Enhancement to Fusion Reactivity in Sheared Flows

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Sheared flow increases the reactivity of fusion plasma. In unmagnetized plasma with flow gradients comparable to the mean free path of reacting ions, fusion reactivity can be more than doubled. The effect is of particular relevance to inertial confinement fusion (ICF), where it allows implosion kinetic energy to contribute to the fusion burn even before thermalizing. Because colder fuel stops alpha particles more quickly, ignition is possible in a smaller volume, substantially reducing energy requirements in fast-ignition designs.

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Introduction—An axiom or belief in inertial confinement fusion (ICF) is that imploding plasma must thermalize to achieve high fusion reactivity [1,2]. The alternative would have the implosion energy directed into rapidly swirling turbulent eddies of lower temperature. But, since fusion depends only on the relative motion of colliding ions, any turbulent energy is useless: in the local fluid frame of reference, only temperature produces relative motion of the reactants [3,4]. Hence, thermalization is axiomatically crucial. This work overturns that belief. Some energy in turbulent eddies, rather than temperature, can in fact produce higher fusion reactivity.

This shear flow reactivity enhancement effect occurs because relatively few suprathermal ions, with mean free paths many times longer than those of thermal ions, govern fusion reactivity. Even when a hydrodynamic description is appropriate for thermal particles, the tail of the distribution often demands a kinetic treatment. In such cases, fusion reactivity $\langle \sigma v \rangle$ becomes a nonlocal functional of fluid properties within a few fast-ion mean free paths [5–7].

Surprisingly, the effect of inhomogeneous flow on reactivity has so far not been considered. In this Letter, we show for the first time that sheared flow directly enhances fusion reactivity and that this enhancement can be large. Inhomogeneous flow can, of course, modify reactivity by compressing and heating patches of fluid, but, remarkably, even solenoidal flow enhances reactivity through the nonlocal effect of fast ions. Furthermore, exchanging thermal for turbulent energy allows fuel to ignite at lower temperature; leveraging this fact in fastignition (FI) designs allows ignitor energy to be reduced by more than half. The reactivity enhancement is even larger for "advanced fuels," such as D³He and p¹¹B, potentially enabling ICF using these aneutronic reactions.

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Physical picture—The effect can be understood simply in physical terms as follows. Consider, as sketched in Fig. 1, a fluid flowing in the x direction and sheared in the z direction. The distribution function at each point is approximately a drifting Maxwellian. A particle sampled from the thermal bulk at z_1 ends up closer to the tail if it reaches z_0 without colliding. For a thermal particle sampled at z_2 , the effect is more pronounced. Some particles will have smaller velocities in their new frame, but the overall effect is to broaden the tail. Neglecting slowing by electrons, the mean free path λ for fast ions scales as $\lambda \propto w^4$, where w is the velocity in the local fluid frame, so faster ions communicate further across flow gradients. Thermal ions travel a relatively short distance λ_{th} between collisions; the dynamics of these ions give rise to viscosity. Fast particles, however, travel beyond viscous length scales, potentially crossing large flow differentials.

For a gradient length scale L, a useful figure is the Knudsen number $Kn \doteq \lambda_{th}/L$. For Maxwellian ions, the reaction rate is peaked at $v_* \propto v_{\rm th} (E_G/T)^{1/6}$, where the Gamow energy E_G gives the energy scale of the

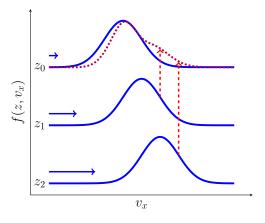


FIG. 1. Fast particles crossing a flow gradient perturb the distribution, particularly on the tail.

Coulomb barrier, T is the temperature (in units of energy), and $v_{\rm th}$ is the thermal velocity. In many cases, $v_*\gg v_{\rm th}$. Because most reacting particles have velocities near v_* , the "Gamow mean free path" λ_* is much longer than $\lambda_{\rm th}$. The "Gamow-Knudsen" number ${\rm Gk} \doteq \lambda_*/L = (v_*/v_{\rm th})^4{\rm Kn}$ of McDevitt *et al.* thus better captures the effect of gradients on reactivity [5,8].

