration tests,
 - Time-dependent & not part of standard DEGAS 2 release.
- Don't be fooled by all this success!
 - BGK model used for neutral-neutral collisions known to get thermal conductivity wrong,
 - Not tested by these cases,
 - \Rightarrow be alert for situations where thermal conductivity matters!



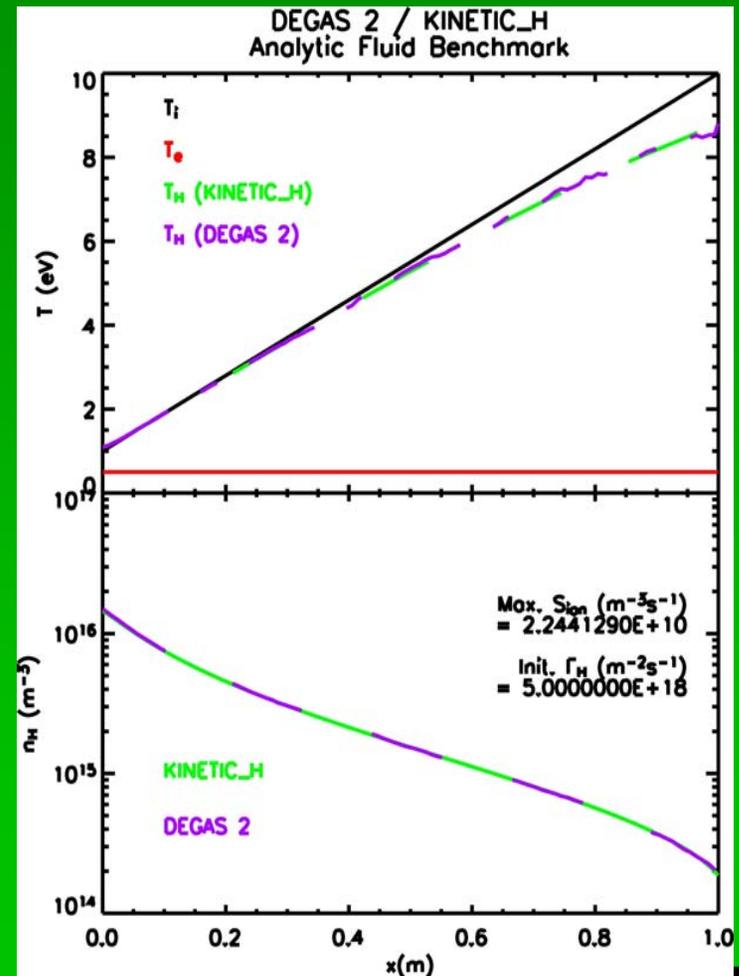
DEGAS 2 – DEGAS Comparison

- Based on variant of analytic fluid model run.
- Roughly same story as in EIRENE benchmark.
- Getting agreement required knowledge of internal operation of both codes:
 - Coordinating meshes,
 - Ensuring $\langle \sigma v \rangle_{CX}$ was same.
- Plot shows error scaled by standard deviation,
 - Relative standard deviations differ by ~ 2 .
 - For uncorrelated errors, should have $68\% < 1$, $95\% < 2$.



DEGAS 2 – KN1D Comparison

- **KN1D: 1-D continuum, kinetic code (B. LaBombard),**
 - Fundamentally different numerical approach complicates resolving discrepancies.
 - Plus, types of possible code modifications different.
- **Initial case: analytic fluid model,**
 - Issues found included CX cross section, v-space resolution,
 - Able to get good match.
- **Subsequent attempts at more realistic modeling (e.g., adding ionization) faltered,**
 - In part due to time constraints.
- **Bottom line on code-code comparisons: anticipate expending considerable resources,**
 - Especially if codes based on different algorithms, have incompatible geometries, etc.

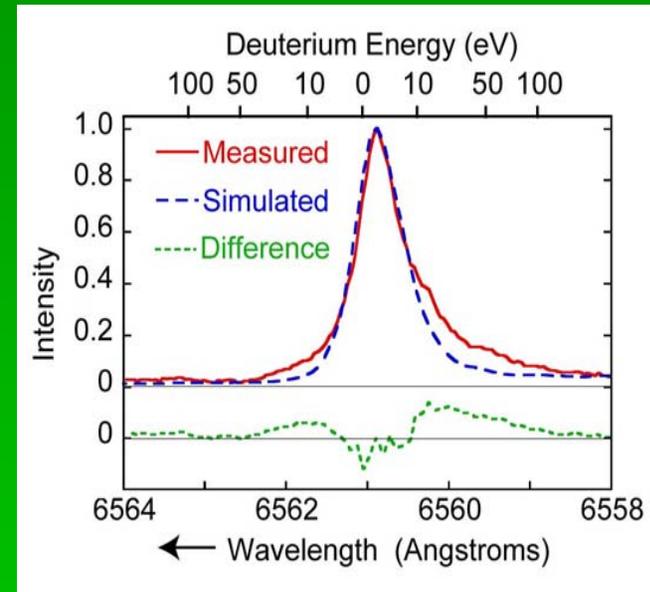


Conservation Checks

- **A legitimate verification test,**
- **Level of difficulty ranges from trivial to great depending on algorithm,**
 - E.g., in DEGAS 2, conservation is exact with “collision” scoring, but statistical with “track length”.
 - Former is still worth doing: used energy conservation to demonstrate that original implementation of BGK collisions was incorrect.
- **Related: symmetry tests,**
 - E.g., If problem & boundary conditions possess some symmetry, does solution?

TFTR H_{α} Spectrum in DT [Stotler 96]

- Actually done with DEGAS, but instructive,
- H_{α} spectrum \leftrightarrow neutral velocity distribution (synthetic diagnostic),
- Plasma n , T & ion fluxes input to DEGAS obtained from TRANSP + SOL plasma model fit using H_{α} chord data,
 - Core data had error bars,
 - Did some sensitivity analyses,
 - But, did no comprehensive error analysis.
- Inferred by process of elimination that spectrum difference due to high energy dissociative recombination of H_2^+ ,
 - Concluded that we needed better data on H_2^+ , including vibrational excitation.
- Very complicated system!
 - Did this really increase confidence in the code?



DEGAS 2 Simulations of C-Mod Gas Conductance Experiments [Stotler 05]

- **Find:**

- Closed: $U_{\text{exp}} = 1.2 \text{ m}^3/\text{s}$, $U_{\text{sim}} = 0.83 \pm 0.06 \text{ m}^3/\text{s}$,
- Open: $U_{\text{exp}} = 4.5 \text{ m}^3/\text{s}$, $U_{\text{sim}} = 7.8 \pm 1.2 \text{ m}^3/\text{s}$.
- In opposite direction! \Rightarrow Single fix unlikely!

- **Simulation error (closed case):**

- MC noise + iterative variation $\sim 0.01 \text{ m}^3/\text{s}$,
- Uncertainty in geometry details: $-0.07 \text{ m}^3/\text{s}$,
- Change in U_{sim} with increased spatial resolution = $0.05 \text{ m}^3/\text{s}$.
 - Issue became apparent following simulations of fluid flow in 3-D square pipe.

- **Experimental errors:**

- Similar pressures measured at multiple locations with different gauge types \Rightarrow error likely small.
- One other parameter: vessel volume = 4.06 m^3 ,
 - Uncertainty unknown,
 - Estimate based on simulated volume $\simeq 3.2 \text{ m}^3$.

