



# Why Should I Believe My Code?

## The Quest for Verification & Validation

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\*Currently: Sarnoff Corporation

# Outline

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- I. **Introduction**
- II. **DEGAS 2 Verification**
  - A. **Code Verification**
  - B. **Solution Verification**
- III. **DEGAS 2 Validation**
- IV. **Dedicated Validation Experiments**

# Introduction

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- **Scientists are supposed to be skeptical!**
  - Treat the code as if it were a perpetual motion machine.
  - [Hatton 97]: “...*the results of scientific calculations carried out by many software packages should be treated with the same measure of disbelief researchers have traditionally attached to results of unconfirmed physical experiments.*”
  - Verification & validation methodologies facilitate this process.
  - These are ongoing efforts ⇒ a quest!
- **Where are we going to get enough manpower & funding to do this?**
  - Effort expended should be commensurate with risk associated with wrong solutions.
  - For most present fusion applications risks are not high,
    - Possible exception: ITER PFC decisions [Skinner, Edge & Pedestal II].
  - ⇒ Might be able to get “good enough” with available resources.
    - But, should always keep in mind how we could do better.
  - Describe V&V of DEGAS 2 as an example,
  - Provide throughout ideas for further discussion.

# DEGAS 2 Uses Monte Carlo Algorithm to Solve Boltzmann Equation for Neutral Species [Stotler 94]

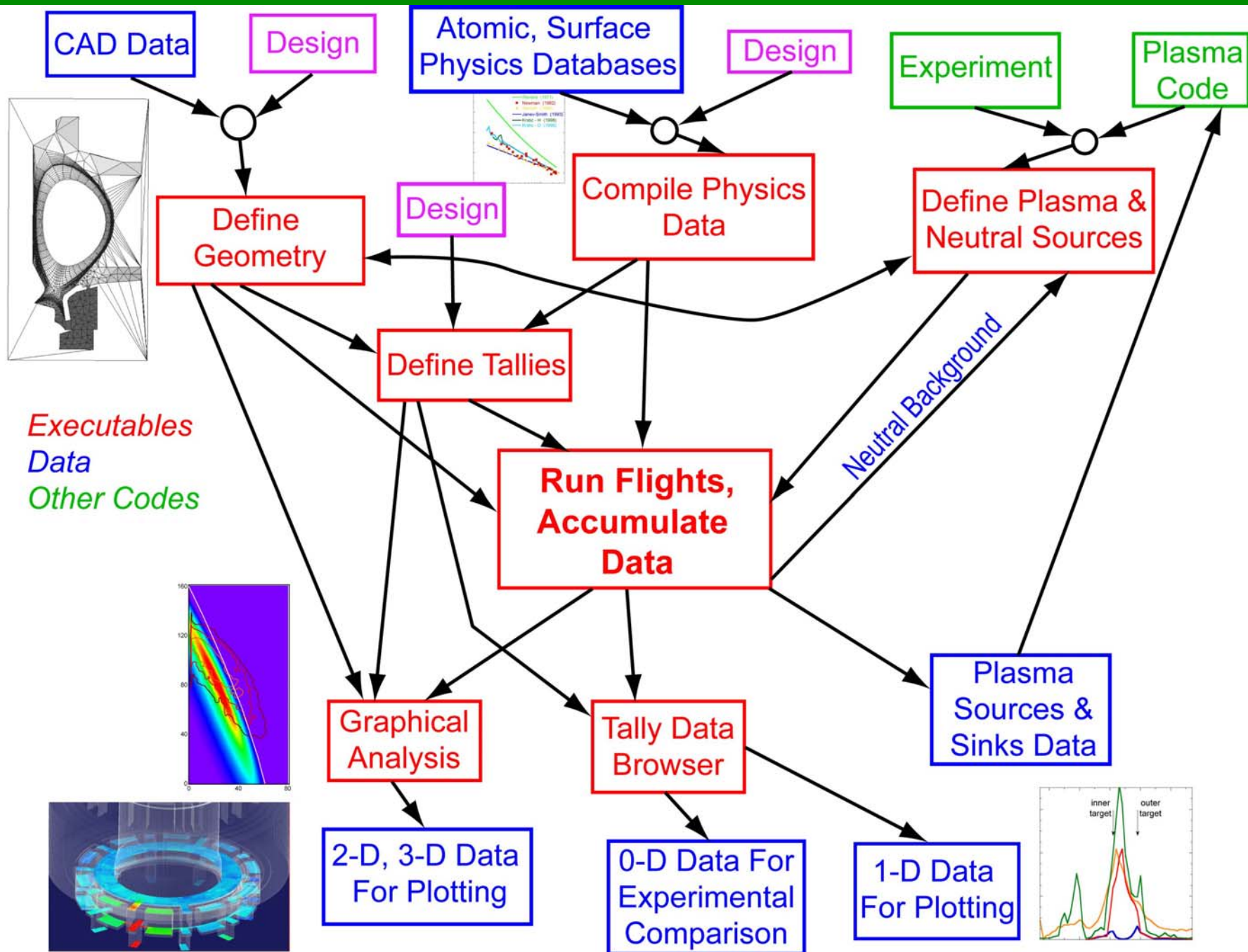
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- **More precisely, compute phase space integrals of form:**

$$I(g) = \int_{\Delta\vec{x}} d^3x \int_{\Delta\vec{v}} d^3v f(\vec{x}, \vec{v}) g(\vec{x}, \vec{v})$$

- **Two good features:**
  - Treat complex geometry & processes,
  - Most aspects of code operation can be understood in analog terms,
    - But, have mathematical basis in central limit theorem, etc.
    - Needed also for non-analog techniques (variance reduction)
- **Drawbacks:**
  - Accuracy of solution scales like  $N^{0.5}$ ,
    - Mitigated by natural parallelism.
  - Comparisons of solutions must be done statistically,
    - I.e., using a mean and a variance.





# Approach to V&V Dictated by Nature of Code Easier for MC?

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- **Modularity simplifies testing of components.**
- **MC code will always converge,**
  - Only question is how fast.
- **MC method naturally provides statistical error,**
  - But, this is only 1 part of total simulation uncertainty!
- **Flexibility facilitates simulating variety of verification problems & experimental situations,**
  - In as much detail as needed.
  - Simulating diagnostic signals straightforward.

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# Code Verification Is About Preventing & Eliminating Bugs – DEGAS 2's Exterminator

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- Use CVS to track code versions & branches.
- Document all non-trivial code.
- `implicit none` – use it, love it.
- Use “assertions” liberally.
- Let the computer do the grungy coding.
- Use a variety of platforms & compilers.
- Check every code change in a debugger.



# What Did You Break This Time?

## Regression Testing

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- **Regression test suite: set of runs performed after code changes to identify problems caused by those changes,**
  - Require results to match previous ones “exactly”,
  - Or that deviations are the ones expected from code modifications.
- **Ideally, would test all aspects of code functionality.**
- **DEGAS 2 has 8 examples,**
  - Most derived from test cases discussed here.
  - Not comprehensive, but do try to add one with each new code capability.
- **matchout code used to compare output files,**
  - Checks every array, printing largest absolute and relative difference,
    - In most cases, this is 0 (to 15 digits).
  - Does statistical comparison, using relative standard deviations in files, for cases in which only statistical agreement is expected.
- **DEGAS 2 examples not ready for automation,**
  - Not quick or easy to run.

# Code Verification

## Ideas for Going Further

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### 1. Static deep-flow analysis tools,

- Imagine a compiler in a really bad mood.
- Source of Hatton's "12 serious faults / 1000 executable FORTRAN lines" [Hatton 97].
- Commercial: **QA C, QA FORTRAN**. Looks for:
  - Coding defects not found by compiler,
  - Non-portable code,
  - Code likely to be difficult to maintain,
  - & Standards violations.
  - Outputs software metrics.
- Freeware: **ftnchek**.

