

Lyman Spitzer's Legacy of Innovation in the Quest for Fusion Energy

Greg Hammett, May 4, 2024
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Princeton Plasma Physics Laboratory (PPPL)
& Princeton University Ph.D. Program in Plasma Physics

Science on Saturday Lecture / Fusion Energy Week

Lyman Spitzer's Legacy of Innovation in the Quest for Fusion Energy

- An informal history of early PPPL fusion research
- Some history of Spitzer's big ideas / innovations:
 - 1946: Telescopes in space (Hubble Space Telescope)
 - 1951: Figure-8 stellarator trick to make a fusion power source
- A fluid picture of the trick for how a figure-8 stellarator works (and basis for later stellarators).
- Continuing innovations at PPPL and elsewhere to improve fusion energy concepts
 - including ideas for further improving the stellarator concept, which is undergoing a renaissance.

I never officially met Prof. Spitzer, though I saw him at a few seminars, and was friends with his last graduate student. (I was a grad student here 1980-1986.) Heard many stories from Prof. Tom Stix, Prof. Russell Kulsrud, & others, learned from the insights in his book and his ideas in other books.

Lyman Spitzer, Jr.

1914-1997

Born in Toledo, Ohio.

Yale B.S. (1935), Cambridge (1936)
Princeton Ph.D. Physics (1938)

Yale professor
World War 2: worked on sonar

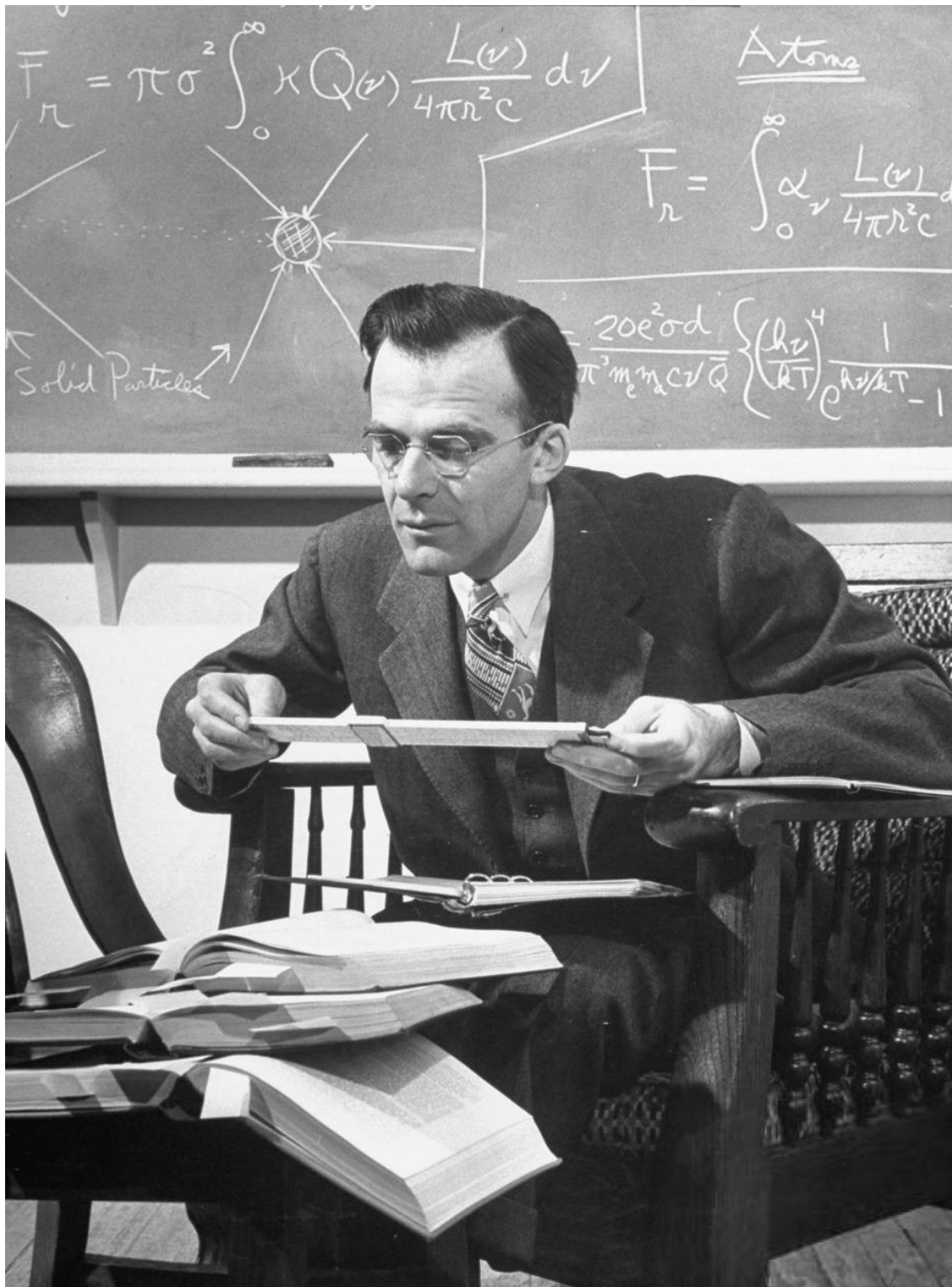
Chair of Princeton Department of
Astrophysical Sciences, 1947-1979



Photo by Orren Jack Turner, from Biographical
Memoirs V. 90 (2009), National Academies Press, by
Jeremiah P. Ostriker.

<http://www.nasonline.org/publications/biographical-memoirs/memoir-pdfs/spitzer-lyman.pdf>

Lyman Spitzer, Jr.



LIFE Magazine, Apr 28, 1948

LIFE Photo Collection, March 1948

http://sliderulemuseum.com/SR_Ephemera.htm

<http://www.google.com/culturalinstitute/asset-viewer/uwHIsK8XRqgCXw?hl=en>
<https://books.google.com/books?id=d0EEAAAAMBAJ&pg=PA98&dq=spitzer&hl=en&sa=X&ved=2ahUKEwjZkZjN5fKFAxVxD1kFHfrCAMsQ6AF6BAgBEAI#v=onepage&q=spitzer&f=false>



• 1960, director of PPPL (1951-1961, and simultaneously, chair of Dept. of Astrophysical Sciences, 1947-1979.)

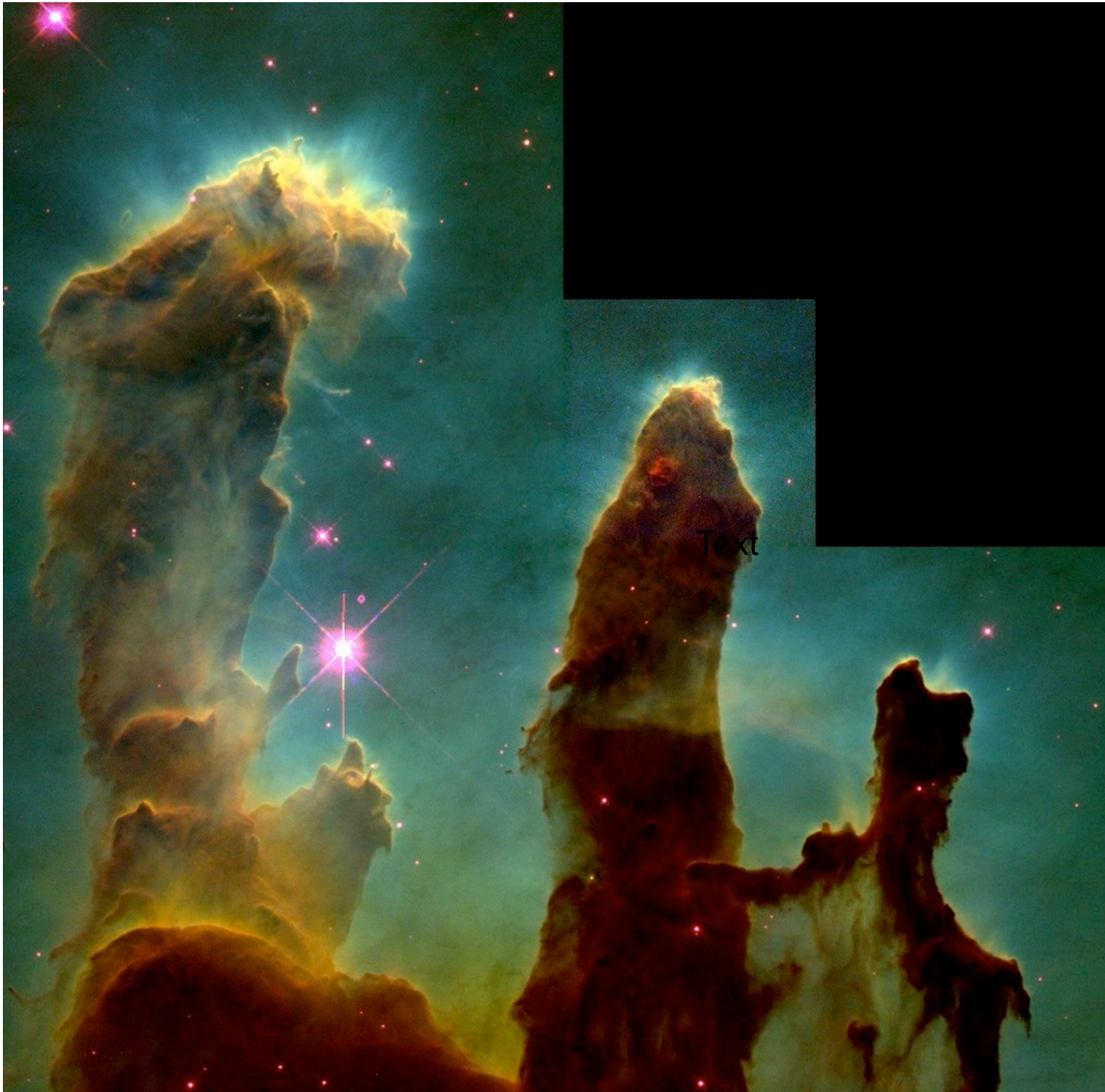
1946: Spitzer Proposes Telescopes in Space

- In 1946, Spitzer wrote a report for the RAND Corporation on “Astronomical Advantages of an Extra-Terrestrial Observatory”
- Spitzer credited with being “a visionary behind the Hubble Space Telescope” [1], documenting the advantages it would have, and seeing that it would be feasible. “While the fundamental concept of sending a large telescope into space wasn’t new, the reality of doing so was.” [1]
- “The most important champion of the project was Lyman Spitzer” [2].
- Hubble Space Telescope launched 1990 (optics fixed in 1993)
(predecessor to the James Webb Telescope)
- NASA infrared space observatory: the Spitzer Space Telescope (2003-2020)

Others had independently proposed a telescope in space, such “as 1923 by the German rocket pioneer Hermann Oberth” [2]

[1] <https://science.nasa.gov/people/lyman-spitzer-making-space-for-hubble>

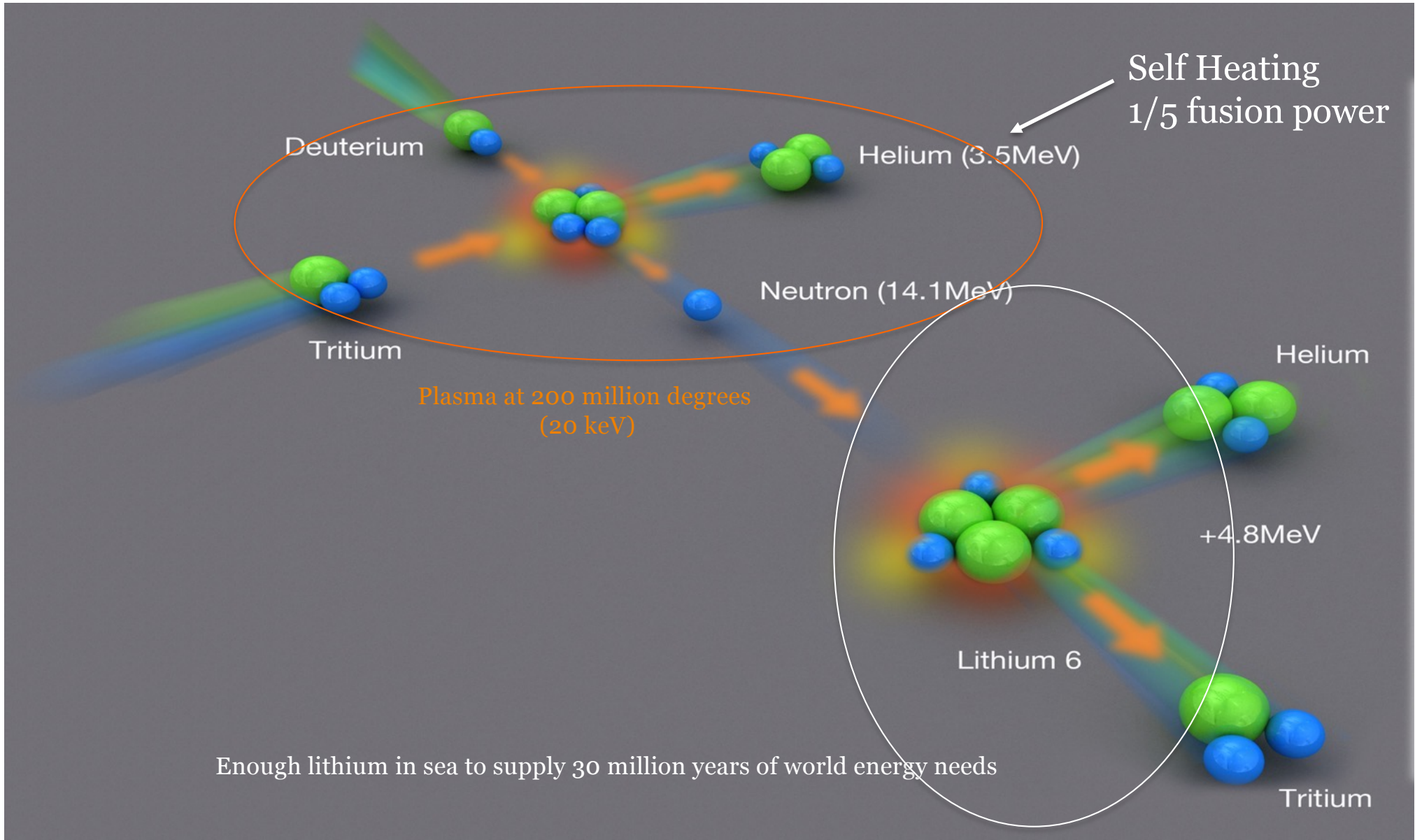
[2] <https://www.amnh.org/learn-teach/curriculum-collections/cosmic-horizons-book/lyman-spitzer-hubble-telescope>



Famous image
from the Hubble
Space Telescope.