Ions crossing a flow gradient attain some drift velocity in their new frame; we show here that even a small drift has a large effect on reactivity. Consider a one-dimensional Maxwellian distribution of ions with thermal velocity $v_{\rm th}$ reacting with some stationary background species. Suppose that the fusion power P is proportional to the number of particles at $v=v_*$ and that v_* is constant (this is a reasonable estimate for strongly resonant reactions, while for others it is merely illustrative), so in equilibrium $P^{(\rm eq)} \propto \exp\{-\frac{1}{2} v_*^2/v_{\rm th}^2\}$. Suppose that we impart to the ions a drift velocity $u \ll v_{\rm th} \sqrt{v_{\rm th}/v_*}$. The fusion power is now approximately $P^{(\rm drift)} \propto \exp(-\frac{1}{2} v_*^2/v_{\rm th}^2 + v_* u/v_{\rm th}^2)$. The drift energy could instead have been used for heating. If the drifting ions are one quarter of total particles, heating produces a new thermal velocity $v_{\rm th}'$ such that $v_{\rm th}'^2 = v_{\rm th}^2 + \frac{1}{4} u^2$, yielding fusion power $P^{(\rm heat)} \propto \exp(-\frac{1}{2} v_*^2/v_{\rm th}^2 + \frac{1}{8} v_*^2 u^2/v_{\rm th}^4)$. Denoting by Φ the enhancement factor relative to $P^{(\rm eq)}$, we have

$$\Phi^{\text{(drift)}} \sim e^{\gamma}, \qquad \Phi^{\text{(heat)}} \sim e^{\gamma^2/8}, \qquad (1)$$

where $\gamma \doteq v_* u / v_{\rm th}^2$ is the single parameter governing the size of the effect. For $\gamma \gtrsim 1$, fusion power is multiplied manyfold even though u is small. For $\gamma < 8$, energy is better spent on drift than on heating. This is the principle by which beam-target fusion offers a high reaction rate [9,10] but with low efficiency since most beam ions scatter before fusing. Anisotropic or counterstreaming Maxwellians likewise increase reaction rates [11–14], but energy must be expended to keep such distributions out of equilibrium, which is unsuitable for a fusion reactor [15]. The shear flow reactivity enhancement is fundamentally different because populations are separated in space. The increase in mean free path with velocity leads to a drifting population of fast ions while the colder thermal bulk is more collisional and therefore relatively inviscid, leading to slow dissipation. This effect is peculiar to plasma, rather than other fluids, because in plasma faster particles have longer mean free paths.

Kinetic model—To isolate the effect of flow shear, we consider uniform, planar x-directed flows separated by a transition layer of width L at z=0. Away from this layer, the flow field \boldsymbol{u} is given by

$$\mathbf{u}(z) = \begin{cases} u_0 \hat{\mathbf{x}} & z \ll L \\ 0 & z \gg L \end{cases}$$
 (2)

where u_0 is a constant. We first consider regimes in which

$$Kn \ll 1 \ll Gk$$
, (3)

permitting a hydrodynamic description: thermal particles, which are responsible for the majority of viscous dissipation, have short mean free paths. On the other hand, particles near the Gamow peak travel far beyond the layer before scattering. If we are exclusively interested in the transport of energetic particles, we can treat the layer as a point discontinuity. In the numerical work below, we will relax this assumption to consider systems in which the scale separation (3) is not so large.

For simplicity, we consider a single ion species with mass m, uniform density n, and uniform temperature T. Electrons form a neutralizing background. The distribution function f evolves according to

$$\frac{\partial f}{\partial t} + \boldsymbol{v} \cdot \nabla f + \boldsymbol{a} \cdot \frac{\partial f}{\partial \boldsymbol{v}} = \mathcal{C}[f, f], \tag{4}$$

where v is the velocity in the laboratory frame, a is the net acceleration, and C is a bilinear collision operator.