### 2. Dynamic testing,

- Includes regression testing.
- Coverage analysis – which lines of code are executed?
  - Appear to be commercial & freeware packages available.
  - Including Lahey-Fujitsu F95!
  - Can design test cases to hit certain sections of code: glass box testing.
- Black-box testing: have someone else run the code!

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# Checking Code Components Separately Speeds & Simplifies Testing

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- **Test code modifications or new atomic physics / PMI data in isolation,**
- **Check input data for new problems at each stage of workflow,**
- **DEGAS 2 has test routines for:**
  - System-dependent routines,
  - Random number generator,
  - Atomic physics reactions,
  - Plasma-material interactions,
  - Geometry,
  - Sources.

# Integrated Tests of DEGAS 2

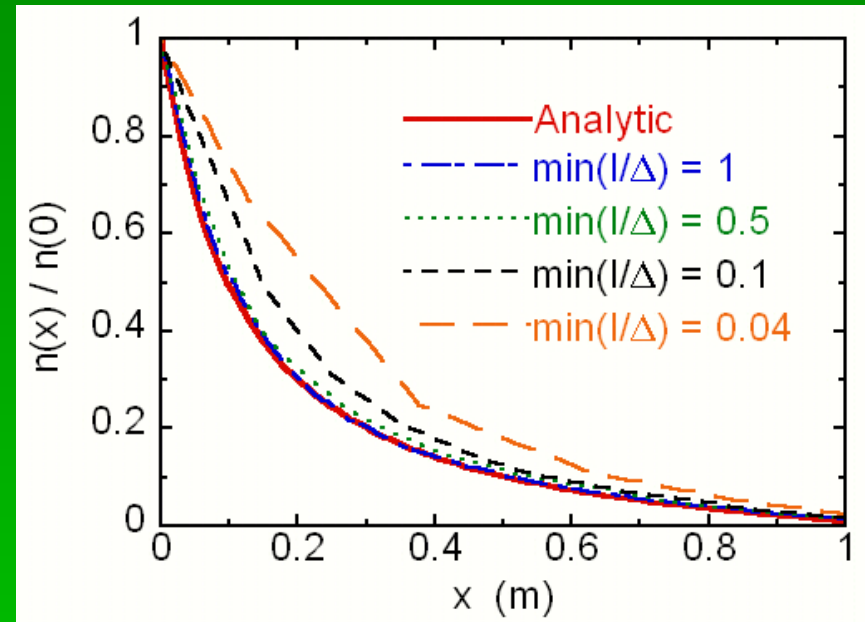
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- **Against analytic solutions,**
  - Escape probability,
  - **1-D analytic fluid model,**
  - Couette flow.
- **Against other codes, aka “benchmarks”,**
  - DEGAS, **EIRENE**, KN1D
  - Checks numerical methods used in both codes,
  - And, gives some idea of impact of different approaches.
- **Some of these are suitable for inclusion in a public collection of test cases,**
  - Certainly for Monte Carlo neutral transport codes,
  - Some are in fluid limit  $\Rightarrow$  test fluid neutral transport codes.
- **Conservation checks are also legitimate verification tests,**
  - Not yet automated in DEGAS 2, but moving towards that.
  - Also symmetry tests.
- **Many simpler checks carried out, but not well documented,**
  - Whenever I see a viable test, I try it!
  - Going forward: compile a record of these.



# Analytic Fluid Neutral Model

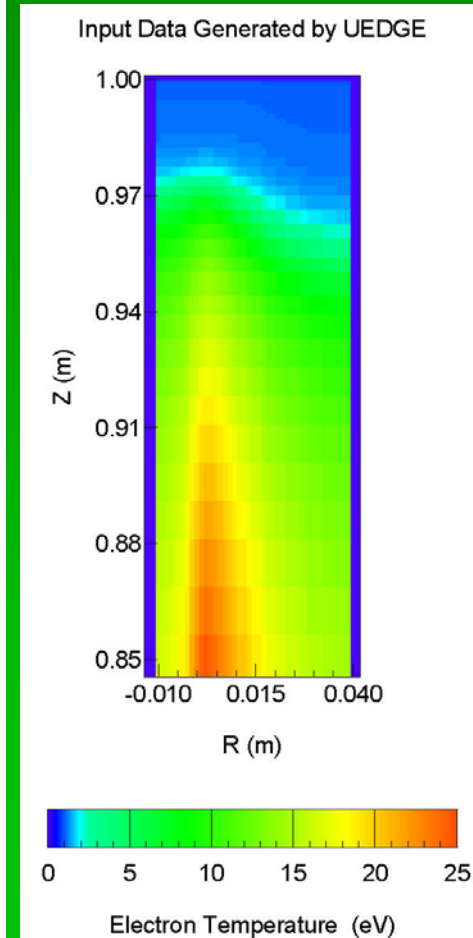
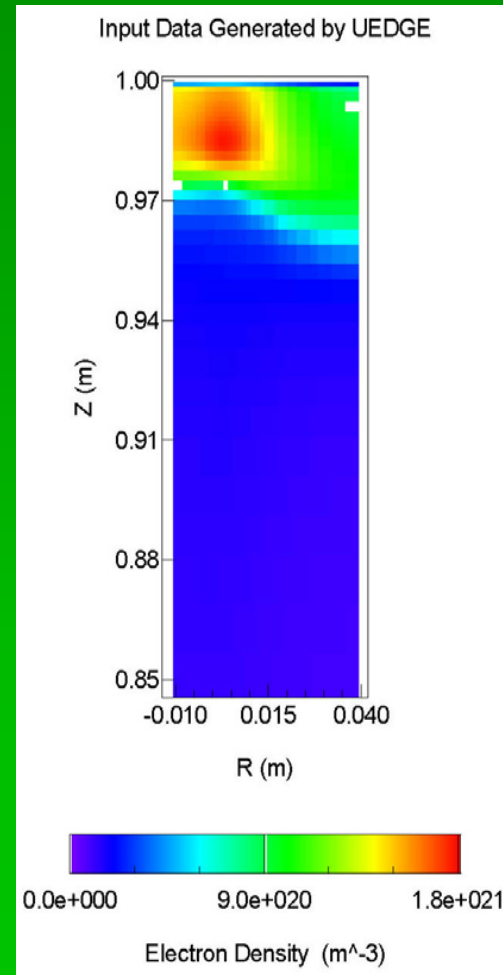
- 1-D fluid neutral momentum balance with constant CX cross section, linearly increasing  $T_i$  [Stotler 97] (courtesy S. Krasheninnikov),
- ~40 cases with DEGAS & DEGAS 2,
- Conclude:
  - $\text{Max}(\text{mfp}/\text{system size}) < 0.1$  for fluid model to be valid,
  - $\text{Min}(\text{mfp}/\text{grid spacing}) > 0.5$  to resolve thermal force.
- Code runs fine even if these are not true,
  - But, problem being simulated differs physically from the one postulated!