The Eagle Nebula:
“Pillars of Creation”
gas pillars in a star-
forming region.

Deuterium and tritium: isotopes of hydrogen that fuse much more easily

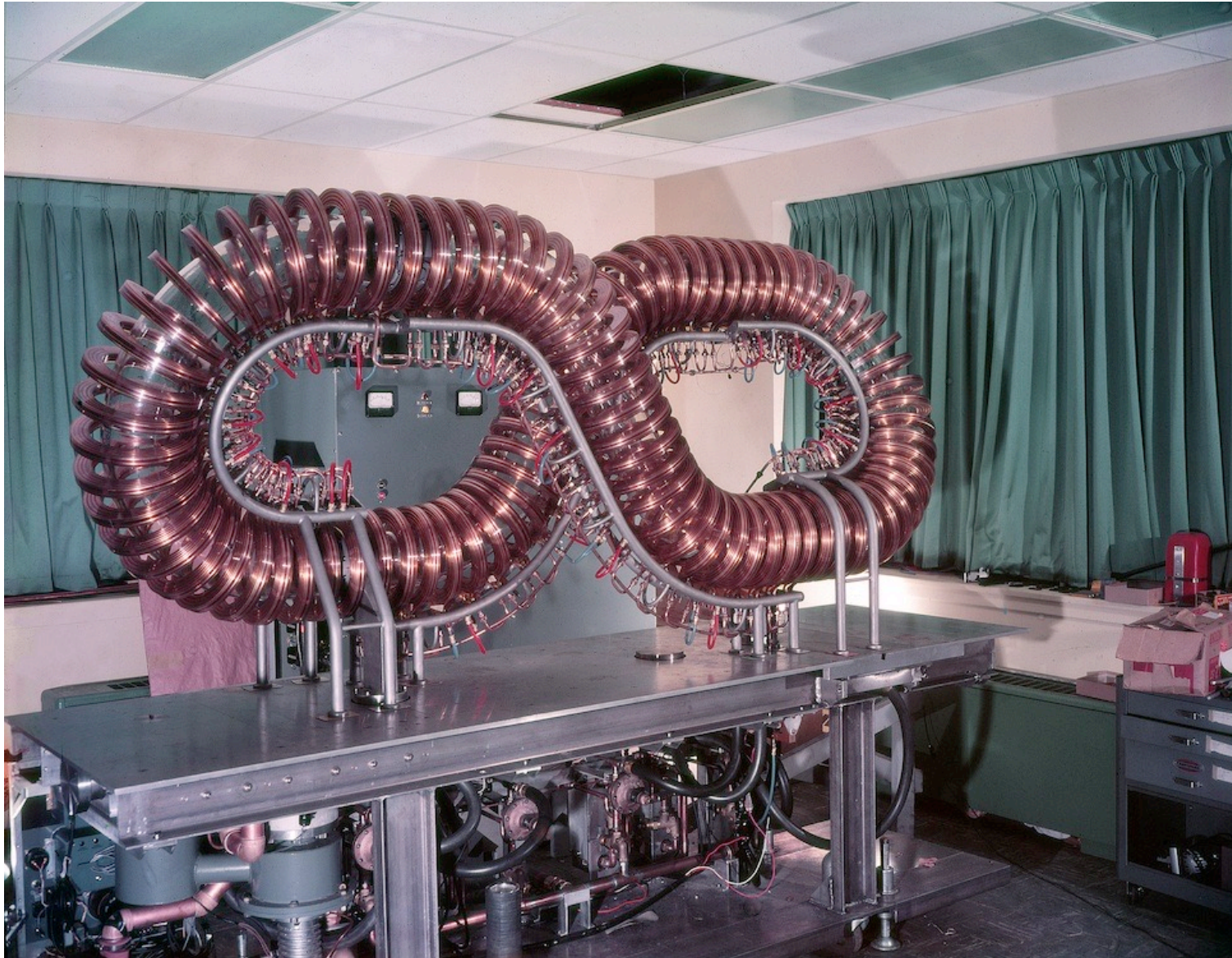


Huge energy gain: 17.6 MeV out / 40 keV in = 440
But need to heat plasma to extreme temperatures

Spitzer's First Exploration of Fusion

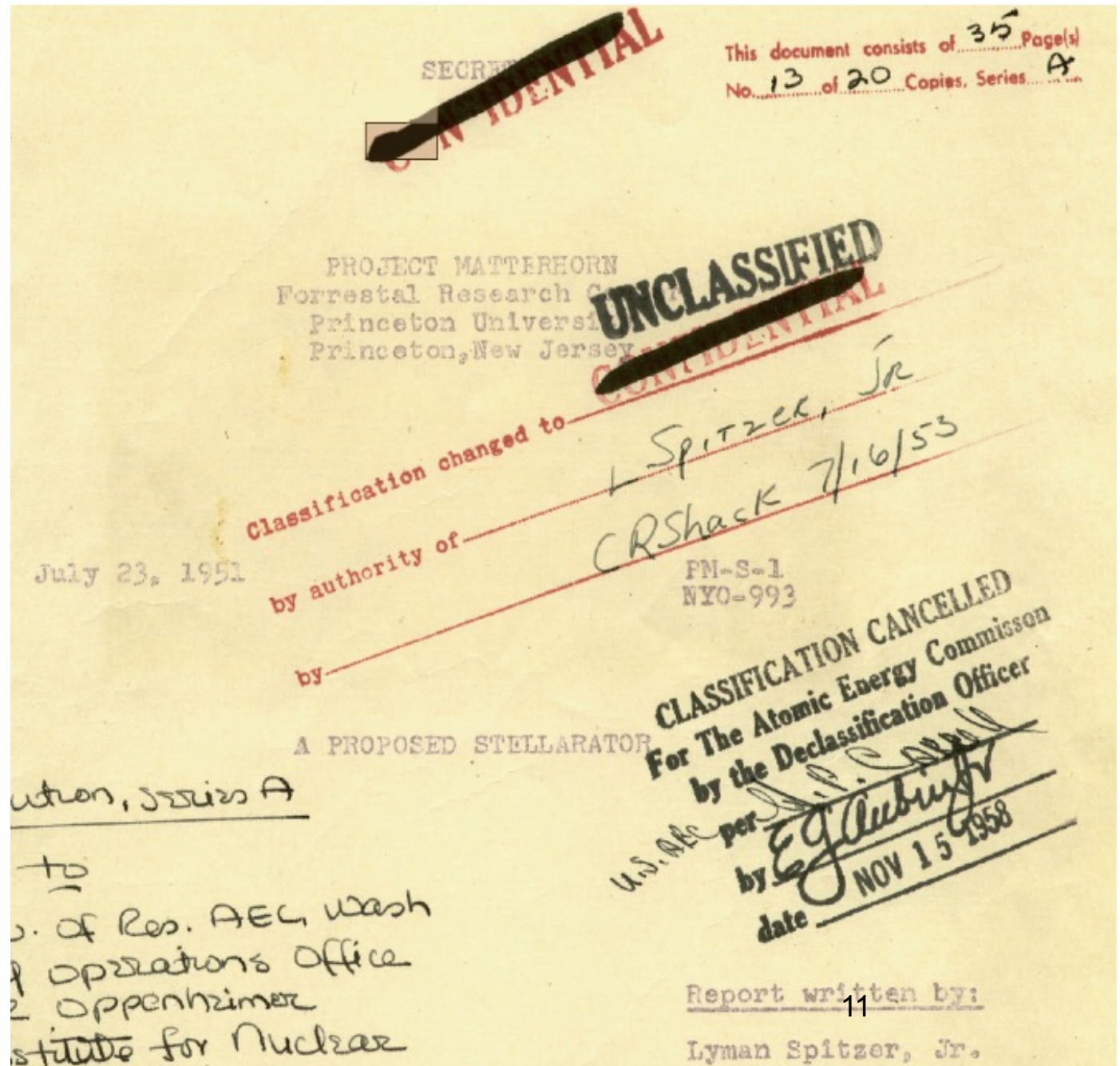
- 25 June, 1950, Korean war started.
- Lyman Spitzer and John Wheeler think about starting a theoretical program at Princeton studying thermonuclear explosions. (Spitzer worked on sonar in WWII)
- March 24, 1951, President Peron of Argentina claimed his scientist, Ronald Richter, had produced controlled fusion energy in the lab. Quickly dismissed by many (later shown to be bogus), but got Spitzer thinking on the Aspen ski slopes.
- Spitzer had been studying hot interstellar gas/plasma for several years & had recently heard a series of lectures by Hans Alfvén on plasmas* (Alfvén later got Nobel prize)
- Spitzer knew a simple toroidal magnetic field couldn't confine a plasma. The story (partially apocryphal?) is that on the chair lift rides in March 1951, he invented the tokamak (later invented in Russia by Igor Tamm and Andrei Sakharov), but dismissed it because it wasn't steady state. Somehow came up with the idea of twisting a torus into a figure-8.
- May 11, 1951, meeting at AEC to describe figure-8 and other approaches to fusion.
- May 12, Spitzer submits proposal to AEC to build a figure-8 stellarator.
- July 1, gets \$50k (= \$600k in 2024) from AEC for 1 year (Bromberg, p. 21, <http://en.wikipedia.org/wiki/Perhapsatron>)

2cd UN Atoms For Peace Conference, Geneva 1958.



SIM-8, one of the simulator stellarators (w/ e-beam) used in demonstrations at the 2cd Atoms-For-Peace Conference, Geneva (1958)

Spitzer's Original May 12, 1951 Proposal



- July 23 reprint of original May 12, 1951 proposal
- All early PM-S reports available online:
- <http://findingaids.princeton.edu/collections/PPL001/c0001>
- <http://diglib.princeton.edu/pdfs/PPL001/c0002.pdf>
- <http://library.pppl.gov/>
- (large PDFs > 100MB)