Let $\mathbf{w} \doteq \mathbf{v} - \mathbf{u}$ be the peculiar velocity and $v_{\rm th} \doteq (T/m)^{1/2}$ be the thermal velocity. By (3), the bulk of the distribution is approximately a Maxwellian f_M , while the tail may deviate significantly. We approximate collisions as occurring between test particles and a thermal background, adopting a Bhatnagar-Gross-Krook (BGK) operator, viz. $\mathcal{C} = -\nu_{\rm ii}(f-f_M)$, where $\nu_{\rm ii} = \nu_0$ for $w \leq v_{\rm th}$, $\nu_{\rm ii} = \nu_0(v_{\rm th}/w)^3$ for $w > v_{\rm th}$, and ν_0 is a constant. We finally assume steady state $(\partial_t f = 0)$ and that all spatial variation is in the z direction. Treating the shear layer as a step function, the solution is

$$f(z > 0) \sim \begin{cases} \frac{\hat{f}}{(2\pi)^{3/2} v_{\text{th}}^3} \left[e^{-\frac{z v_{\text{ii}}}{w}} \exp\left\{ -\frac{|\mathbf{w} - u_0 \hat{\mathbf{x}}|^2}{2v_{\text{th}}^2} \right\} + \left(1 - e^{-\frac{z v_{\text{ii}}}{w}} \right) \exp\left\{ -\frac{|\mathbf{w}|^2}{2v_{\text{th}}^2} \right\} \right] & w_z > 0, \\ \frac{1}{(2\pi)^{3/2} v_{\text{th}}^3} \exp\left\{ -\frac{|\mathbf{w}|^2}{2v_{\text{th}}^2} \right\} & w_z \leq 0, \end{cases}$$
(5)

where \hat{f} is a normalization factor to conserve density. The distribution for z < 0 is obtained by reversing signs.

Fusion reactivity—For a single species, reactivity is

$$\langle \sigma v \rangle = \frac{1}{2} v_{\rm th} \iint d^3 w d^3 w' \sqrt{2} p \sigma(p) f(\mathbf{w}) f(\mathbf{w}'), \quad (6)$$

where σ is the fusion cross section and $p = (w - w')/\sqrt{2}v_{\text{th}}$ is the normalized relative velocity. Assuming a constant S factor and no resonances, σ can be approximated by

$$\sigma(p) = \frac{A}{v_{\rm th}^2 p^2} e^{-b/p},\tag{7}$$

where A and b are constants (note $b \propto v_{\rm th}^{-1}$). Physically, b represents the height of the Coulomb barrier relative to the thermal energy ($b^2 \propto E_G/T$). In general, fusion reactions are classically forbidden and require quantum tunneling; in other words, b is large. For DD reactions at 3 keV, for example, $b \approx 26$ [16]. When $b \gg 1$, the integrand is sharply peaked, allowing (6) to be evaluated by steepest descent. To leading order in b, we define the enhancement factor Φ based on

$$\langle \sigma v \rangle \sim \left(\sqrt{\frac{2}{3}} \frac{Ab^{1/3}}{v_{\rm th}} e^{-\frac{3}{2}b^{2/3}}\right) \Phi$$
 (8)

so that $\Phi=1$ for Maxwellian distributions. Starting from (5) and making the approximation that every excess (nonthermal) fusion reaction occurs between a particle from the perturbed distribution, i.e., the first line of (5), and a particle from a Maxwellian, we have

$$\Phi \sim \frac{1}{2} + \frac{\iint \frac{d^3 p d^3 s}{(2\pi)^3} \frac{e^{-b/p}}{p} e^{-\frac{1}{2}|s - \frac{1}{2}\hat{u}\hat{x}|^2} e^{-\frac{1}{2}p^2 + \frac{1}{2}\hat{u}p_x - \frac{1}{8}\hat{u}^2}}{2 \iint \frac{d^3 p d^3 s}{(2\pi)^3} \frac{e^{-b/p}}{p} e^{-\frac{1}{2}s^2} e^{-\frac{1}{2}p^2}}, \quad (9)$$

where $s \doteq (\mathbf{w} + \mathbf{w}')/\sqrt{2}v_{\text{th}}$ and $\hat{u} \doteq \sqrt{2}u_0/v_{\text{th}}$. Assuming $\hat{u} \lesssim 1$, evaluating (9) to leading order in b yields

$$\Phi \sim \frac{1}{2} + \frac{e^{-\frac{1}{12}\hat{u}^2}\sinh(\frac{1}{2}\hat{u}b^{1/3})}{\hat{u}b^{1/3}}.$$
 (10)

By (8), $\langle \sigma v \rangle$ is a strongly decreasing function of b (so an increasing function of temperature) in reactor-relevant regimes. However, by (10), Φ is an increasing function of b. Therefore, while fusion reactivity is largest at high temperature, the fractional enhancement is largest at low temperature. Additionally, the flow speed u_0 corresponding to a fixed \hat{u} is smaller at low temperature. For these reasons, a promising application of strongly sheared flow is to "jump-start" a fusion burn in warm fuel. Because b increases with the charge of the reacting species, the enhancement is larger for "advanced fuels" such as D^3 He and p^{11} B. In plasma containing high-Z elements, whether from nonhydrogen fuels, impurities, or alpha particles, the relative value of shear flow compared to heating is greater because additional

electrons increase heat capacity, but do not significantly increase flow kinetic energy.

