Secondary electron emission from dielectric materials of a Hall thruster with segmented electrodes

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The discharge parameters in Hall thrusters depend strongly on the yield of secondary electron emission. Comparative measurements of the yield of secondary electron emission at low energies of primary electrons were performed for several dielectric materials used in Hall thrusters with segmented electrodes. The measurements showed that at low energies of primary electrons the actual energetic dependencies of the total yield of secondary electron emission could differ from fits, which are usually used in theoretical models. The observed differences might be caused by electron backscattering, which is dominant at lower energies and depends strongly on surface properties. Fits based on power or linear laws are relevant at higher energies of primary electrons, where the bulk material properties play a decisive role. © 2003 American Institute of Physics. [DOI: 10.1063/1.1568344]

I. INTRODUCTION

Plasma–wall interaction is one of the key processes in the physics of Hall thrusters. The material of the channel wall determines the difference between so-called stationary plasma thrusters (SPTs), where the channel is made of dielectric ceramics, and thrusters with anode layer (TAL) with metal channel walls. Higher secondary electron emission (SEE) from ceramic walls in SPTs might be a reason for lower electron temperature and longer acceleration region compared to TALs. According to the model of a SPT suggested by Ahedo, the potential drops on both the inner and outer sheath and presheath, and, as a result, the electron losses on the channel walls depend strongly on the yield of SEE. The distribution of the electron temperature along the SPT channel is also affected by SEE. In numerical simulations by Keidar et al., a change in the SEE coefficient from 0.95 to 0.8 leads to an increase of the peak value of $T_e$ from 16 to 30 eV. The effect of the electron backflow parameters on the sheath potential was shown in the original work of Hobbs and Wesson. Assuming a Boltzmann distribution for plasma electrons, the potential drop on the sheath in the presence of secondary electron emission could be expressed as

$$\varphi = kT_e \ln \left( \frac{1 - \sigma(T_e)}{V_0 \sqrt{2 \pi m_e kT_e}} \right).$$

Here $\sigma(T_e)$ is the total yield of secondary electron emission at the plasma electron temperature $T_e$, defined as a ratio of secondary emission flux to the primary flux. The model of Hobbs and Wesson does not consider the plasma-sheath transition and assumes that the velocity at the sheath edge, $V_0$, is equal to the Bohm velocity. In modern models of SPT, the actual radial velocity at the sheath edge is considered as different from the Bohm velocity and is calculated from presheath models in the presence of the SEE flux.

The dependence $\sigma(T_e)$ is usually derived by averaging of the dependence of $\sigma(E_p)$ on the energy of the primary electrons, $E_p$, over the Maxwellian distribution of $E_p$. At present, however, there are no systematic data for $\sigma(E_p)$ at $10 < E_p \approx 100$ eV for most modern ceramics and dielectric materials. Existing theories of SEE are able to predict the behavior of $\sigma(E_p)$ analytically only at $E_p > 80$–100 eV. Therefore, the yield of SEE in SPT models is usually determined from various fits. Ahedo and Jolivet and Roussel used a power law to fit the slope $\sigma(E_p)$ as

$$\sigma(E_p) = \left( \frac{E_p}{E_1} \right)^{\alpha},$$

where $E_1$ is a reference energy. In Sec. IV we discuss the results of SEE measurements from boron nitride, quartz, and macor.

II. REVIEW OF THE ROLE OF SEE IN PLASMA SHEATH

The role of electron emission from the wall on the sheath potential was shown in the original work of Hobbs and Wesson. Assuming a Boltzmann distribution for plasma electrons, the potential drop on the sheath in the presence of secondary electron emission could be expressed as

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where $E_1$ corresponds to $\sigma = 1$. The average over the Maxwellian distribution yields

$$\langle \sigma(E_p) \rangle = (E_p)^{\alpha} \Gamma(2 + \alpha)(2E_1)^{-\alpha} \approx (E_p)^{\alpha} \Gamma(2 + \alpha) b.$$  

(3)

The same fit was used by Choueiri with $b = 0.141$ and $\alpha = 0.567$ for boron nitride.\(^2\)

The fit of $\sigma(E_p)$ based on a power law assumes the monotonic decrease of the total SEE yield to zero with the decrease of $E_p$. The same nature of $\sigma(E_p)$ is conjectured by the majority of authors who deal with interactions of low temperature plasmas with dielectric walls. However, the contribution of backscattered electrons in the total backflow grows with the decrease of $E_p$. Consequently, the behavior of $\sigma(E_p)$ from dielectric materials should be more complicated in the low energy region, as follows from our measurement presented in the following.