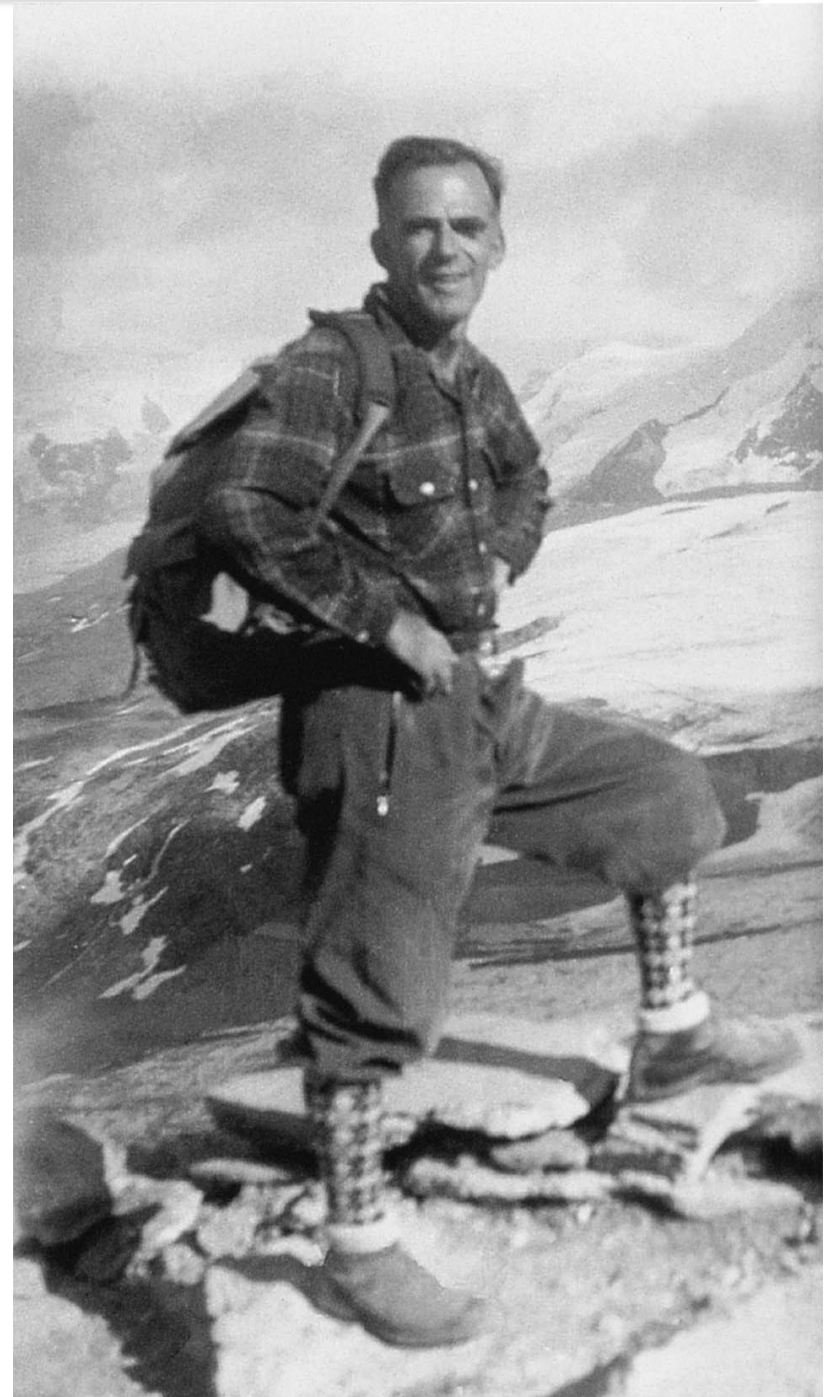
July 1, 1951 Project Matterhorn Begins

- Two sections:
 - S: headed by Spitzer, studying the stellarator concept
 - B: headed by John Wheeler
- “Project Matterhorn” name recommended by Spitzer, because “The work at hand seemed difficult, like the ascent of a mountain”*.
- “Stellarator” named by Wheeler, “a star generator”

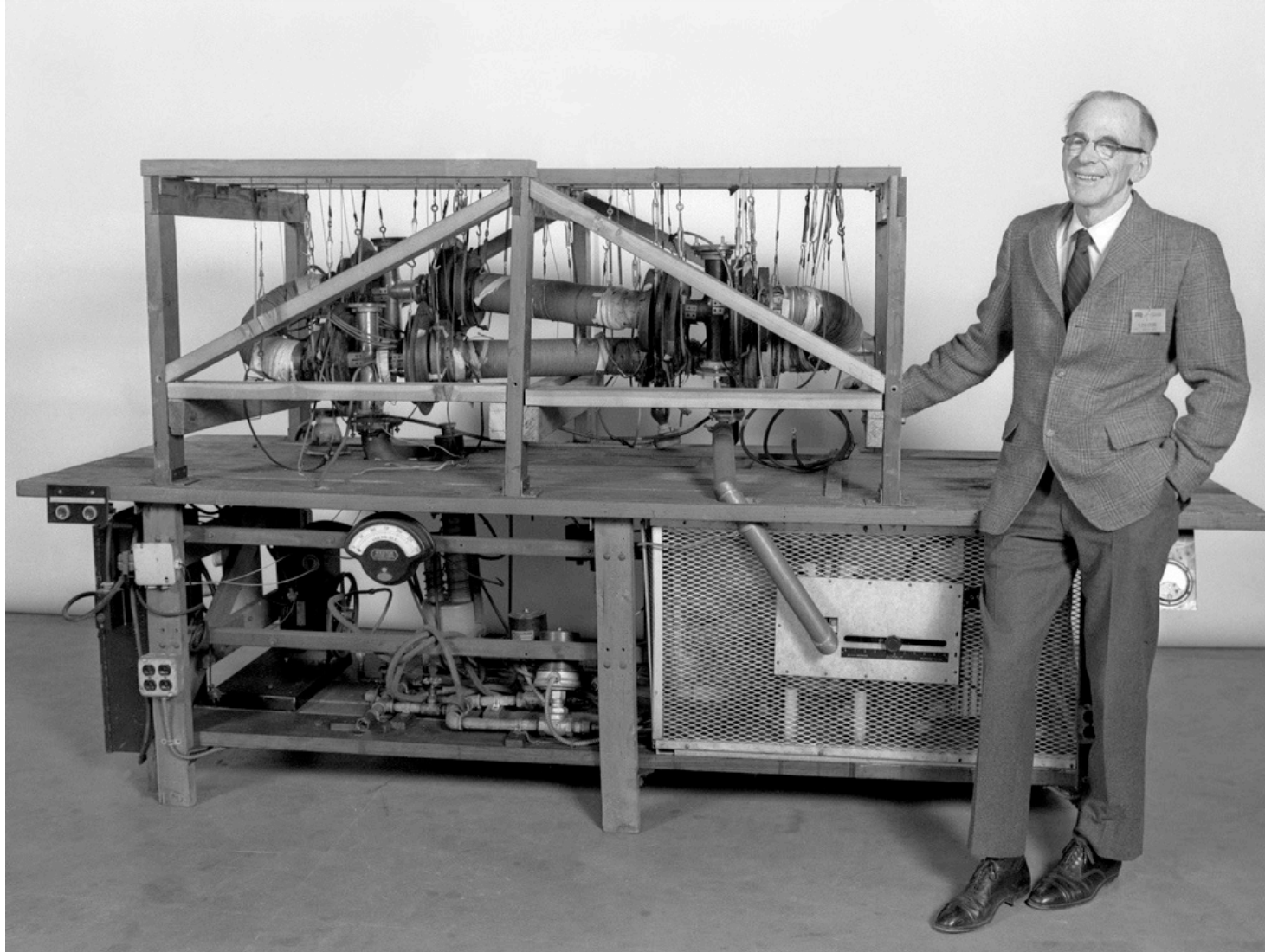
A serious mountain climber:

The American Alpine Club annually awards the Lyman Spitzer Cutting Edge Climbing Award.

Lyman Spitzer, Jr. once climbed the outside of the Graduate College tower...

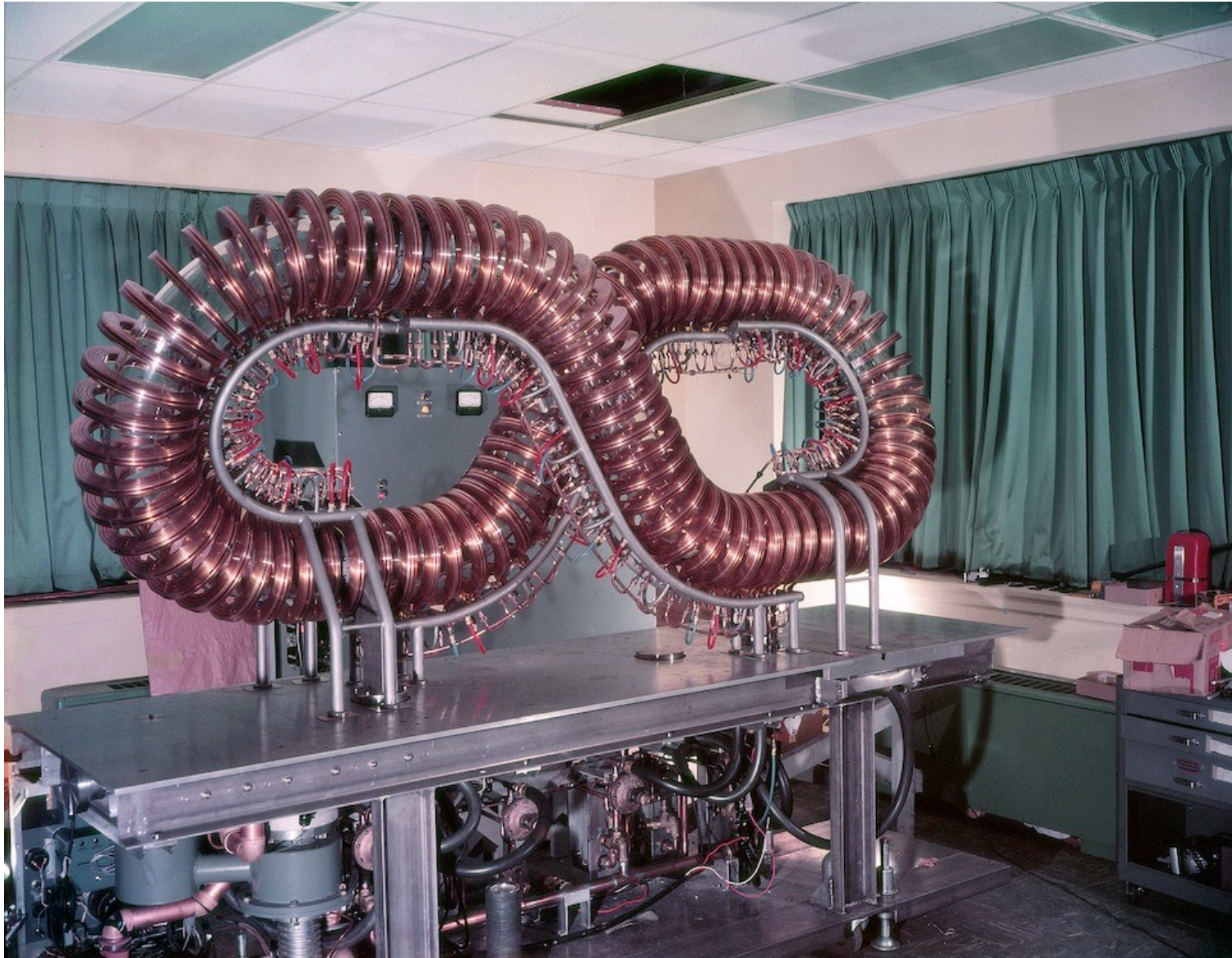


Spitzer's Model-A Stellarator



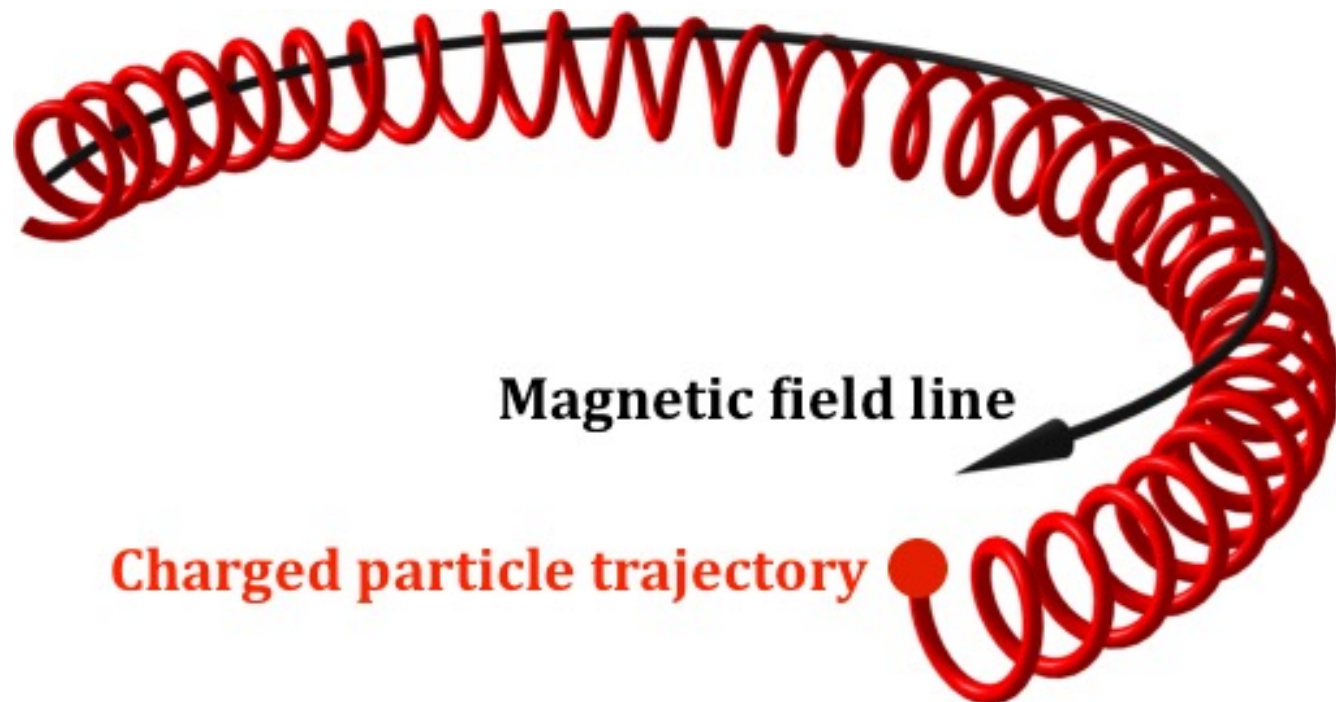
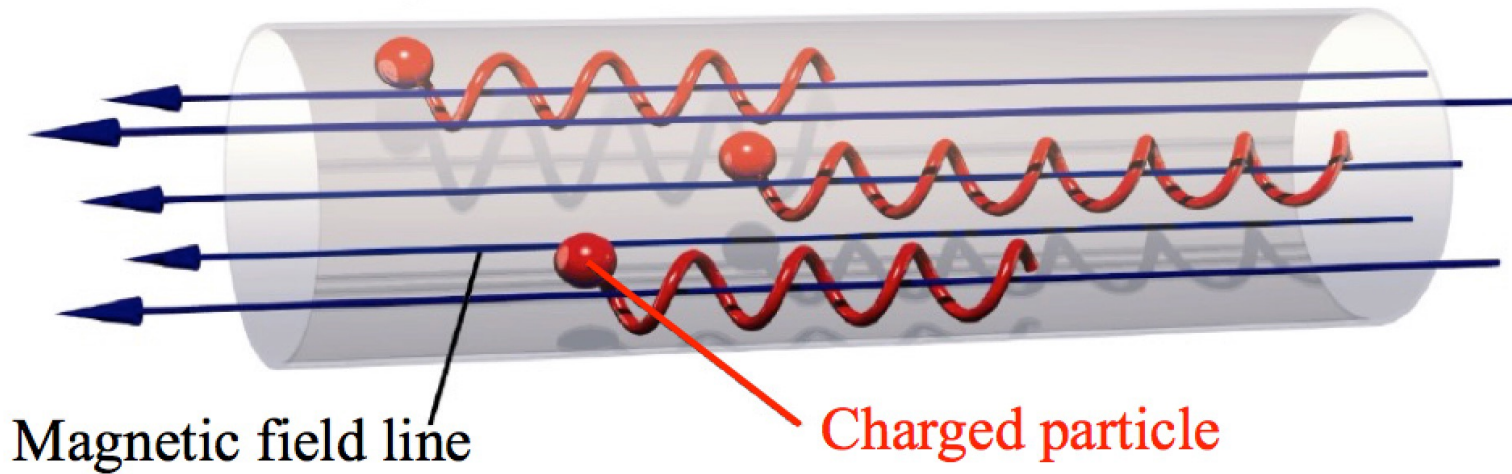
- Operated in early 1953, as figure-8 or racetrack. Showed that figure 8 could make plasmas much more easily (at lower voltage & field).
- Spitzer and his friend Prof. Martin Schwarzschild (both theorists) wound copper coils by hand, while sitting on the floor of "rabbit hutch" on Forrestal campus (formerly Rockefeller Inst. for Medical Research). Tanner, "Project Matterhorn": Model-A fabricated under direction of Profs. C.H. Willis (chief engineer for Model-A & B) and N. Mather.
- Hired Prof. James Van Allen to run experimental program, 1953-1954. Mel Gottlieb came in 1954
- This picture in 1983, just before donated to the Smithsonian.