Numerical results—To improve on the analytical estimate in (10), we solved (4) numerically in steady state using a BGK operator with collision frequency $\nu=\nu_{\rm ii}+\nu_{\rm ie}$. The ion-ion collision frequency $\nu_{\rm ii}$ was given by the same model as above, and the ion-electron collision frequency was a constant $\nu_{\rm ie}=\nu_0\sqrt{m_e/\bar{m}}$, where m_e,m_D , and m_T are the electron, deuterium, and tritium masses, respectively, and $\bar{m}\doteq(m_D+m_T)/2$. An equimolar DT plasma was assumed, and velocities were normalized to $\bar{\nu}_{th}\doteq\sqrt{T/\bar{m}}$. The background was a Maxwellian with uniform temperature and with stationary flow profile

$$\boldsymbol{u}(z) = \frac{u_0}{2} \left(1 - \tanh\left(\frac{z}{L}\right) \right) \hat{\boldsymbol{x}}$$
 (11)

for constant flow velocity u_0 and gradient length scale L. Viewed in the $z-w_x$ plane [Fig. 2(a)], the perturbation to f appears as "wings" near z=0, where particles arriving from the other side of the shear layer have not yet caught up to the local flow velocity. This phenomenon affects all particles, but it persists over a much longer distance for fast particles. In the w_x-w_z plane [Fig. 2(b)], the perturbation appears as a lobe of higher phase-space density at $w_x, w_z > 0$; this fast-ion population is responsible for the reactivity enhancement.

From these distributions, reactivity was calculated using the cross-section formulas of Bosch & Hale [16] for the $D(d,n)^3 He$ and $T(d,n)^4 He$ reactions (Fig. 3). The enhancements $(\Phi_{DD}$ and $\Phi_{DT},$ respectively) peak just outside the transition layer but actually dip within the layer because the

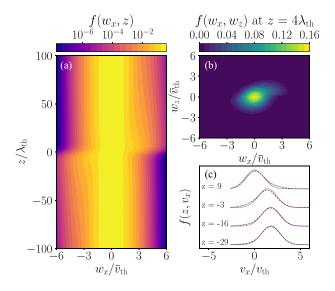


FIG. 2. Distribution function for a $u_0 = 2v_{\rm th}, L = 5\lambda_{\rm th}$ layer: (a) $f(z,w_x)$ showing a jump in peculiar velocity near z=0, (b) $f(w_x,w_z)$ showing the anisotropic distribution of fast particles, (c) $f(z,v_x)$ (purple, dotted) compared to $f_M(z,v_x)$ (gray); cf. Fig. 1.

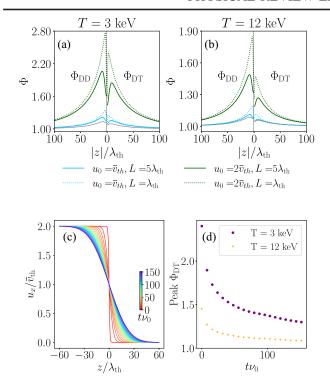


FIG. 3. Top: reactivity enhancement at (a) $T=3~{\rm keV}$ and (b) $T=12~{\rm keV}$. The left half of each panel shows $\Phi_{\rm DD}$ and the right shows $\Phi_{\rm DT}$. Bottom: (c) viscous relaxation of a shear layer beginning with $u_0=2v_{\rm th}$ and $L=\lambda_{\rm th}$; and (d) peak $\Phi_{\rm DT}$ at each time step.