# Code-Code Comparisons

## DEGAS 2 – EIRENE

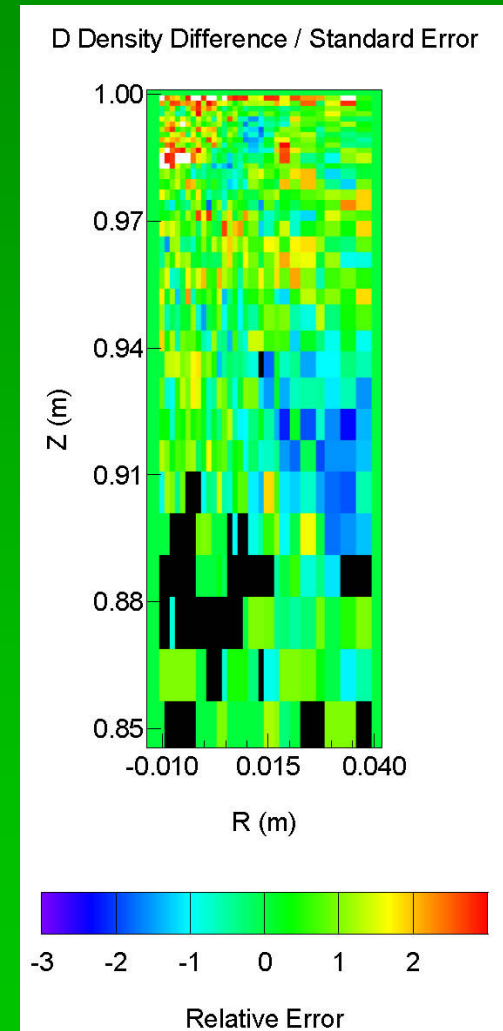
- Details in User's Manual (36 pp.).
- Codes share same basic algorithm & some data,
  - Yet, this was a lengthy exercise.
  - Similar story for DEGAS,
  - Different for KN1D.
- Addressed subtleties in handling of atomic & surface physics, scoring, & interpolation,
  - Required knowledge of internal workings of both.



# Code-Code Comparisons

## DEGAS 2 – EIRENE

- **Compiled histograms of differences normalized to Max(relative standard deviation, systematic error),**
  - Compare histogram with expected fractions to estimate systematic error,
  - Conclude that systematic error is ~5%.
- **Also did performance benchmark,**
  - $\Rightarrow$  Initial optimization of DEGAS 2.



# Solution Verification

## Ideas for Going Further

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- Establish database of verification test cases,
- Quantify accuracy of results [Oberkampf 02],
  - I.e., error trends in convergence studies,
  - Due to spatial and / or temporal discretization,
  - Iterative error,
  - Roundoff error.
  - Estimates will be useful in validation work!
- Analytic solutions
  - Undoubtedly many already exist & have been used,
  - Identify some for addition to test case database.
- Method of manufactured solutions [Roache 02],
  - Concoct solution that will exercise part or all of algorithm,
  - Analytically compute sources & boundary conditions associated with that solution,
  - Use these to set up run of code.
  - Solution need not be physical!
  - Useful solutions can be added to the test case database.
- Run metadata: record of details pertaining to particular run,
  - Code version,
  - Platform & compiler,
  - Location of input & output data files,
  - Else?

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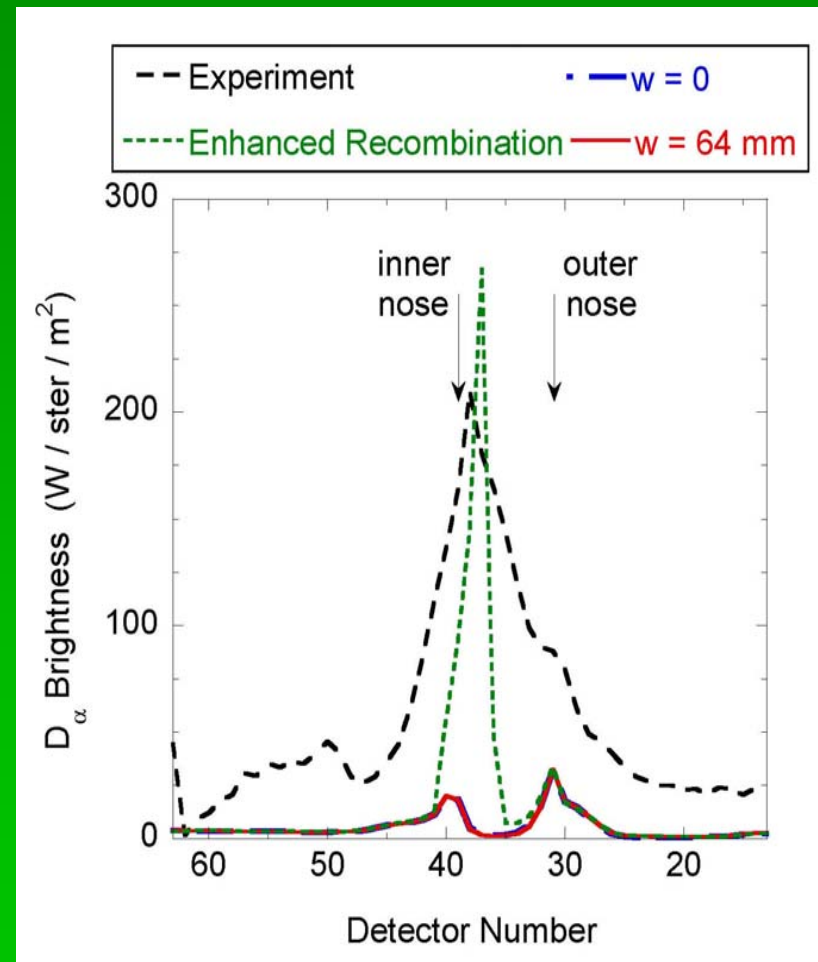
# DEGAS 2 Validation History

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1. TFTR  $H_\alpha$  Spectrum in D-T [Stotler 96]
  2. Alcator C-Mod Divertor Baffling Experiments
  3. NSTX Gas Puff Imaging Experiments
  4. C-Mod Gas Conductance Measurements
- None is an ideal validation in which code is run “blind”,
    - All code runs done after experiment,
    - Some code input based on experimental data.
    - Error analysis could be more rigorous.
  - But, trend over the 4 cases is towards that ideal,
    - Not a conscious effort!
    - Physics content progressively simpler.
  - All cases involved close interaction with experimentalists,
    - Acquire needed details about machine & experiment,
    - Understand subtleties & limitations of diagnostics.