2cd UN Atoms For Peace Conference, Geneva 1958.

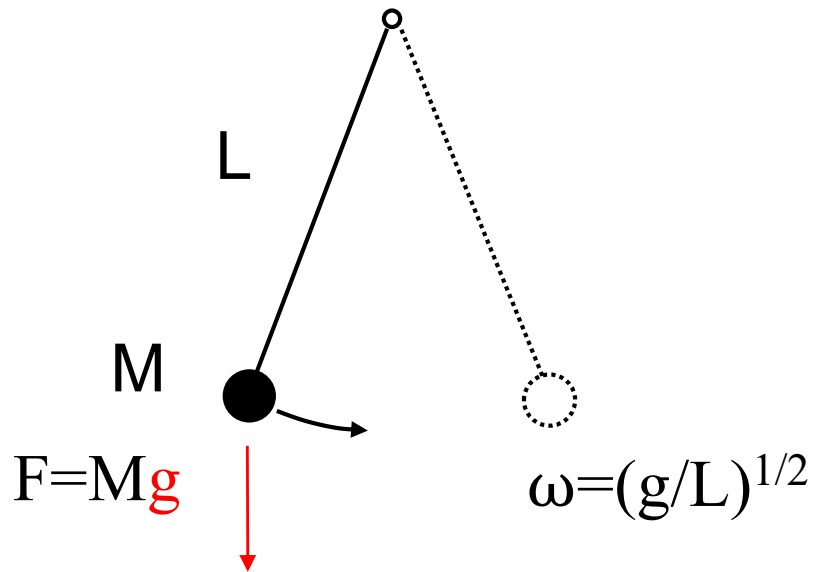


SIM-8, one of the simulator stellarators (w/ e-beam) used in demonstrations 14
at the 2cd Atoms-For-Peace Conference, Geneva (1958)

Magnetic confinement of particles



Stable Pendulum



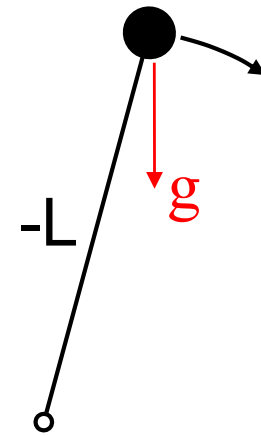
$$X(t) = X_0 \cos(\omega t) + \dots$$

Famous Euler's Formula:

$$e^{-i\omega t} = \cos(\omega t) - i \sin(\omega t)$$

Unstable Inverted Pendulum

(rigid rod)



$$\omega = (-g/|L|)^{1/2} = i(g/|L|)^{1/2} = i\gamma$$

↑ instability

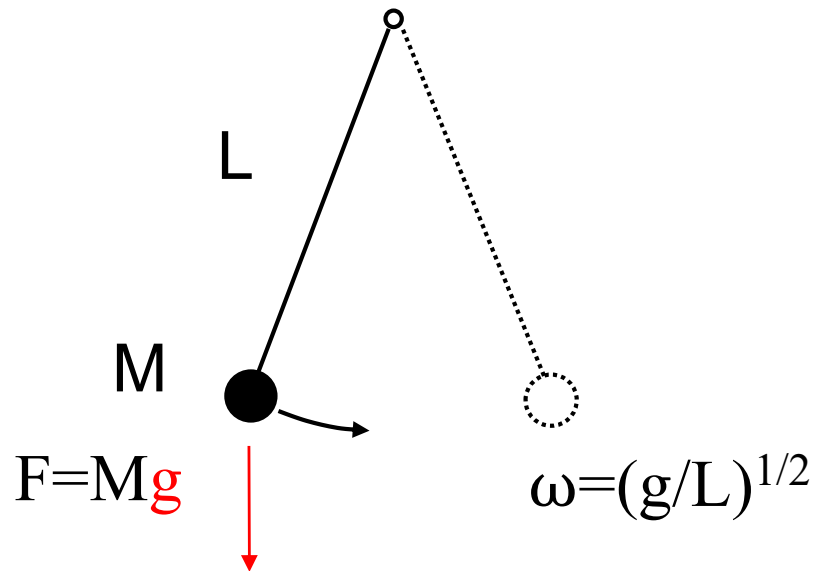
$$X(t) = X_0 e^{\gamma t} + \dots$$

Replace ω with $i\gamma$:

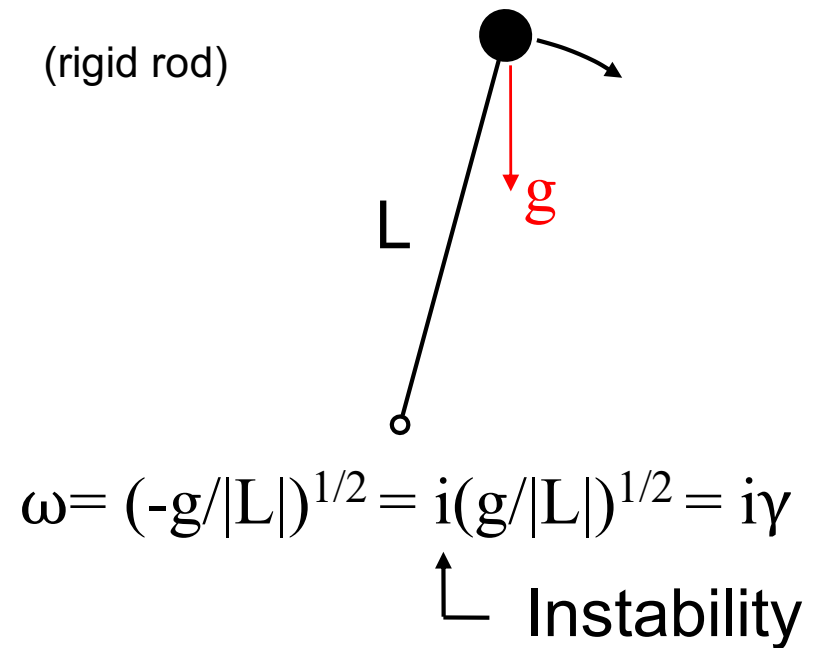
$$e^{-i\omega t} = e^{-i(i\gamma)t} = e^{\gamma t}$$

(broom demonstration)

Stable Pendulum

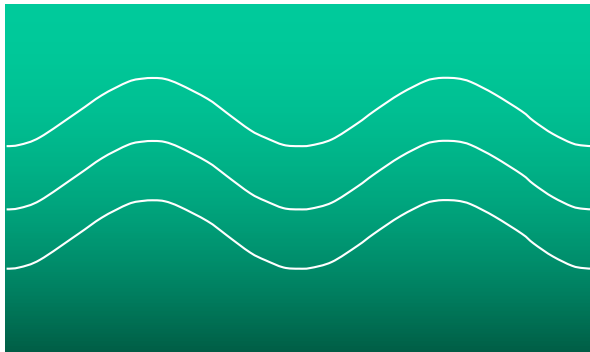


Unstable Inverted Pendulum



Density-stratified Fluid

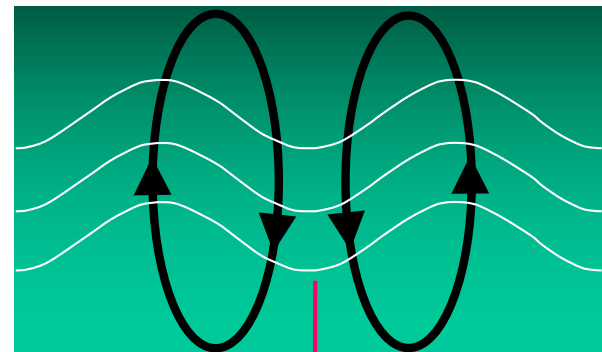
$$\rho = \exp(-y/L)$$



stable $\omega=(g/L)^{1/2}$

Inverted-density fluid ⇒ Rayleigh-Taylor Instability

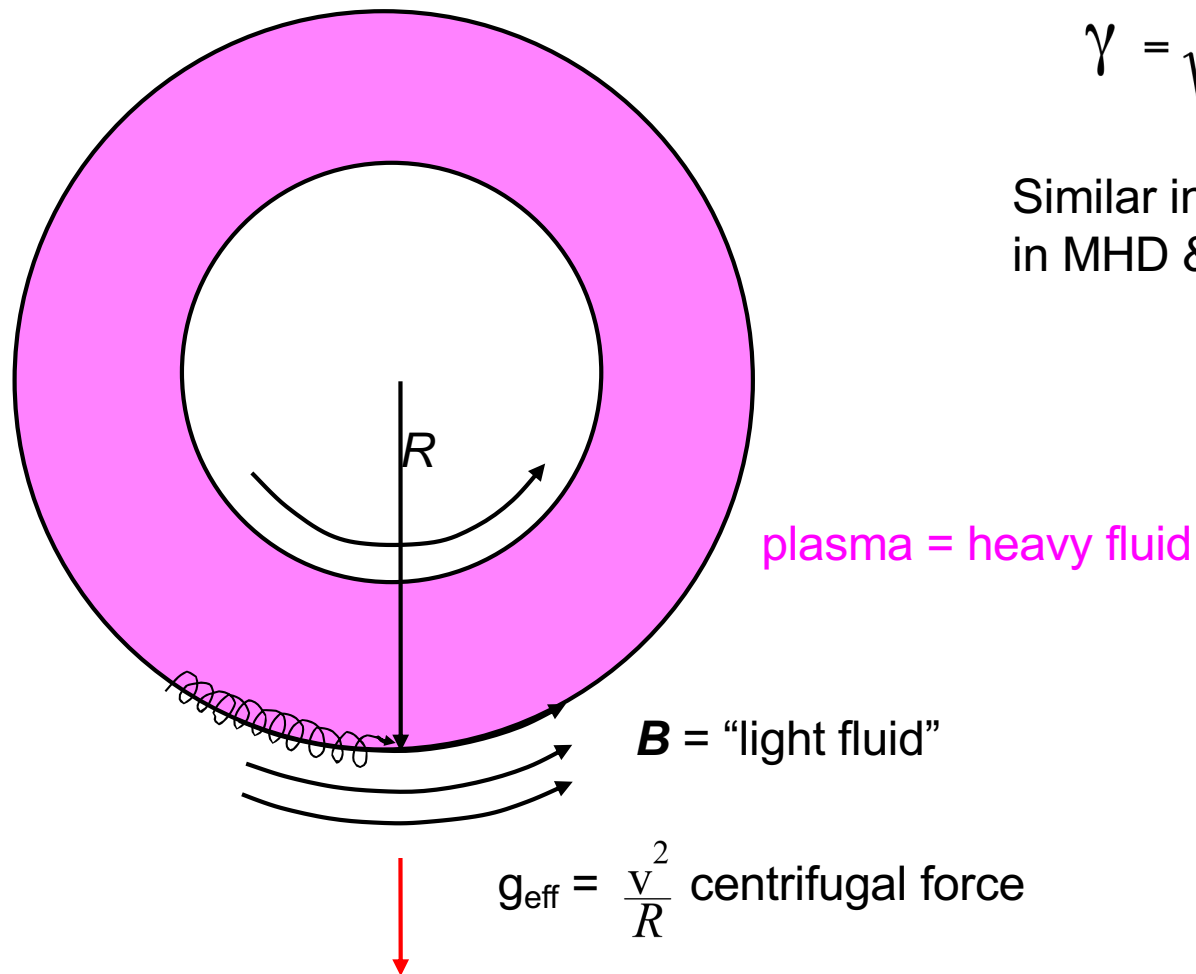
$$\rho = \exp(y/L)$$



Max growth rate $\gamma=(g/L)^{1/2}$

Why a simple magnetic torus is unstable: ≈ Inverted Pendulum / Rayleigh-Taylor Instability