maximum difference in flow velocity is not as large there as in the outer regions. As anticipated by (10), the enhancement factor is larger at low temperature [17]. For one set of conditions, Φ_{DT} reaches 2.4 at its peak, a dramatic increase in fusion rate over a region tens of λ_{th} in width. For equivalent conditions, Φ_{DD} is larger than Φ_{DT} due to a leveling off of the DT cross section at high energy. This is consistent with experiments finding a lower than expected DT:DD yield ratio [18]. The reactivity enhancement is an inherently kinetic effect. To illustrate this, moments of f were computed at each z location for one flow profile $(u_0 = \bar{v}_{th}, L = 5\lambda_{th})$, and Maxwellians were generated with the same moments. Reactivities for these Maxwellians are shown in gray in Fig. 3, demonstrating that the enhancement, in fact, occurs not simply because more energetic ions cross the shear layer, but because the ions furthest out on the tail are the most affected due to their long mean

The flow profile described by (11) is subject to rapid viscous dissipation when $L \sim \lambda_{\rm th}$. To assess the effect of viscosity on reactivity, we performed kinetic simulations in Gkeyll [19] using as initial conditions (11) with $u_0 = 2v_{\rm th}$ and $L = \lambda_{\rm th}$. Figure 3 shows the flow profile at later times (c) and the height of the peak of the $\Phi_{\rm DT}$ profile at each time (d). Reactivity drops quickly at first but begins to level off at later times; $(\Phi_{\rm DT} - 1)$ drops to about one sixth of its original value in 150 collision times. For the parameters

discussed below, this is about 30 ps, meaning that the enhancement is significant for a sizable fraction of the burn duration [20].

Shear flow in ICF—As seen in Fig. 3(d), viscosity is important but does not preclude large effects. In magnetic compression, it has been well established that flow kinetic energy can greatly exceed thermal energy [21–23]; in fact, observations of highly turbulent flows at peak compression in z-pinch experiments [22,24,25] inspired the consideration of strongly sheared flows in this work. In laser-driven compression, too, flow kinetic energy can rival or exceed thermal energy [26–29]. A conservative estimate of the size of the effect can be made from past experiments on the National Ignition Facility (NIF). The numerical methods described above, applied to simulations of NIF experiment N120321 [27,29], yield a hot-spot averaged reactivity enhancement of approximately 4%. That this is a modest effect is not surprising; NIF targets are carefully designed to minimize turbulence. Nevertheless, even modest changes in reactivity are significant in systems near ignition. Substantially larger enhancements can be contemplated if turbulence is driven deliberately. Although viscosity dissipates fine-scale turbulent kinetic energy (TKE) during compression, instabilities provide sudden driving at late times; fine-scale TKE has actually been observed to increase near stagnation [26,30]. In the hot spot at bang time, viscous and inviscid simulations show similar levels of TKE [26,29], so viscosity is not playing the dominant role in quenching turbulence during burn, consistent with Fig. 3. It follows that larger TKE could be driven at fine scales, perhaps by seeding Rayleigh-Taylor unstable perturbations [30–33] or using structured materials [34–37]. Simulations of deuterated-foam targets exhibit a kinetic reactivity enhancement (and then suppression) as voids collapse [38]; while largely attributable to colliding flows and the Knudsen-layer reactivity reduction [5,38], these results indicate that structured targets can access regimes relevant to the effect presented in this Letter. Further technical details relevant to driving TKE are given in the End Matter.

Reduction in ignition energy—A corollary to the shear flow reactivity enhancement effect (which we will show to have large implications) is that turbulent plasma may ignite at lower temperature, suggesting the question, what partition between thermal energy and turbulent kinetic energy is optimal for fusion? The practical question is whether an ICF design can be improved by intentionally driving turbulent flows.

The following case suggests that substantial energy savings are, in fact, possible. To see this, consider a 8 keV DT plasma with TKE in micron-scale eddies driven to a level of 90% of the ion thermal energy. The numerical methods used above (described in detail in the End Matter) give $\Phi \approx 2.7$, which, remarkably, is comparable to the enhancement if the TKE were instead thermalized.

But keeping the TKE unthermalized allows a smaller hot spot because alpha-particle stopping distance scales as $T^{3/2}$ [39–41]. In FI, where an ignitor pulse rapidly heats a region of precompressed fuel to initiate fusion, this means that the ignitor can heat a smaller fuel mass to a lower temperature. Reducing ignition temperature by a factor of τ yields a $\tau^{11/2}$ reduction in ignitor energy [42]. Now the key result is that if, for example, enough TKE is driven to permit ignition at 8 keV rather than at 12 keV, then the required ignitor energy is reduced by a factor of 9.7. Thus, an order-of-magnitude reduction in ignition energy might be achieved in fast ignition.