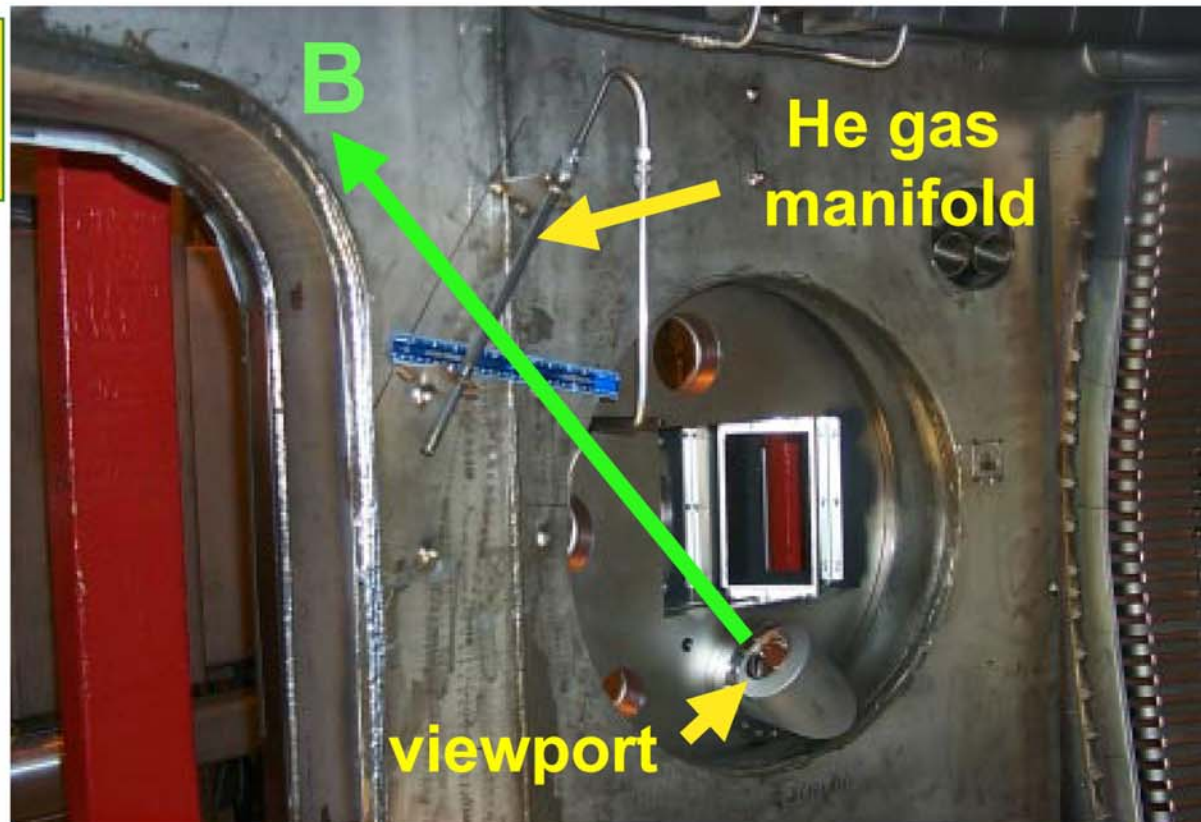
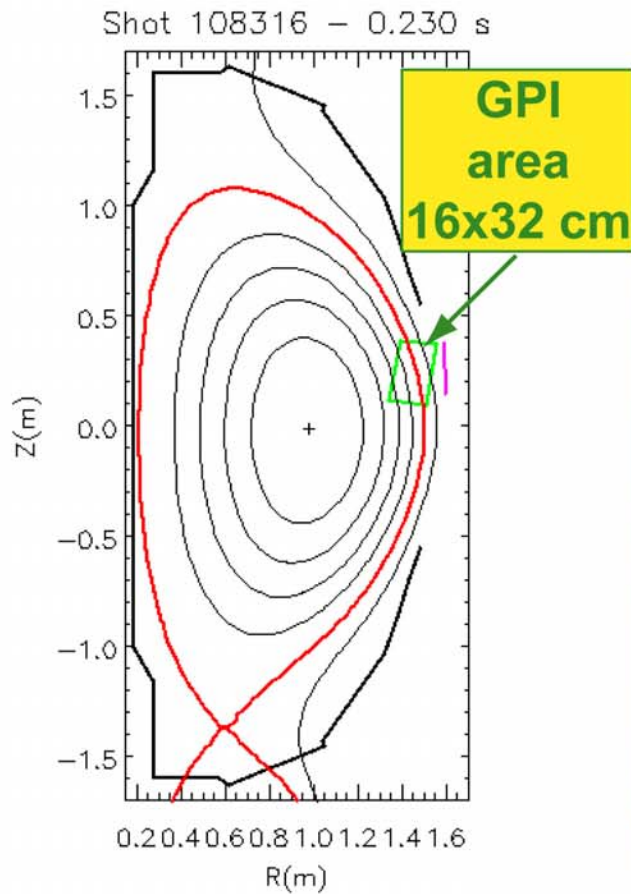
# Alcator C-Mod Divertor Baffling Experiments [Stotler 01]

- Like TFTR case, simulate complex system,
  - Input to code again was experimental plasma data + model to fill in gaps,
  - Used 2-point model  $\Rightarrow$  no adjustable parameters,
  - Assumed divertor neutral pressure dominated by recycling on outer target.
- Found neutral pressures too low by  $\sim 10$ ,
  - Divertor  $D_\alpha$  also off.
  - Concluded that assumed plasma model was inadequate.
- [Lisgo 05] has found that PFR recombination dominates both,
  - Divertor pressure still off by 2 & error bars do not overlap.
  - Photon trapping & 3-D effects matter,
  - Other phenomena may enter
  - $\Rightarrow$  not done adding physics!
- We did learn something,
  - But, did this increase our confidence in the code?



# NSTX Gas Puff Imaging Experiments

## [Zweben 03, poster PI-18]



# NSTX Gas Puff Imaging Experiments

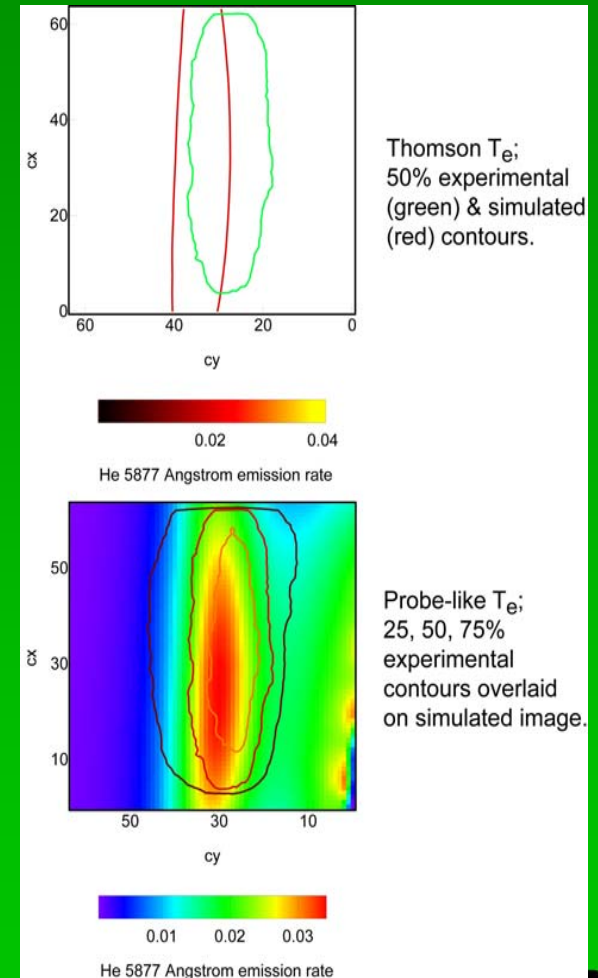
## [Stotler 04]

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- **Our standard list of objectives for DEGAS 2 modeling:**
  1. Demonstrate that we understand physics underlying GPI  $\leftrightarrow$  validation,
  2. Use 3-D model to clarify spatial relationships of physical objects,
  3. Provide neutral density profiles that can be used to unfold 2-D  $n_e$ ,  $T_e$  from camera images. [Myra, Edge & Pedestal I]
- **Still need data from experiment as input:**
  - Equilibrium,
  - Plasma  $n_e$ ,  $T_e$  radial profiles.
- **But, only “model” needed for plasma parameters is that they are constant on flux surface,**
  - GPI experiment poloidally close to Thomson & probe locations.
- **Simulated physics also simpler:**
  - Only neutral source is gas puff,
  - Plasma recycling negligible,
  - Material interactions not significant.
  - Focused only on neutral transport & resulting light emission due to electron excitation,
  - Use of He as puffed gas reduces required atomic physics.
- **Another example of direct simulation of diagnostic, the 64x64 pixel camera view,**
  - Able to compare directly with experimental images,
  - Yielded 2-D, effective neutral density data used by Lodestar.