Top view of toroidal plasma:



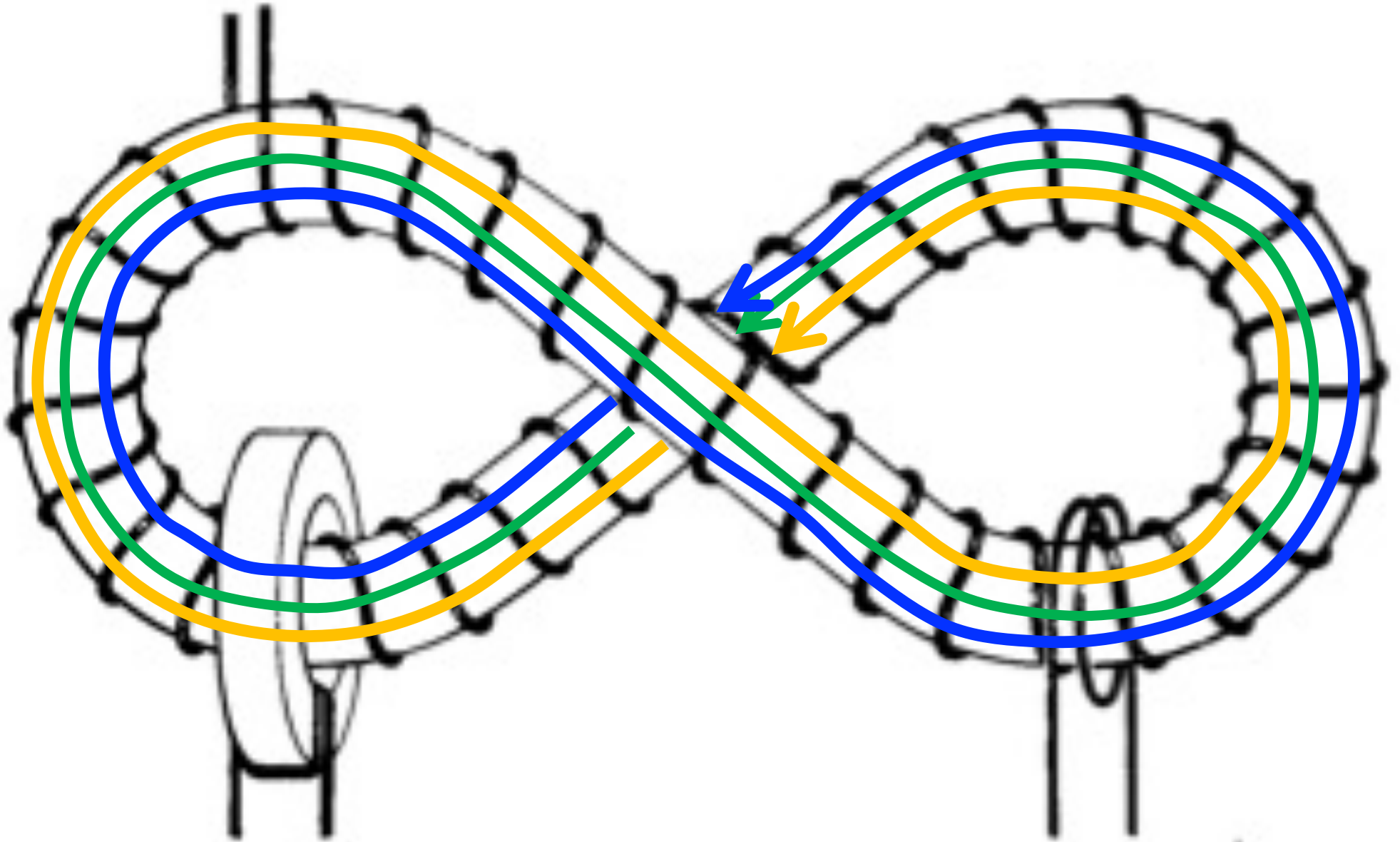
Growth rate:

$$\gamma = \sqrt{\frac{g_{\text{eff}}}{L}} = \sqrt{\frac{v_t^2}{RL}} = \frac{v_t}{\sqrt{RL}}$$

Similar instability mechanism
in MHD & drift/microinstabilities

$1/L = \nabla\rho/\rho$ in MHD,
 \propto combination of ∇n & ∇T
in microinstabilities.

Spitzer's stellarator trick: twist torus into figure-8

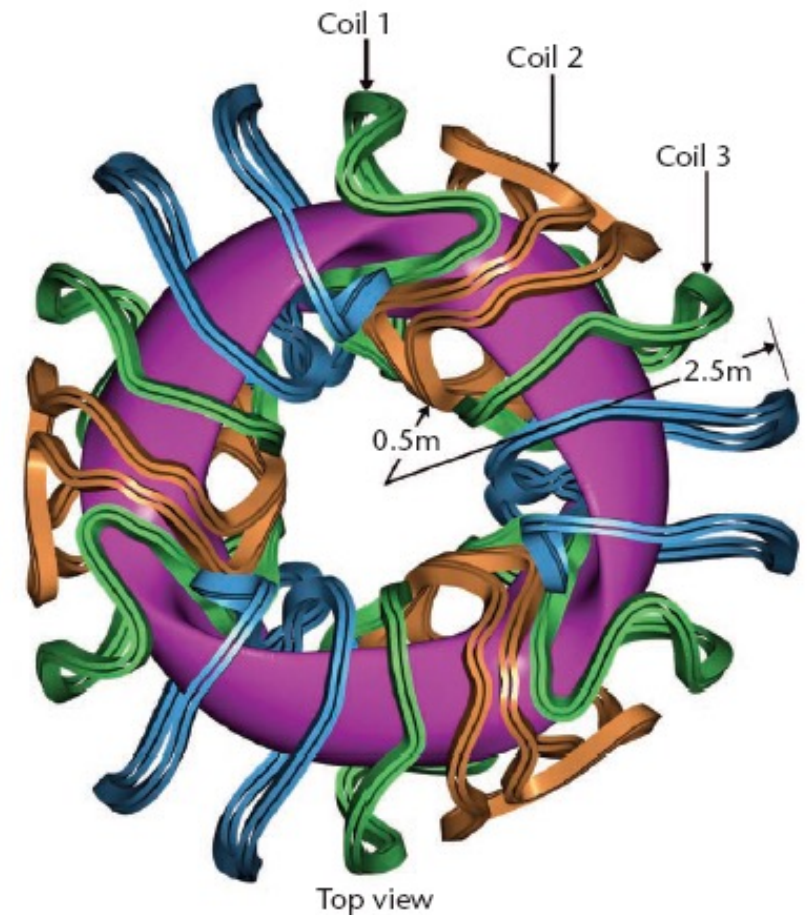
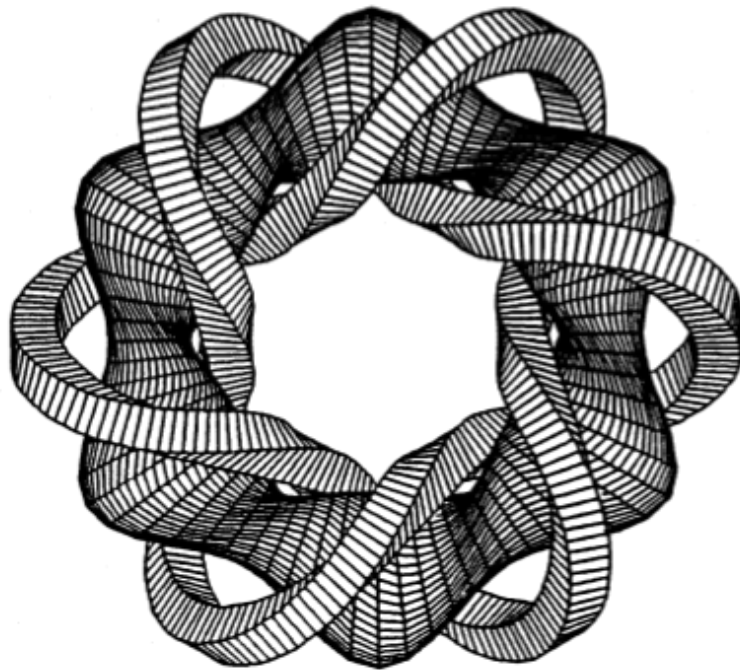


Centrifugal force alternates directions on each side
(relative to the plasma center – the green line)

A Demonstration

Modern stellarators

Spitzer et al. later realized that particles can be confined by a net poloidal twist in the magnetic field produced by helical coils. (First realization of the “Berry Phase”^{*}.) Eventually evolved into modern stellarator designs with modular, unlinked coils.



JF Lyon et al., 1997 <http://aries.ucsd.edu/LIB/REPORT/SPPS/FINAL/chap2.pdf>

Princeton Quasar (Quasi-axisymmetric Stellarator)
/ NCSX

^{*} pointed out in Bhattacharjee, 1992

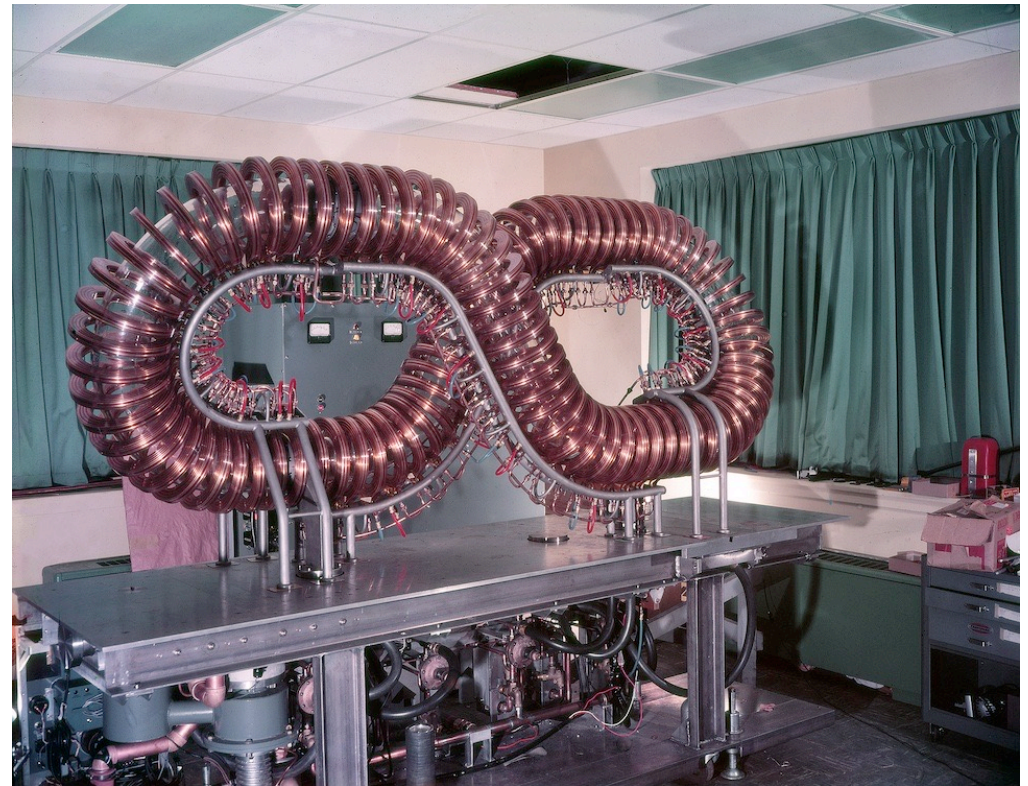
2cd Atoms-For-Peace Conference, Geneva 1958.

Controlled fusion energy declassified worldwide in 1958. Roald Sagdeev, then a young physicist, said that going from Soviet Union to meet western scientists was like meeting Martians.

Both sides invented pinches, mirror machines, symmetric toroidal devices. But the one unique idea invented only by one side was the stellarator.