Moreover, the cold, dense fuel is relatively inviscid until the ignitor pulse heats the hot spot. Viscosity increases as $T^{5/2}$, but turbulent eddies need only persist for a fraction of the burn time (tens of ps) to facilitate ignition; Figure 3(d) shows that this is reasonable. For this example, assuming a density $\rho = 300 \text{ g/cm}^3$, the Gamow mean free path is $\lambda_* \approx 0.8 \ \mu\text{m}$; for eddies on this scale, the viscous dissipation time is about 70 ps at 8 keV but about 12 ns at 1 keV, easily long enough to survive compression. Including TKE as well as the ignitor energy, the energy requirement is reduced by a factor of about 6.4.

Despite simplifications, this model demonstrates from first principles that very large energy savings are possible. While localizing TKE and heating in small hot spots comes with its own challenges [43,44], this calculation is broadly a conservative one, ignoring several loss mechanisms that scale favorably with decreasing temperature. For instance, the final steps of ion heating are the longest and least efficient [45], while the lower temperature reduces radiative losses [46–48]. Many of these favorable scalings apply to conventional ICF schemes as well.

Discussion—Why has the shear flow reactivity enhancement effect put forth here not already been noted in simulations? The answer lies, at least in part, in its multidimensional nature, involving at least one spatial dimension and two velocity dimensions (see Fig. 2), as well as a velocity-dependent collision frequency. Simplifications common in kinetic simulations, such as one-dimensional velocity space, spherical symmetry, and constant collision frequency, obscure these features [7,49–53]. Nonetheless, this is a fundamental effect relevant to a variety of ICF systems with likely analogues in magnetically confined and astrophysical plasmas.

To date, ICF designs have sought to minimize TKE at bang time on the assumption that turbulence harbors no advantages. This Letter shows that assumption to be false. Remarkably, the sheared flows present in turbulent eddies contribute directly to fusion reactivity. The question of optimal partition between turbulent and thermal energy in fusion plasmas is a rich one, offering, beyond its intrinsic theoretical appeal, the prospect of novel ICF designs. In this Letter, we identified cases where the shear flow reactivity enhancement can be large in practical DT

implosions. Of even greater importance, we showed that because ignition then occurs at lower temperature, alpha particles are stopped more promptly, leading to a smaller hot spot and lower ignition energy.

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End Matter

End Matter—This Letter introduced the shear flow reactivity enhancement effect in the case of simple planar shear layers to highlight the key physics at play. It is straightforward, however, to generalize the analysis to more complex flows. This End Matter describes such

a generalization; it is organized as follows. First, we provide supplemental details on the calculation of the reactivity enhancement reported in the main text for NIF experiment N120321. Second, we show that the scalings derived in the main text readily lead to a simple

approximation scheme for the reactivity enhancement in turbulent flows. Finally, we offer an example of how these results might be used in the design of an experiment to test the theory.

A fill-tube jet is thought to produce only detrimental effects, introducing impurities and quenching the hot spot. However, simulations and experimental data on these jets are able to inform, at least partially, on the flows present in ICF implosions. For a fill-tube jet entering a hot spot, a simple estimate can be made by considering a planar shear layer with velocity equal to the jet velocity and a length scale comparable to the size of the shearing region between the jet and background fuel. We make such an estimate based on high-resolution viscous simulations [27,29] of NIF experiment N120321. In a region near the fill-tube iet with ion density $n \approx 10^{25} \text{ cm}^{-3}$ and temperature $T \approx$ 2.5 keV (cf. Fig. 9 of [29] and Fig. 7 of [27]), the simulations indicate $u \approx 1.6\bar{v}_{th}$ and $L \approx 20\lambda_{th}$. DT reactivity is enhanced by \sim 22% in a region about 5 μm in width $(\Phi_{\rm DT} \approx 1.22)$, while $\Phi_{\rm DD} \approx 1.29$). Taking the hot spot radius to be $R \approx 40 \ \mu m$ and estimating the total area of the shear layers to be half of the hot spot surface area (although folded deep within the hot spot), the volume-averaged DT reactivity enhancement is a more modest 4%. In some cases, such as for the initiation of a fusion burn, the local (22%) enhancement is more relevant.