# Could This Be A “Slam Dunk”?

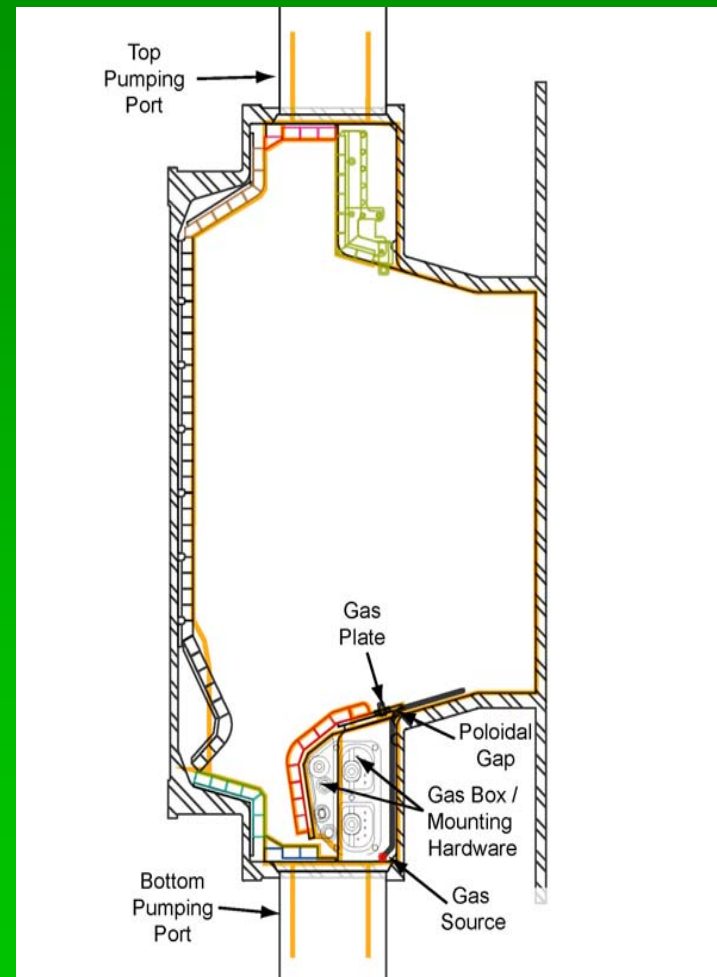
- **1<sup>st</sup> complication: doing steady-state simulation, with constant on flux surface plasma, of time-varying, 3-D plasma,**
  - Only have 1 or 2 TS profiles near GPI time.
  - Assume TS profile  $\leftrightarrow$  equilibrium,
  - & Compare with “median” experimental image computed from entire movie.
- **2<sup>nd</sup> complication: far SOL probe  $T_e \gg$  TS  $T_e$ ,**
  - Discrepancy not surprising given large blobs there.
- **Within error bars (not shown), simulated & experimental image peak locations agree.**
- **But, to really understand would need to account for impact of 3-D & time variation on TS & probe data as well as on emission cloud!**





# C-Mod Gas Conductance Measurements [LaBombard 03]

- Experiments were specifically designed to answer questions raised in modeling of divertor baffling experiments,
  - I.e., to validate the simulation codes!
- Focus here on measurements made without plasma,
  - Two cases: gas puff in open & closed divertor.
- ⇒ isolate physics components
  - Neutral viscosity,
  - 3-D representation of geometry.



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# Dedicated Validation Experiments

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- “...validation experiments are indeed different from traditional experiments.” [Oberkampf 02],
  - Primary distinction is that the code & code developer are primary customers.
- Not incompatible with present modes of operation,
  - But, making real progress with validation will require shift in priorities.
- Revisit some guidelines in [Oberkampf 04]:
  - Should be designed jointly by experimentalists & simulation scientists,
  - Experiment should measure all quantities needed as input to code,
  - Exploit synergies between code & experiment,
    - E.g., design experiment to offset a code weakness,
    - Use exploratory code runs to identify needed measurements.
  - Keep experimental & code results independent, i.e., blind comparison.
- [Oberkampf 02] goes on to discuss validation metrics,
  - Involving experimental & simulation uncertainties,
  - Postpone consideration for now.

# Opportunities for Validation Experiments

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- **Comparing simulation results against tokamak discharges represents the top level of the validation hierarchy,**
  - If they don't match, how do you know where the model is going wrong?
  - Developing confidence in model requires going through entire hierarchy,
  - Focus here on lowest level(s).
- **My experience (this talk): even simplest benchmarks or experimental comparisons are worthwhile,**
  - Rarely as simple as they seemed,
  - Always learn something.
  - Even demonstrating that physics is different than in full system constitutes progress.
- **Plasma turbulence codes may be good place to start,**
  - At or close to “first principles”  $\Rightarrow$  no adjustable parameters,
  - **Universal character of edge turbulence [Zweben 04]  $\Rightarrow$  conceivably could make significant progress w/o tokamak experiments.**
- **Dedicated validation experiments ideal for university environment,**
  - Relatively small scale compatible with typical university funding,
  - Multiple diagnostics  $\Rightarrow$  opportunities for student involvement.
  - Requisite connection with code developers & theorists would keep university researchers & primary fusion labs closely coupled.
- **Ideas for possible validation experiments?**
  - Will need expertise of both experimentalists & simulation scientists,
  - **TTF is perfect forum for this!**

# Conclusions / Discussion

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- **Code verification**
  - Tools for improving software quality,
  - Static deep-flow analysis,
  - Dynamic testing.
- **Solution verification**
  - Database of accurate test cases from analytic results & MMS.
  - Code-code comparisons: may be tough!
  - Quantify accuracy of results.
  - Run metadata?
- **Code Validation**
  - Simulating full tokamak behavior may provide limited insight,
  - More constrained experiments can still be challenging.
- **Dedicated Validation Experiments**
  - Code is the primary customer!
  - Can we design experiments for lowest tier of hierarchy?
- **See also the V&V talks in the parallel sessions**
  - **Core Working Group II Thursday 10:10 – 11:30**
  - **Core Working Group V Friday 3:00 – 4:15**



# References

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- **[LaBombard 03]** B. LaBombard and C. J. Boswell, “In-Situ Gas Conductance and Flow Measurements Through Alcator C-Mod Divertor Structures With and Without Plasma Present”, MIT PSFC Tech. Report PSFC/RR-03-6 (2003).
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- **[Oberkampf 02]** W. L. Oberkampf and T. G. Trucano, “Verification and Validation in Computational Fluid Dynamics”, *Prog. in Aero. Sci.* **38**, 209 (2002).
- **[Oberkampf 04]** W. L. Oberkampf, “Verification and Validation in Computational Simulation”, Transport Task Force Meeting, Salt Lake City, Utah (April 2004).
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- **[Roache 02]** P. J. Roache, “Code Verification by the Method of Manufactured Solutions”, *ASME J. Fluids Eng.* **124**, 4 (2002).

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- **[Stotler 94]** D. P. Stotler and C. F. F. Karney, “Neutral Gas Transport Modeling with DEGAS 2”, *Contrib. Plasma Phys.* **34**, 392 (1994). See also <http://w3.pppl.gov/degas2>
- **[Stotler 96]** D. P. Stotler et al., “Modeling of Neutral Hydrogen Velocities in the Tokamak Fusion Test Reactor”, *Phys. Plasmas* **3**, 4084 (1996).
- **[Stotler 97]** D. P. Stotler et al., “DEGAS 2 Neutral Transport Modeling of High Density, Low Temperature Plasmas”, 16<sup>th</sup> International Conference on Plasma Physics and Controlled Nuclear Fusion Research (Montreal, Canada, October 1996) (IAEA, Vienna, Austria, 1997), Vol. **2**, p. 633.
- **[Stotler 01]** D. P. Stotler et al., “Modeling of Alcator C-Mod Divertor Baffling Experiments”, *J. Nucl. Mater.* **290-293**, 967 (2001).
- **[Stotler 04]** D. P. Stotler et al., “Three-Dimensional Neutral Transport Simulations of Gas Puff Imaging Experiments”, *Contrib. Plasma Phys.* **44**, 294 (2004).
- **[Stotler 05]** D. P. Stotler and B. LaBombard, “Three-Dimensional Simulation of Gas Conductance Measurement Experiments on Alcator C-Mod”, *J. Nucl. Mater.* **337-339**, 510 (2005).
- **[Zweben 03]** S. J. Zweben et al., “High-Speed Imaging of Edge Turbulence in NSTX”, *Nucl. Fusion* **44**, 134 (2004).