**III. EXPERIMENTAL SETUP**

Direct measurements of the yield of SEE at low energies of primary electrons are difficult because of the charging of the sample surface. Indeed, the surface will acquire a positive charge if the flux of secondary electrons is higher than primary flux, and negative in the opposite case. The electric field of the surface charge changes the energy of primary electrons. This electric field may also impede or facilitate the yield of low energy “true” secondary electrons. The uncertainty in measurements induced by surface charging should reach several times.\(^{15}\)

In order to minimize the influence of the surface charging, the primary electron beam can be modulated by short pulses, as was proposed in earlier works by Heydt\(^16\) and Johnson.\(^15\) The amplitude of the primary current and the duration of the current pulse should be short in order to minimize the surface charging. The total current in the sample circuit, $I_s$, can be expressed as\(^{17}\)

$$I_s = C \frac{d\varphi_s}{dt} + I_c,$$  

(4)

where $I_c$ is the leakage current due to surface conductivity, $\varphi_s$ is the surface potential, and $C$ is the sample capacitance. Assuming $I_c = 0$, which is correct for the most dielectric materials with low surface conductivity, the surface potential will increase linearly along with the current pulse of the primary electron beam

$$\varphi_s = \frac{I_p d}{\varepsilon \varepsilon_0 4\pi r^2} t.$$  

(5)

Here $d$ and $\varepsilon$ are the sample thickness and the dielectric constant, and $r$ is the radius of the beam focal spot. At the lowest energies of primary electrons, the total SEE yield is usually less then unity. Therefore, one should consider the maximal charging current $I_s \approx I_p$. Assuming $\varepsilon \sim 2$, $d = 0.3$ mm, $I_p = 50$ nA, and $r = 0.5$ mm, the surface voltage should reach $\varphi_s \approx -1$ V in $1 \mu$s. Thus, at $E_p \sim 10$ eV the pulse duration of the primary electron beam is limited at $t < 1 \mu$s by the desired uncertainty of the energy of primary electrons $\leq 10\%$. Oppositely, at total SEE yield higher than 2, which realizes energies of primary electrons of several tens of electron volts or higher, the charge of the surface is correspondingly higher than $+1$ V. However, the surface potential remains less than 5% of the energy of incident electrons, and should be decreased by a proper decrease of the beam current.

One can see that the surface potential can be decreased by the increase of the focal spot radius and by the decrease of the sample thickness. The decrease of $d$ will also lead to the increase of the time constant of the measuring circuit, $RC$, which is required to be higher than the pulse duration, and to decrease the influence of parasitic capacitances.

Our experimental setup is represented schematically in Fig. 1. The primary electron beam was generated by an electron gun ELG-2 produced by Kimball Physics, Inc. The range of electron energies was 6–1000 eV; the maximal beam current was 10 mA. The minimal diameter of the beam focal spot was 1 mm. The duration of the pulse can be set down to 100 ns, which was set by an external 6040 pulse generator produced by Berkley Nucleonics Corp.

Samples were mounted on a sample holder made of boron nitride. The parasitic capacitance between the rear sample electrode and ground was minimized to $<1.5$ pF. The sample holder was attached to the high vacuum sample heater produced by HeatWave Corp. The temperature of the samples was monitored by K-type thermocouple mounted into the sample holder. The sample holder was mounted on a rotating stage, together with a Faraday cup for measurement of the primary current, $I_p$ (see Fig. 1).