While large-scale coherent structures, such as jets, are useful for calculation, random turbulent flows represent a more general case. Moreover, small-scale turbulent motions are preferable in fusion experiments because they are less prone than jets to introduce impurities into the hot spot. We describe here an approximation scheme generalizing the reactivity calculations in the main text to turbulent flow fields. Guided by (10), a simple estimate of the reactivity enhancement for a profile of length scale L and normalized flow speed \hat{u} is

$$\Phi \sim 1 + C_L b^{2/3} \hat{u}^2,$$
 (A1)

where C_L is an unknown factor depending on L. We define a "Gamow wave number"

$$k_* \doteq \frac{\nu_0}{v_*} \left(\frac{v_{\text{th}}}{v_*}\right)^3 \tag{A2}$$

such that sinusoidal flow structures on the scale of k_* have a width comparable to the mean free path of particles at the Gamow peak.

The flow can be broken down into many modes, each with a wavenumber k. These modes are described by an energy spectrum $\varepsilon(k)$. Let us assume that the spectral region around k_* can be characterized by a turbulent cascade with power-law form $\varepsilon(k) \propto k^{-\alpha}$. Although viscosity in ICF hot spots is known to inhibit the development of a true inertial range in many cases [26], simulations

suggest a turbulent cascade at some scales near bang time [30,54]. All modes contribute to the reactivity, with larger enhancements coming from higher wavenumbers until this trend is arrested by the decreasing energy per mode (note that this model is supported by more detailed kinetic calculations [55]). We therefore estimate Φ using the energy in the $k = k_*$ mode, viz.

$$\Phi \sim 1 + C_* b^{2/3} \frac{k_* \varepsilon(k_*)}{(\alpha - 1)E_{th}},$$
 (A3)

where $E_{\rm th}$ is the ion thermal energy, C_* is a constant related to C_L and found numerically, and the factor of $k_*/(\alpha-1)$ estimates the contribution from integrating over all higher-k modes. This underestimates the increase in Φ at $k>k_*$ as well as the fact that $k< k_*$ modes contribute a nonzero amount to Φ , but integrating over these would require a complicated cutoff procedure at viscous scales; (A3) remains a practical, and likely conservative, estimate. Using the method described in the main text, we simulated a shear flow with profile $u(z)=v_{\rm th}\hat{x}\sin(\pi k_*z)$ in an equimolar DT 3 keV plasma; taking a spatial average of the resulting DT reactivity yields the estimate $C_*\approx 0.08$ (for DD, $C_*\approx 0.10$).

To illustrate the implications of these formulas, we provide two quantitative examples beyond those in the main text. At conditions relevant to the onset of burn (7 keV and 100 g/cm³) [20], with small-scale TKE around 25% of the ion thermal energy, reactivity is enhanced by about 24% throughout the hot spot. Here, it is assumed that eddies are on the scale of 2–4 μ m; the viscous dissipation time τ at this scale is ~200 ps, estimated by $\tau \approx L^2/\eta$, where L is the eddy size and η is the kinematic viscosity. For a turbulent z-pinch plasma at 4 g/cm³ and 10 keV, with TKE four times the ion thermal energy and contained in large-scale (~1 mm) eddies with a Kolmogorov cascade to smaller scales ($\lambda_* \approx 33 \,\mu\text{m}$), reactivity is more than doubled $(\Phi \approx 2.3)$. To realize these enhancements, the implosion must be designed to drive TKE into the scales assumed here, rather than into the deleterious large scales; some promising techniques to accomplish this are described below in the context of a proposed experiment.

The accuracy of (A3) was evaluated using simulations based on N120321 [27,29] involving a prominent fill-tube jet. We used kinetic-energy spectra spectra [27], which are agnostic of jet structure, along with (A3) to estimate the reactivity enhancement ($u^2 \approx 3 \times 10^3 \ \mu m^2/ns^2$ at $\lambda_* \approx 1.2 \ \mu m$). The result of approximately 5% was in good agreement with the estimate based on a planar shear layer. Percent-level effects are difficult to discern among the numerous experimental uncertainties, so it is unsurprising that the shear flow reactivity enhancement effect has not previously been noted in data from ICF experiments. However, these estimates help to inform a possible experimental test of the theory.