# **Supplementary Slides**

# What is DEGAS 2?

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- **A Monte Carlo neutral transport code [Stotler 94]**
  - **Fast, efficient**
    - Parallelization built in at the start
    - Most arrays allocated dynamically
  - **Portable**
    - Karney's parallel random number generator
    - Most data exchanges via netCDF files
  - **Easy to add new physics**
  - **Written in FWEB,**
    - Grungy tasks handled by macro preprocessor,
    - TeX documentation interwoven with code.
  - **Statistics:**
    - 31 executables:
      - Main code
      - 13 setup
      - 10 test
      - 7 post-processor
    - ~120 source files
    - Source code (including internal documentation): ~70K lines.
    - 85 atomic & surface physics data files

# Does CVS Stand for “Crummy, Vexing Software”?

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- **Use CVS (Concurrent Version System) to maintain code versions,**
  - Including binary data & output files!
  - “Tags” keep track of code releases & branches.
  - CVS has no “undo”  $\Rightarrow$  be careful!

# I Don't Have Time to Write Documentation!

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- **Write documentation as code is being developed,**
  - Especially in source code,
    - Explain less-than-obvious code,
    - You'll be glad you did in ~3 years.
    - Be sure comments & source code agree!
  - Where applicable, refer to equations & expressions in published literature.
- **Compile a User's Manual,**
  - Writing comprehensive manual very time consuming,
  - Many sections of DEGAS 2 User's Manual were written first for posters or talks,
    - It is my reference of choice for these topics!
- **Document reference data files,**
  - E.g., DEGAS 2's atomic and plasma-surface interaction data files.
  - Have one file containing brief description of origin of each data file.
  - Atomic physics data generated by codes I run are also tracked by CVS.

```
if (Day.eq.'Thursday') then
    x = 2.
else
    x = 3.
end if
```

# Implicit None: Use It, Love It

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- **Primary value is to catch misspelled variable names.**
- **Much easier to have compiler point them out to you than to track down an obscure bug at run time.**
- **Strong typing (e.g., Java) would be even better.**



# `assert(cell_intersect < geom_infinity)`

---

- An “assertion” checks conditions that ought to be true,
  - Print warning,
  - And / or stop code.
- If a line of code makes some assumption about a variable in it, check it! E.g.,
  - Array index  $\leq$  dimension,
  - Denominator  $\neq 0$ ,
  - Particle is still in problem space.
- Very useful in catching memory corruption,
  - Memory corruption can make the “impossible” come true.
- In DEGAS 2, used in:
  - All setup, testing, and codes,
  - Some post-processing codes,
  - Initial runs of main program.
  - Disabled for production runs.

# Let Computer Do Grungy Coding

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- **DEGAS 2 uses FWEB based macros to:**
  - Handle dynamic memory allocation,
  - Specify common blocks, including with MPI,
  - Read & write netCDF files.
- **E.g., the string `gi_ncread(fileid)` expands to ~280 lines of code I don't have to maintain.**
- **Represents “heroic” application of FWEB by Karney,**
  - Not clear how to best do this in general.

# Suns are From Venus, Linux Machines are From Mars

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- **Trying different platforms & compilers ensures portability. Duh!!!**
  - Beneficial to do so before your users try it.
- **Some compilers picky about syntax,**
  - “Best” is NAG F95.
- **Compilers / platforms differ in subtle ways,**
  - E.g., handling of uninitialized variables,
  - $\Rightarrow$  Comparing runs on different systems will help find such bugs.
- **For parallel codes, compare single & multiple processor runs.**

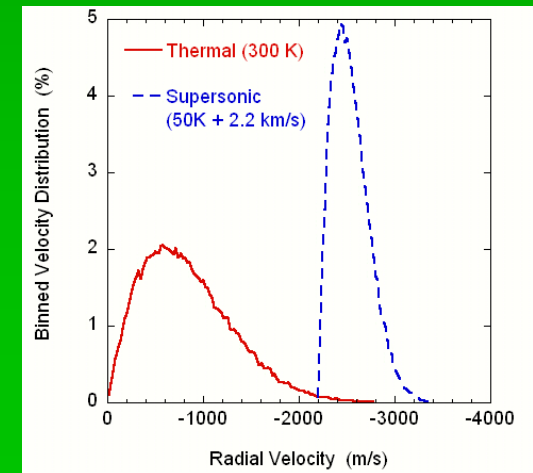
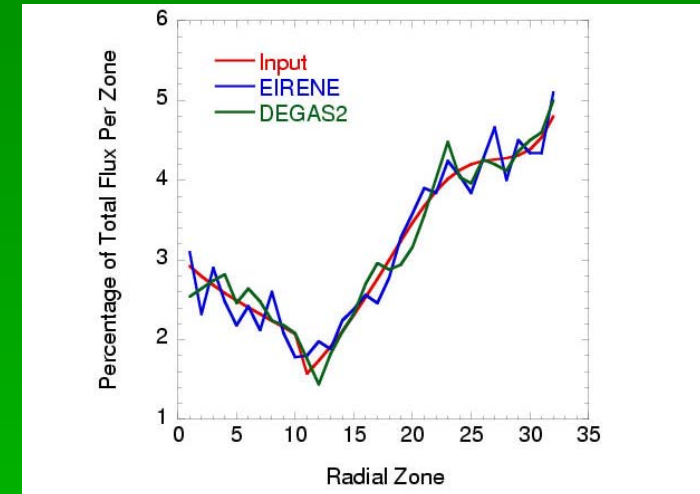
# Testing of DEGAS 2 Geometry

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- **Tracking flights through problem space is key component of MC algorithm,**
  - Code must always know where flight is!
- **Geometry problems very hard to catch at run time,**
  - E.g., might be very small volume of phase space entered only after  $\sim 10^6$  flights.
- **$\Rightarrow$  Essential to test thoroughly during problem development.**
- 1. **Basic consistency checks of geometry objects & connectivity information,**
  - E.g., a surface with something on one side, but nothing on other must be “outer” surface.
- 2. **Divide problem space into “pixels” & track through them,**
  - Same routine used to generate 2-D & 3-D plots.