Rosenbluth went to the meeting, surprised to see Russians had a stellarator: “... the Stellarator always seemed to me like something ... I never quite understood how Spitzer was ever able to envision it. His geometrical intuition was better than mine. Sure enough, the Russians showed up with a Stellarator. And Sagdeev later told me that that was just a fake. Artsimovich had heard about our Stellarator and told them we couldn't claim that we had something they hadn't thought of, so they just added it on.”

“... That's one of the few examples I know that that sort of chicanery was going on in this business.” AIP oral history, Marshall Rosenbluth, 2003, http://www.aip.org/history/ohilist/28636_1.html



SIM-8, one of the simulator stellarators (w/ e-beam) used in demonstrations at the 2cd Atoms-For-Peace Conference, Geneva (1958)

B-3 Stellarator Group

Original Plan: Models A, B, C, and D (industrial scale)

Model A showed basic advantage of figure 8 over racetrack.

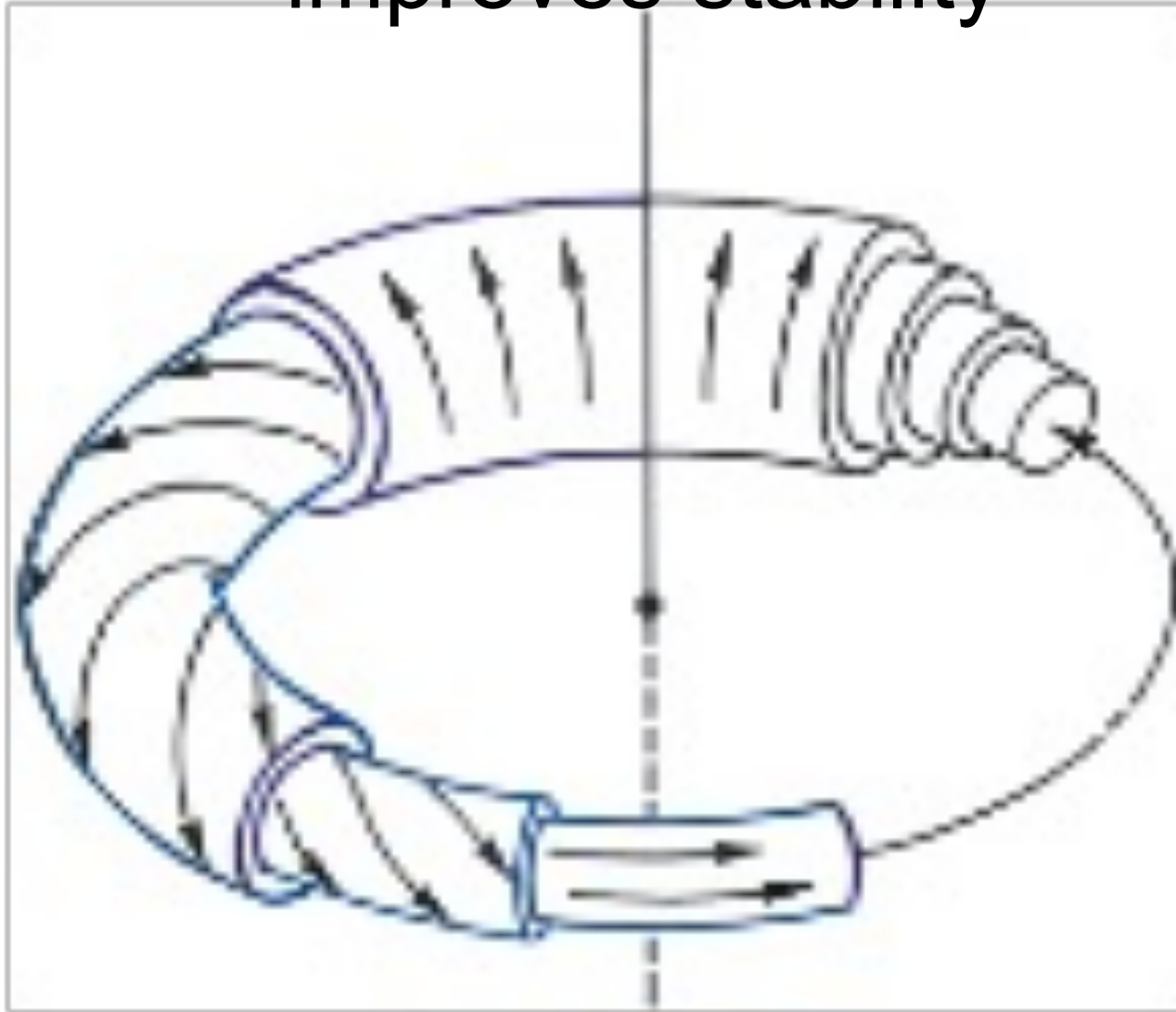
But started to find difficulties with Model B. Series of expts. built in 1950's: Model B, B-2, B-3, B-64/65/66.

B-3 was first with $\ell = 3$ helical coils, provides magnetic shear in response to Teller's concerns.

Spitzer built a team of excellent scientists. Here are members of the B-3 Group in 1960, including Bob Ellis (3rd from left on bottom), who led the PPPL experimental program for decades.



Sheared helical magnetic fields improves stability



Extreme example,
magnetic field is mostly in
toroidal direction in
standard tokamak.

magnetic shear can help stabilize instabilities
(negative & zero average shear can be better, average \neq local shear)

Model-C Stellarator, 1961-1969

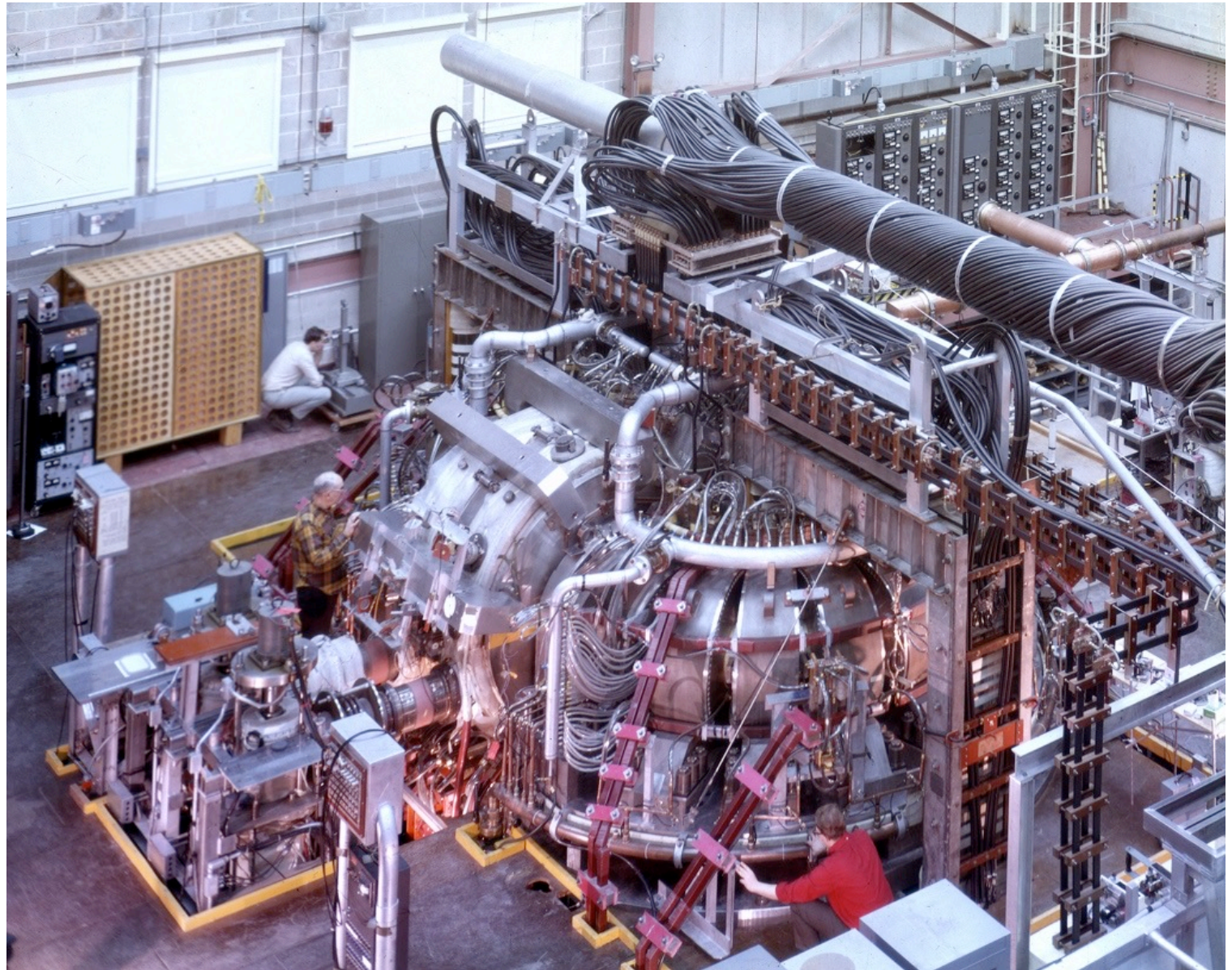
$R \sim 1.9 \text{ m}$
 $a = 5 - 7.5 \text{ cm}$

Principal finding:
strong turbulent
diffusion limited
performance:

$D \sim D_{\text{Bohm}}$
 $\sim T_e / (eB)$

But with 4MW ICRF
heating, got mirror
trapped
 $T_i \sim 8 \text{ keV}$,
avg $T_i \sim 400 \text{ eV}$

Stix, 1998



(1967). Converted to ST Symmetric Tokamak in 1970, in 4 months, after breakthrough results by Russian tokamak reported at 1968 IAEA meeting, much better than Bohm diffusion. British laser team went to Russia, confirmed $T_e \sim 1 \text{ keV}$ with just ohmic heating (Nature, Nov. 1969).

December 9-10, 1993: Momentous Days for Two of Spitzer's Biggest Ideas: Fusion Energy & Space Telescopes

- Sequence of larger Princeton tokamaks built starting in 1970: ST, ATC, PLT, PDX ... (and others elsewhere). Arab Oil Embargo & 1st Energy Crisis led to large funding of alternative energy. Combined with good performance of tokamaks, motivated a large tokamak experiment to actually use tritium. 1974: Design of TFTR began, 1976: construction authorized, 1982: first plasma (construction ~\$1.4B in 2012\$), 1993: DT experiments.
- December 9, 1993, TFTR (Tokamak Fusion Test Reactor) does first DT shots, eventually made 10 MW of fusion power. Joint European Torus (JET) eventually make 17 MW.
- Fusion power gain $Q = (\text{Fusion power out}) / (\text{Heating power in})$
“Increased the fusion power gain by a factor of 1 million over the value when it was designed in 1975, to $Q = 0.3$ in 1995”
- December 10, 1993: Space shuttle fixed Hubble Space Telescope optics.

<http://www.nytimes.com/1993/12/10/us/scientists-at-princeton-produce-world-s-largest-fusion-reaction.html>

- <http://www.nytimes.com/1993/12/11/us/shuttle-releases-hubble-telescope.html>

Scientists at Princeton Produce World's Largest Fusion Reaction

By Malcolm W. Browne

Princeton, N.J., Dec. 19 — A huge experimental reactor... Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor...

Fusion record set at Princeton

Princeton Plasma Physics Laboratory

Princeton, N.J. — Scientists at Princeton University... Tokamak Fusion Test Reactor... 3.1 million watts...

The Orlando Sentinel 2nd fusion test again 'replicates the sun'

Princeton Plasma Physics Laboratory



Princeton Plasma Physics Laboratory

Princeton, N.J. — Hours after producing the world's most powerful controlled fusion reaction, scientists nearly doubled their record... Princeton University... Tokamak Fusion Test Reactor...

Keep fusion dream alive

Nuclear fusion promises cheap, unlimited energy supply; \$8 billion in research support, it could take over when oil runs out

The promise of nuclear fusion... Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor...

STAR POWER Do we have the vision to harness it?

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

FUSION EUPHORIA

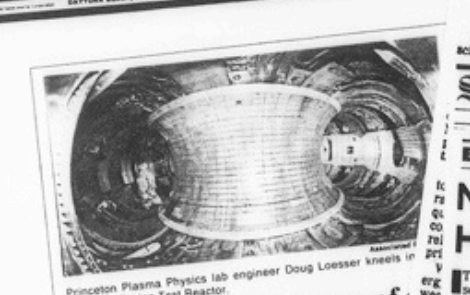
Princeton team again shatters its record producing energy in huge reactor



Ronald Davidson, left, a physicist who heads the Princeton Plasma Physics Laboratory...

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

THE NEWS-JO Serving Volusia And Flagler Counties SATURDAY



Princeton Plasma Physics Lab engineer Doug Loesser kneels in front of the Tokamak Fusion Test Reactor.

Fusion lab clones power of the sun... Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor...

San Francisco Chronicle

IN THE VOICE OF THE WEST

Nuclear Fusion's Hopeful Promise

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

Chicago Tribune



Princeton Plasma Physics Laboratory

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

THE SUN

circulation 496,067

Fusion reactor generates record energy in tests

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

THE DAILY OKLAHOMAN

Will fusion turn out to be 1993's big story?