The signals from the sample and from the collector were amplified by direct coupled fast amplifiers with the input resistance of 200 kW and the bandwidth limit of 10 MHz. Amplified signals were recorded by the Tektronix digitizing oscilloscope. The total yield of SEE was determined as

$$\sigma = \frac{I_p - I_s}{I_p}.$$  

(6)

The potential of the collector, $U_c$, was chosen in the range of $10–15$ V depending on the saturation condition for each material and $E_p$.

After each shot, the vacuum chamber was opened and the surface of the samples was cleaned by a volatile conduct-
ing solvent with the following heating at 150–200 °C in vacuum of about $10^{-7}$ Torr. This procedure does not provide complete removal of the surface charge, which is accumulated inside the material to the depth of several monolayers. However, repetitive measurements at the same primary energy showed the deviation of the SEE yield less than 5%–10%.

The influence of the thermal surface treatment, the angle of incident electrons, the surface roughness, and the bounded surface charge on the total yield of electron induced SEE should be taken into account, as well. However, all these effects were neglected in the present work. This should imply some discrepancy between the actual measurements and the results of other authors.

IV. RESULTS AND DISCUSSION

The measured curves of the total yield of SEE at energies lower than 100 eV are presented in Fig. 2 for two materials, boron nitride and quartz, together with the results of other authors. One can see that the present measurements of $\sigma(E_p)$ from SiO$_2$ appear in good agreement with the results reported by Dionne. Some difference in SEE yield from boron nitride was observed between our present results and the measurements performed by Bugeat and Koppel and by Dawson, who found for boron nitride $E_t \approx 50$ eV. In our experiments, we used samples made of boron nitride grade HP produced by Saint Gobain Corp.

The obtained results show significant deviation of $\sigma(E_p)$ from the power fit. The curves of $\sigma(E_p)$ for different materials should cross each other at low energies of primary electrons. Moreover, $\sigma(E_p)$ from ceramics may have a local minimum and maximum in the low energy region, as it appears for macor (see Fig. 3).

The origin of the observed behavior of $\sigma(E_p)$ in the low energy region should be in the increasing role of backscattered electrons. Indeed, the total yield of SEE consists of the yield of “true” secondary electrons, $\delta$, and of the coefficient of backscattering, $\rho$:

$$\sigma = \delta + \rho.$$  

Detailed investigations of $\delta$ and $\rho$ components for several dielectric materials were performed by Fridrikhov and Shul’man. They showed that the coefficient of backscattering usually increases with the decrease of $E_p$, while the yield of “true” secondary electrons decreases and reaches zero at energy of about the width of the potential gap between vacuum and the upper level of valent band. Therefore, the superposition of $\delta$ and $\rho$ should have a distinguishable minimum and maximum in the low energy region, which was observed for several oxides. Baral et al. also considered the role of the backscattering electrons in their model of a SPT thruster.

The measured behavior of $\sigma(E_p)$ at low energies of primary electrons suggests a possible deviation from the power fit. In some sense, the linear fit

$$\sigma(E_p) = \sigma_0 + (1 - \sigma_0) \frac{E_p}{E_1},$$

suggested by Morozov also seems relevant. Indeed, for macor at $E_p > 50$ eV both power and linear fits coincide well with the experimental data, as illustrated by Fig. 3. Physical meaning of the linear fit is in nonzero electron backflow at $E_p > 0$, which should be reasonable for backscattering process. Parameters of both types of fits are presented in Table I for our data and data reported by Dionne and by Jolivet and Roussel.

However, at low $E_p$ the behavior of $\sigma(E_p)$ should differ substantially from both types of fits. Moreover, the actual values of $\sigma(E_p)$ should obviously vary with surface conditions. Indeed, primary particles with energies of a few elec-
tron volts could involve in interaction only thin surface layer, which can have different roughness, can contain impurities and absorbed gases, can be contaminated, etc. The electron backscattering process is sensitive to these factors. The surface temperature should change $\sigma(E_p)$ in the low energy range, as well. Thus, the actual slope of $\sigma(E_p)$ in the low energy region for each particular wall material and operating conditions should also differ from our present results, and would be better measured experimentally.

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