# Testing of Physical & Velocity Space Sampling of DEGAS 2 Sources

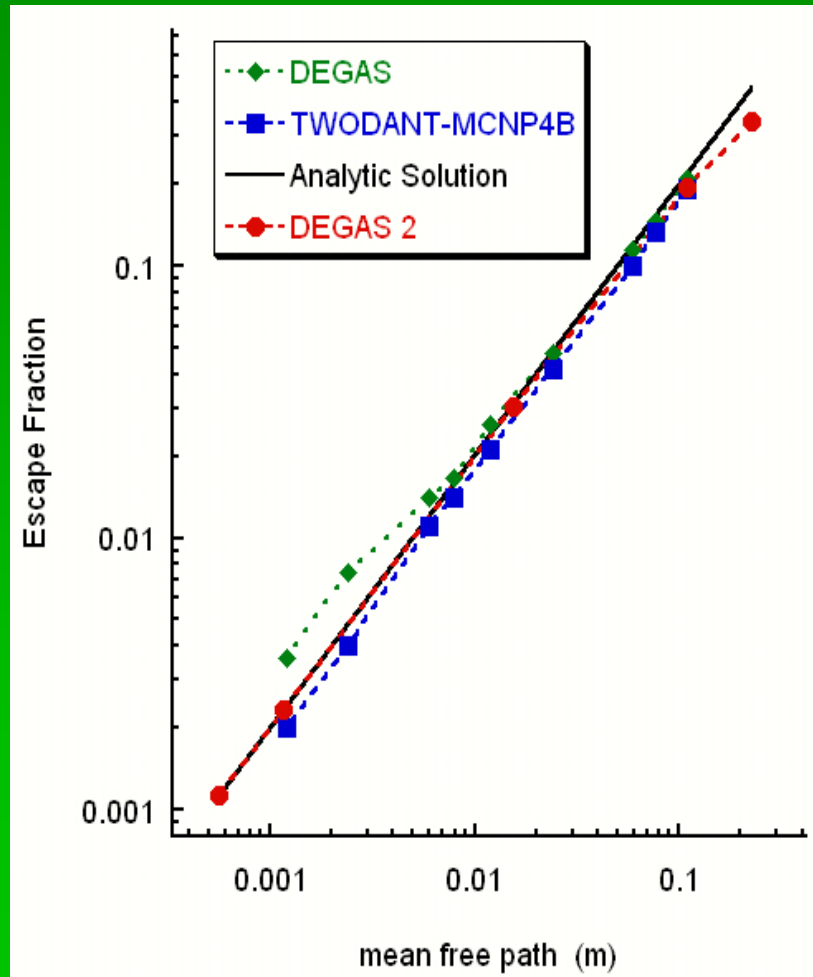
- Know distributions & expected sampling error  $\Rightarrow$  verify!
1. Compare sampled distribution of flights over source “segments” with requested distribution,
    - Check scaling of deviations with # flights,
    - Consistency quantified by  $\chi^2$  test.
  2. Compare sampled spatial & velocity distribution of source at given segment with expectations,
    - Exact same random number sequence as main code,
    - Dump out each flight  $x$ ,  $v$  as well as averages,
      - Load flight data into KaleidaGraph to check higher moments or make scatter plots.



# Tests Against Analytic Solutions

## Escape Probability

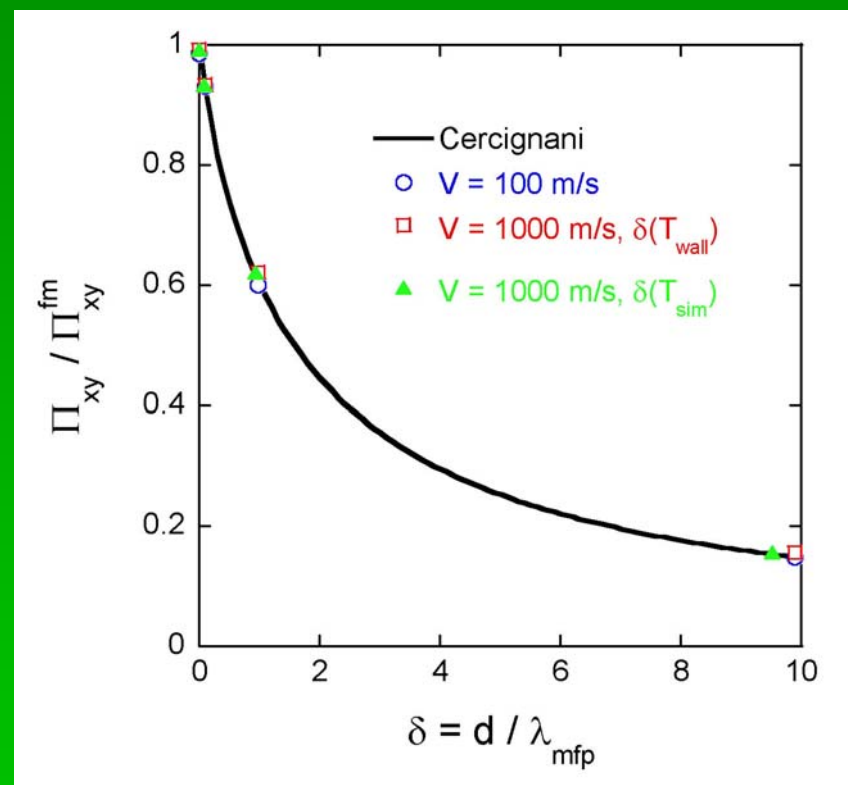
- Volume source in box  $\gg$  ionization mfp (courtesy R. Rubilar, ca. 1998)
  - $\rightarrow \text{mfp} * \text{Area} / (4 * \text{Volume})$ .
- Old DEGAS had problems due to overlap between “external” & “tracking” meshes.
- Low mfp TWODANT & MCNP data lacked precision.
- What’s missing?
  - Error bars!
  - On analytic expression,
  - & on MC results.



# Couette Flow

## Test of Neutral Viscosity

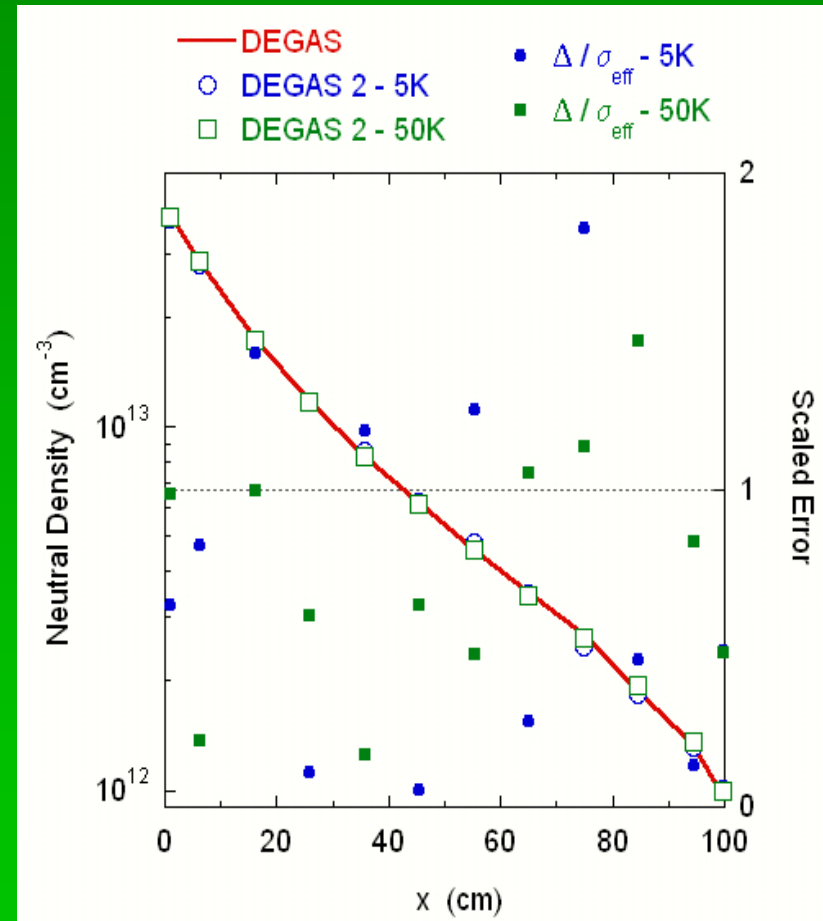
- Fluid flow between sliding plates,  $d$  apart, relative velocity  $V$  (courtesy D. Reiter, Chr. May).
- Getting free molecular (kinetic) limit right requires “Maxwell flux” distribution  $\Rightarrow$  flux leaving wall = flux hitting wall.
- Still missing error bars,
  - Now have statistical + iterative errors.
- Also have from Reiter & May, 1 & 2 component equilibration tests,
  - Time-dependent & not part of standard DEGAS 2 release.
- Don't be fooled by all this success!
  - BGK model used for neutral-neutral collisions known to get thermal conductivity wrong,
  - Not tested by these cases,
  - $\Rightarrow$  be alert for situations where thermal conductivity matters!