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

The top science stories of 1993

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

The Philadelphia Inquirer

A milestone for nuclear fusion

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

Fusion power: The fire finally lights

Princeton Plasma Physics Laboratory... Tokamak Fusion Test Reactor... 3.1 million watts... 'replicates the sun'...

TFTR First DT Fusion Shot, Dec. 9, 1993



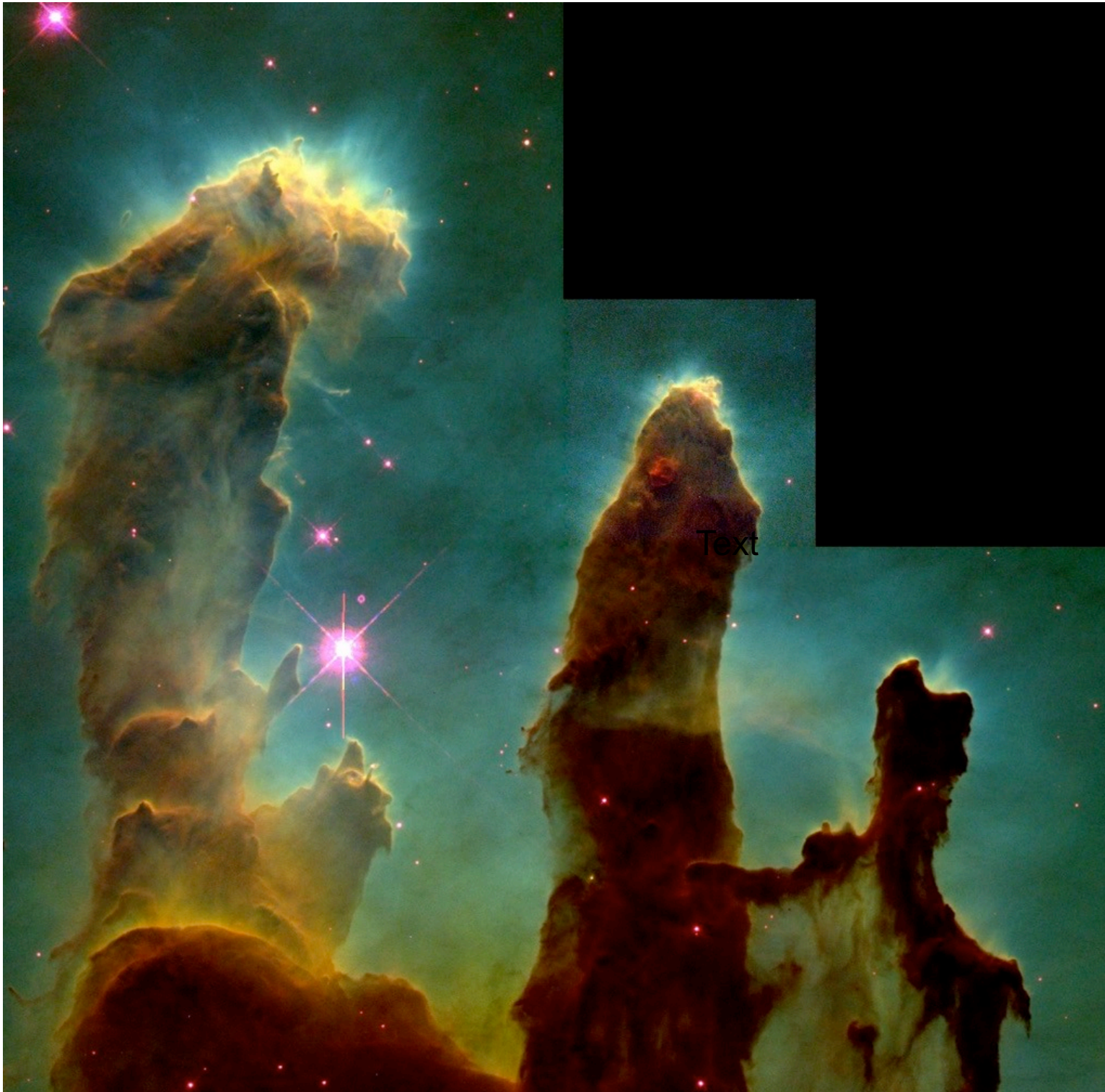
- December 9, 1993. TFTR does first DT shots, eventually making 10 MW of fusion power.
- <http://www.nytimes.com/1993/12/10/us/scientists-at-princeton-produce-world-s-largest-fusion-reaction.html>

TFTR First Plasma, 3:06 am, Dec. 24, 1982





- December 10, 1993: Space Shuttle fixed Hubble Space Telescope optics.
- <http://www.nytimes.com/1993/12/11/us/shuttle-releases-hubble-telescope.html>



The Eagle Nebula:
“Pillars of Creation”
gas pillars in a star-
forming region.

Text

The road ahead for fusion:

- Continuing innovation: Interesting ideas being pursued in fusion, & reduce the cost of power plants

My Perspective on Fusion Energy

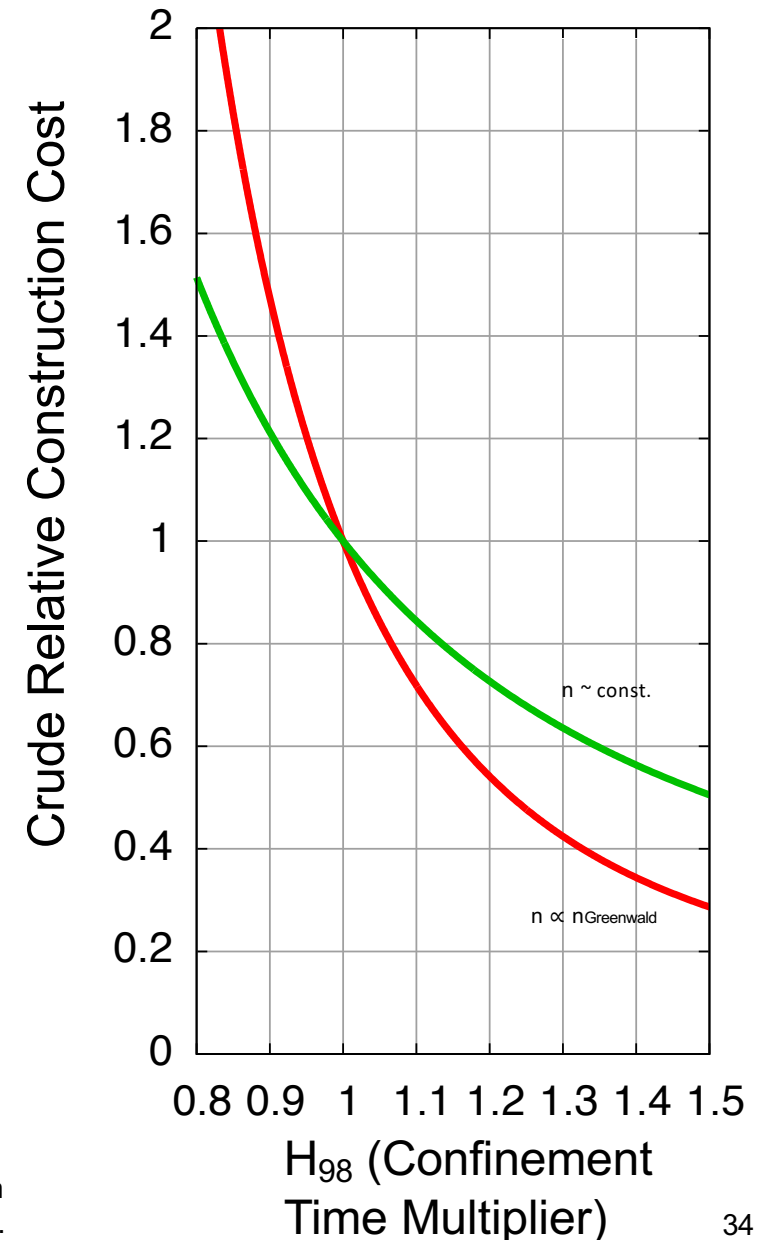
- Need to pursue many energy sources. All have tradeoffs & uncertainties. Challenging to supply all energy needed in the long term. Energy demand expected to triple throughout this century as poor countries continue to develop.
- Fusion energy is hard, but it's an important problem, we've been making progress, and there are interesting ideas to pursue that could make it more competitive.

Improving Confinement Can Significantly ↓ Size & Construction Cost of Fusion Reactor

Well known that improving confinement & stability limits can lower Cost of Electricity / kWh, at fixed power output.

Even stronger effect if consider smaller power: better confinement allows significantly smaller size/cost at same fusion gain Q ($nT\tau_E$).

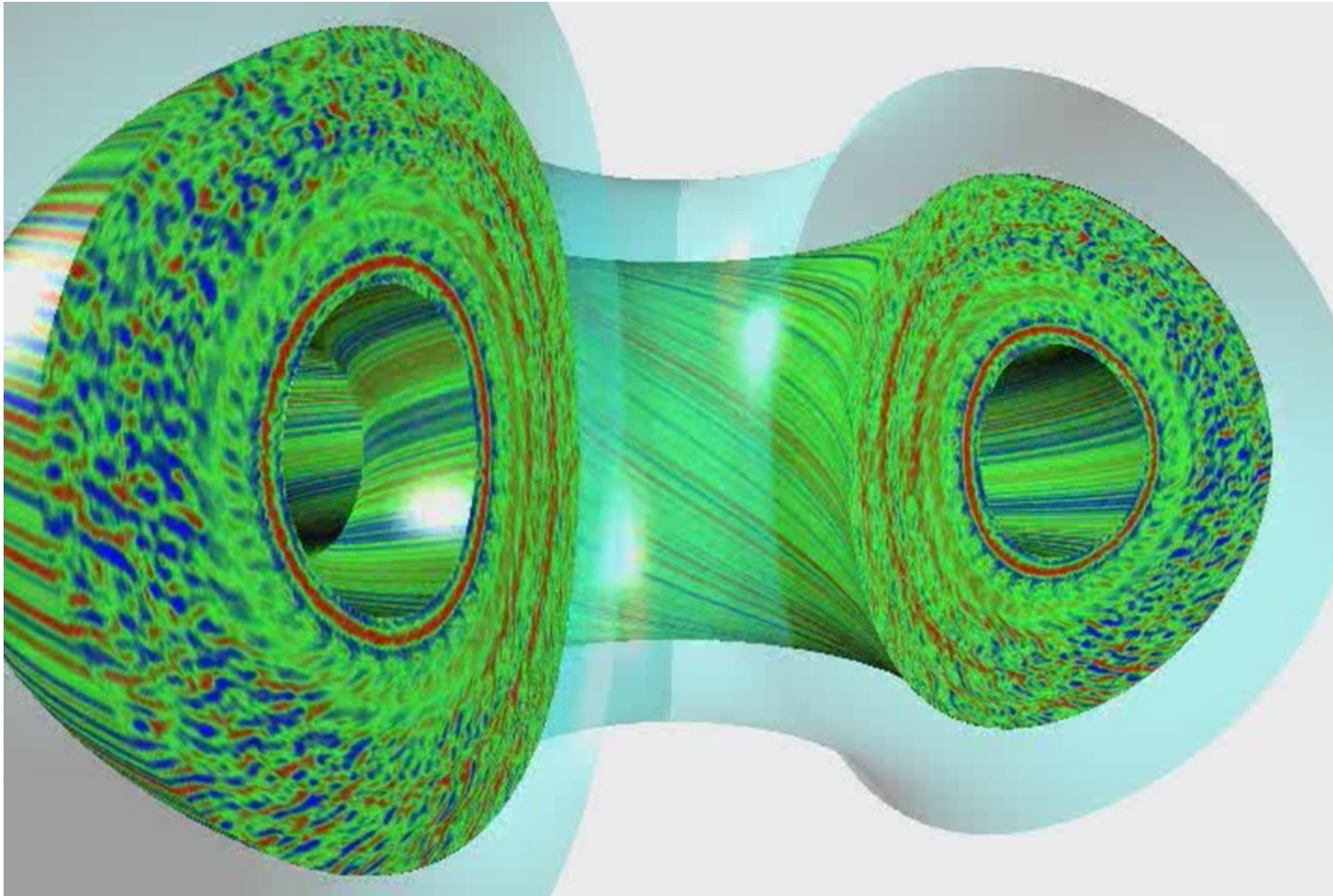
Comprehensive computer simulations on supercomputers are helping us search for improved fusion concepts. Want to be confident of extrapolation to larger sizes when building billion \$ experiments.