The conjecture emerging from this work is that, if smallscale TKE can be isolated from the loss mechanisms that typically accompany its generation, a previously obscured positive effect will appear. To test this conjecture, we describe a proof-of-principle experiment based on the FI scheme described in the main text. As in FI and shockignition (SI) [39,56], the design contemplates a slow implosion and a large shell mass, giving good hydrodynamic stability and, therefore, low TKE. In sharp contrast to FI and SI, however, we add perturbations on the inner surface of the DT shell large enough to drive TKE (in spite of the improved stability) [33,54,57]. Low fuel temperature gives a relatively slow dissipation time for these driven eddies, and a thick shell reduces the injection of ablator material into the hot spot by the perturbations. To establish a trend, we envision imploding a range of targets with perturbations of varying sizes, including a baseline case without deliberate perturbations.

At the end of the laser drive, a sharp spike in power launches a shock timed to reach the hot spot near peak compression, rapidly heating the fuel [56,58]. This design employs a shock, rather than fast particles generated by a laser pulse, for better compatibility with current NIF infrastructure. Because a large fraction of the hot-spot thermal energy is due to the final shock heating, the burn temperature is (partially) decoupled from the dynamics of compression; this is important in order to compare multiple implosions, where different perturbations entail different temperatures during compression. The assembly need not ignite when the shock arrives; in fact, low yield is preferable to avoid complications from self-heating and burn propagation. A trend linking increased fusion yield to TKE, beyond being highly counterintuitive, would be a strong signature of the shear flow reactivity enhancement effect. Moreover, this scheme obviates the need to predict yield with high accuracy; rather than seeking a discrepancy between theory and experiment, it sufficies to establish a trend among several implosions subjected to a range of perturbations.

This experimental design is distinctive in requiring the driving of TKE, whereas ICF designs generally seek the opposite. While optimizing this driving constitutes an interesting hydrodynamics problem, doing it at a basic level is straightforward. At minimum, it is possible to simply replicate N120321 [27,29], generating the flows considered above and yielding a roughly 5% enhancement at T=2.5 keV. Suppose that this replicated N120321 is shocked to T=6 keV on a short enough time scale that the TKE spectrum remains initially unchanged (the collision time is \sim 3 ps for ions at the Gamow peak, so the fuel has

time to equilibrate after the shock). The Gamow mean free path after heating is $\lambda_* \approx 3.9~\mu m$. Approximating the TKE spectrum by a k^{-2} power law [27] and neglecting compression by the final shock, the reactivity enhancement roughly doubles to ~10%. It is not proposed to recycle the N120321 design, but this calculation illustrates that generating TKE of the required magnitude and on the required scales is well within NIF capabilities. Building on these capabilities, the additional design features outlined above help to suppress competing effects so as to isolate the shear flow reactivity enhancement under better-controlled conditions.

Additional control can be achieved by varying pulse shapes and by mixing small amounts of inert high-Z gas to modify the viscosity and reduce the implosion temperature, although we do not anticipate this to be necessary for an initial proof-of-principle experiment. Structured materials offer a flexible TKE-driving method to complement the shell perturbations described above. Theoretical work shows turbulence to be an intrinsic feature of shock propagation in materials of nonuniform density and suggests schemes for controlling turbulent spectra by modifying material composition and geometry [34]. Experiments with deuterated foams, namely on the MARBLE platform [35-37,59], have demonstrated a relationship between pore size and turbulent mixing, thereby indirectly validating the capability to control turbulence using target structure. As mentioned in the main text, PIC simulations of collapsing pores in MARBLE experiments have shown kinetic reactivity enhancements (and suppression) [38]. These enhancements might be accentuated by modifications to the target structure and implosion profile based on the results of this Letter.

What we have described here is a fundamental-science experiment to demonstrate the effect predicted in this Letter. While improved experiments may be developed, this design serves as a concrete example of a viable path to isolating the effect of TKE on fusion yield. Demonstrating the fundamental effect would set the stage for a full-scale demonstration that small-scale TKE can be beneficial in igniting ICF plasmas. The fast ignition scheme described in the main text would easily provide this demonstration. Recent work, in fact, supports the feasibility of such a scheme; a modified ignition criterion for ICF plasma with reactivity enhanced by turbulence [60] shows that, even in conventional central hot-spot ignition, small-scale turbulence could allow plasma to ignite at lower levels of confined energy (thermal plus TKE) than would otherwise be possible.