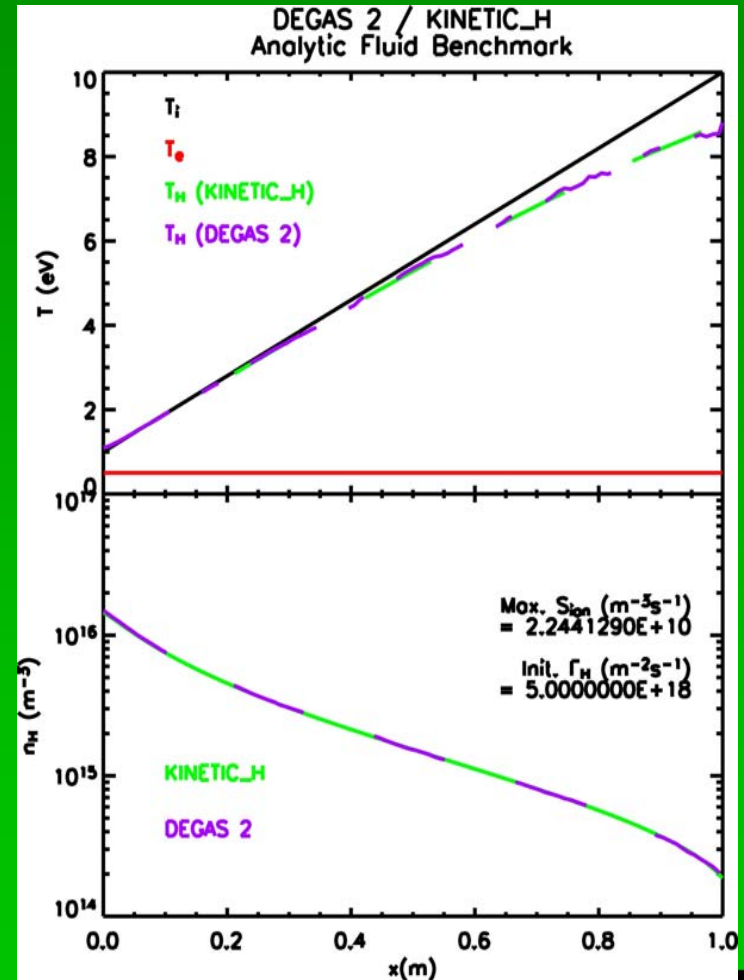
# DEGAS 2 – DEGAS Comparison

- Based on variant of analytic fluid model run.
- Roughly same story as in EIRENE benchmark.
- Getting agreement required knowledge of internal operation of both codes:
  - Coordinating meshes,
  - Ensuring  $\langle \sigma v \rangle_{CX}$  was same.
- Plot shows error scaled by standard deviation,
  - Relative standard deviations differ by  $\sim 2$ .
  - For uncorrelated errors, should have  $68\% < 1$ ,  $95\% < 2$ .



# DEGAS 2 – KN1D Comparison

- **KN1D: 1-D continuum, kinetic code (B. LaBombard),**
  - Fundamentally different numerical approach complicates resolving discrepancies.
  - Plus, types of possible code modifications different.
- **Initial case: analytic fluid model,**
  - Issues found included CX cross section, v-space resolution,
  - Able to get good match.
- **Subsequent attempts at more realistic modeling (e.g., adding ionization) faltered,**
  - In part due to time constraints.
- **Bottom line on code-code comparisons: anticipate expending considerable resources,**
  - Especially if codes based on different algorithms, have incompatible geometries, etc.



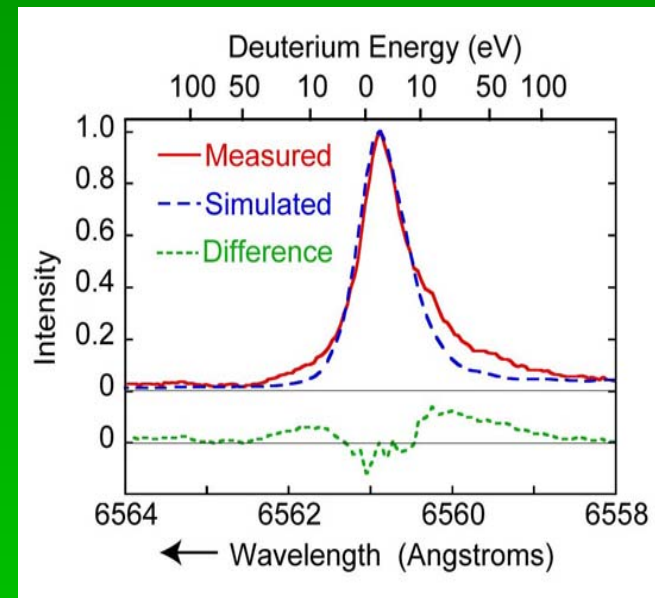
# Conservation Checks

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- A legitimate verification test,
- Level of difficulty ranges from trivial to great depending on algorithm,
  - E.g., in DEGAS 2, conservation is exact with “collision” scoring, but statistical with “track length”.
  - Former is still worth doing: used energy conservation to demonstrate that original implementation of BGK collisions was incorrect.
- Related: symmetry tests,
  - E.g., If problem & boundary conditions possess some symmetry, does solution?

# TFTR $H_{\alpha}$ Spectrum in DT [Stotler 96]

- Actually done with DEGAS, but instructive,
- $H_{\alpha}$  spectrum  $\Leftrightarrow$  neutral velocity distribution (synthetic diagnostic),
- Plasma  $n$ ,  $T$  & ion fluxes input to DEGAS obtained from TRANSP + SOL plasma model fit using  $H_{\alpha}$  chord data,
  - Core data had error bars,
  - Did some sensitivity analyses,
  - But, did no comprehensive error analysis.
- Inferred by process of elimination that spectrum difference due to high energy dissociative recombination of  $H_2^+$ ,
  - Concluded that we needed better data on  $H_2^+$ , including vibrational excitation.
- **Very complicated system!**
  - Did this really increase confidence in the code?



# DEGAS 2 Simulations of C-Mod Gas Conductance Experiments [Stotler 05]

- **Find:**

- Closed:  $U_{\text{exp}} = 1.2 \text{ m}^3/\text{s}$ ,  $U_{\text{sim}} = 0.83 \pm 0.06 \text{ m}^3/\text{s}$ ,
- Open:  $U_{\text{exp}} = 4.5 \text{ m}^3/\text{s}$ ,  $U_{\text{sim}} = 7.8 \pm 1.2 \text{ m}^3/\text{s}$ .
- In opposite direction!  $\Rightarrow$  Single fix unlikely!

- **Simulation error (closed case):**

- MC noise + iterative variation  $\sim 0.01 \text{ m}^3/\text{s}$ ,
- Uncertainty in geometry details:  $-0.07 \text{ m}^3/\text{s}$ ,
- Change in  $U_{\text{sim}}$  with increased spatial resolution =  $0.05 \text{ m}^3/\text{s}$ .
  - Issue became apparent following simulations of fluid flow in 3-D square pipe.

- **Experimental errors:**

- Similar pressures measured at multiple locations with different gauge types  $\Rightarrow$  error likely small.
- One other parameter: vessel volume =  $4.06 \text{ m}^3$ ,
  - Uncertainty unknown,
  - Estimate based on simulated volume  $\simeq 3.2 \text{ m}^3$ .