Interesting Ideas To Improve Fusion

- * **Liquid metal (lithium, tin) films or flows on walls:** (1) protects solid wall (2) absorbs incident hydrogen ions, reduces turbulence, and improves global performance.
- * Spherical Tokamaks (STs) appear to be able to suppress much of the ion turbulence: PPPL upgrading the National Spherical Tokamak Experiment (NSTX-U) to test scaling
- * **Advanced tokamaks**, alternative operating regimes (reverse magnetic shear or “hybrid”), methods to control Edge Localized Modes, negative triangularity. Tokamaks sometimes spontaneously spin (like a smoke ring vortex) and reduce the turbulence some.
- * Many possible stellarator designs, room for further optimization: Quasi-symmetry / quasi-omnigenity improvements discovered relatively recently, after 40 years of fusion research. Stellarators fix disruptions, steady-state, density limit.
- * Tokamaks & stellarators furthest along, but some researchers & companies pursuing **more speculative concepts** (mirrors, FRCs, pinches, ...), sometimes with interesting new twists. Might be cheaper. **Can shear flow help stabilize one of these concepts? Plasma smoke ring?**
- * **Advances in magnet technology** (high-temperature superconductors, higher field) and other fusion-related technologies could help all fusion concepts.
- * **Robotic manufacturing advances:** reduce cost of complex, precision, specialty items

Fairly Comprehensive 5-D Gyrokinetic Turbulence Codes Have Been Developed



Major progress in developing computer simulations of plasma turbulence,

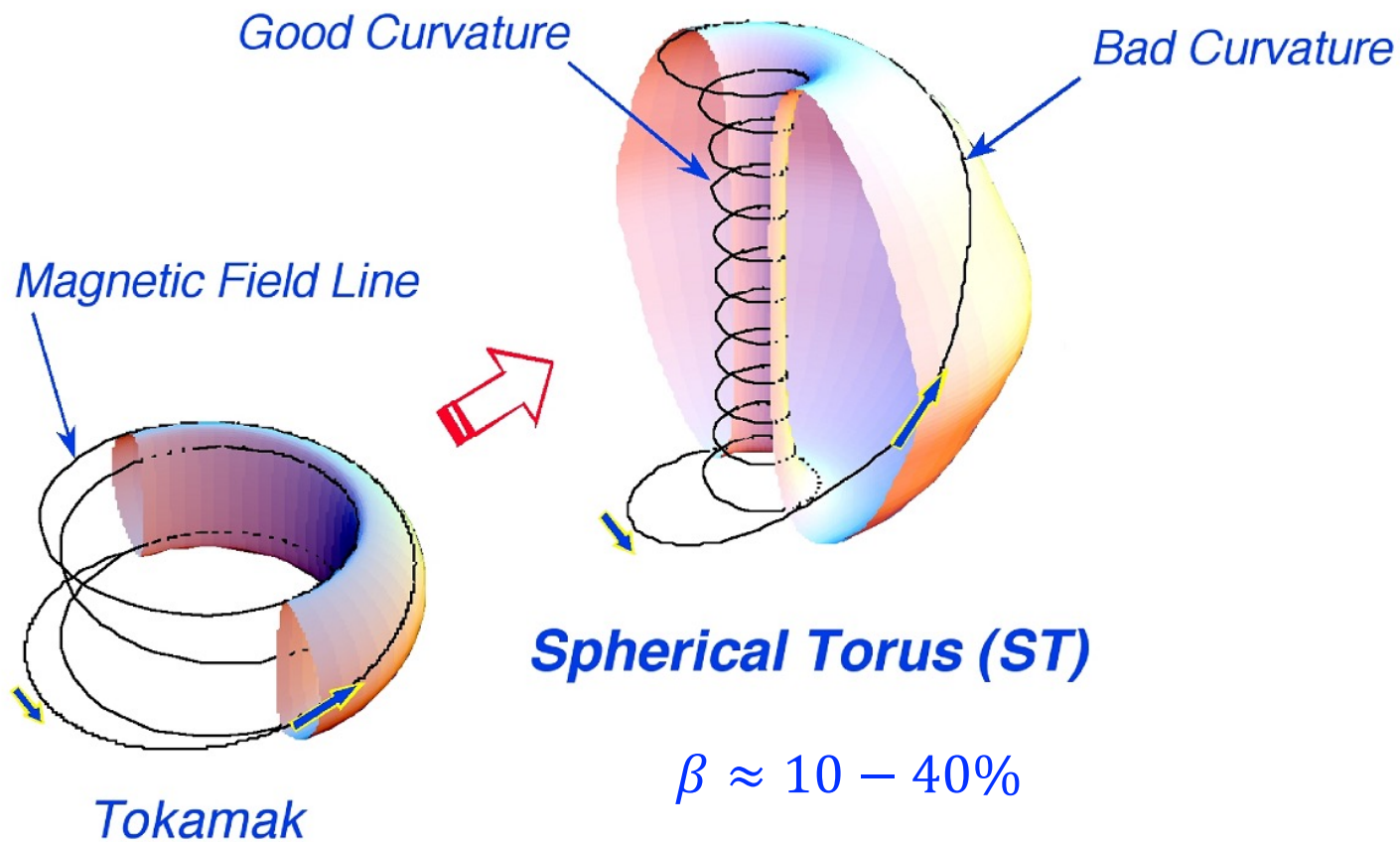
but still important unfinished work, including edge region.

Movie of density fluctuations from GYRO simulation
<http://fusion.gat.com/THEORY/images/0/0f/N32o6d0.8.mpg>
from <http://fusion.gat.com/theory/Gyromovies>

Waltz, Austin, Burrell, Candy, PoP 2006

- 500 radii x 32 complex toroidal modes (96 binormal grid points) x 10 parallel points along half-orbits x 8 energies x 16 $v_{||}/v$, 12 hours on ORNL Cray X1E with 256 MSPs

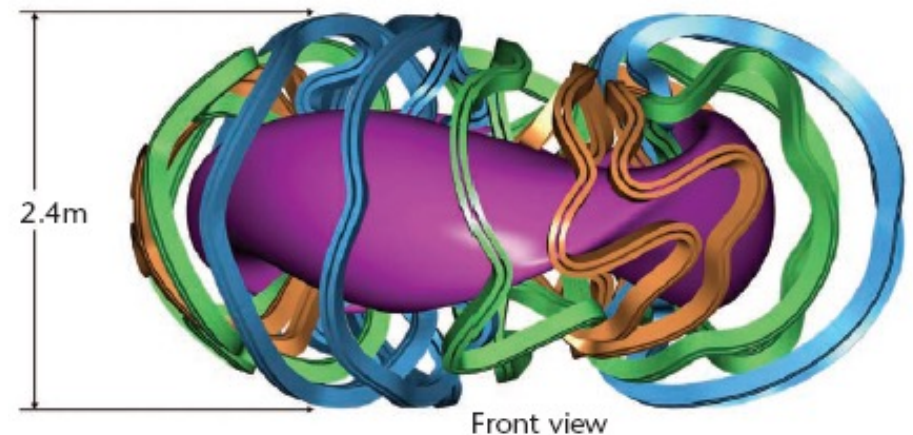
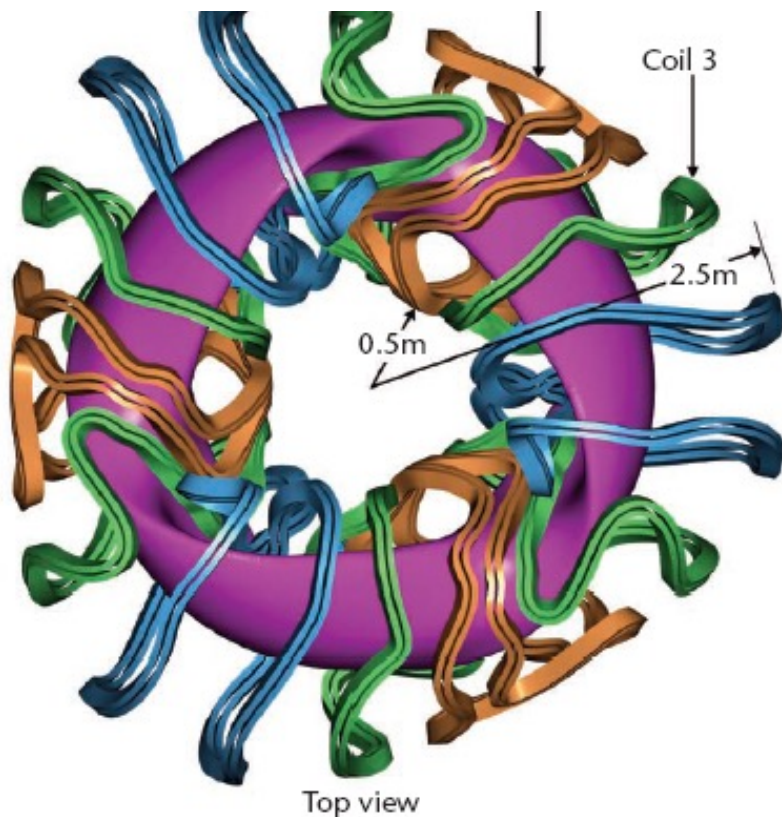
Spherical Torus has improved confinement and pressure limits (but less room in center for coils)



National Spherical Tokamak Experiment Upgrade (NSTX-U) at PPPL being rebuilt and enhanced. Has twice the magnetic field and heating power as original NSTX, to see how performance scales towards a real reactor scale.

Improved Stellarators Being Studied

- Originally invented by Spitzer ('51), the unique idea when fusion declassified ('57)
- Mostly abandoned for tokamaks in 1969. But computer designs now much better.
- Hidden quasi-symmetry discovered in 80's-90's: don't need vector \mathbf{B} exactly symmetric toroidally, $|\mathbf{B}|$ symmetric in field-aligned coordinates sufficient to be as good as tokamak.
- Magnetic field provided by external coils, inherently more stable, intrinsically steady state, no hard stability limit.
- Robotic manufacturing / 3-D printing might reduce cost a lot?



~\$1B W7-X stellarator in Germany getting good performance.

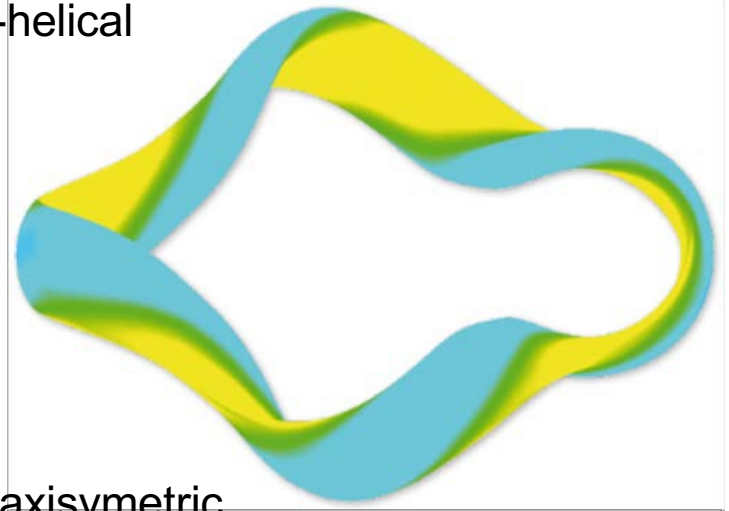
Many types of stellarators possible

Quasisymmetry discovered in 80's, but full range of possibilities still being explored. (Color contours indicate magnetic field strength.)

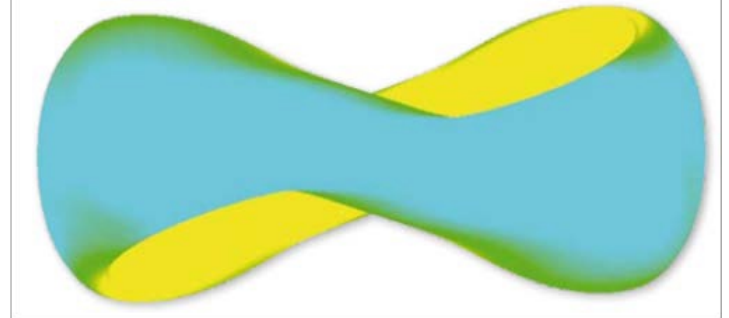
Recently discovered designs that confine single-particle orbits extremely well, even for energetic particles. (Paul & Landreman PRL 2022.)

Ongoing research: particles can interact collectively and cause small scale turbulent fluctuations. Not sure how these will scale to a larger reactor-scale. Comprehensive computer codes being developed.

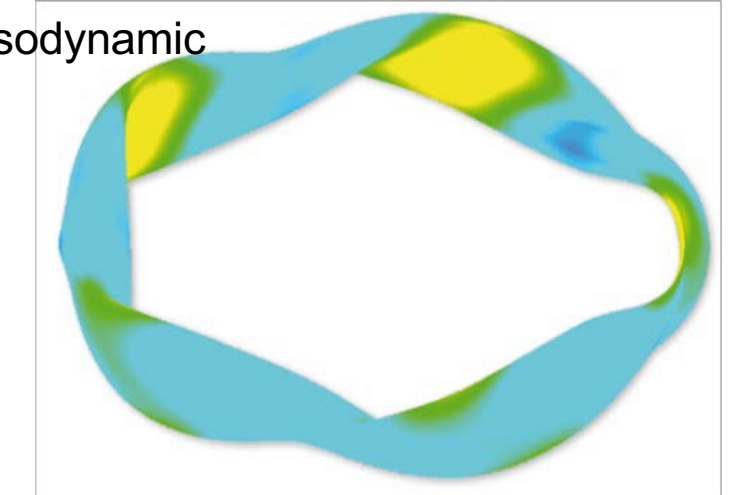
QH, quasi-helical



QA, quasi-axisymmetric



QI, quasi-isodynamic

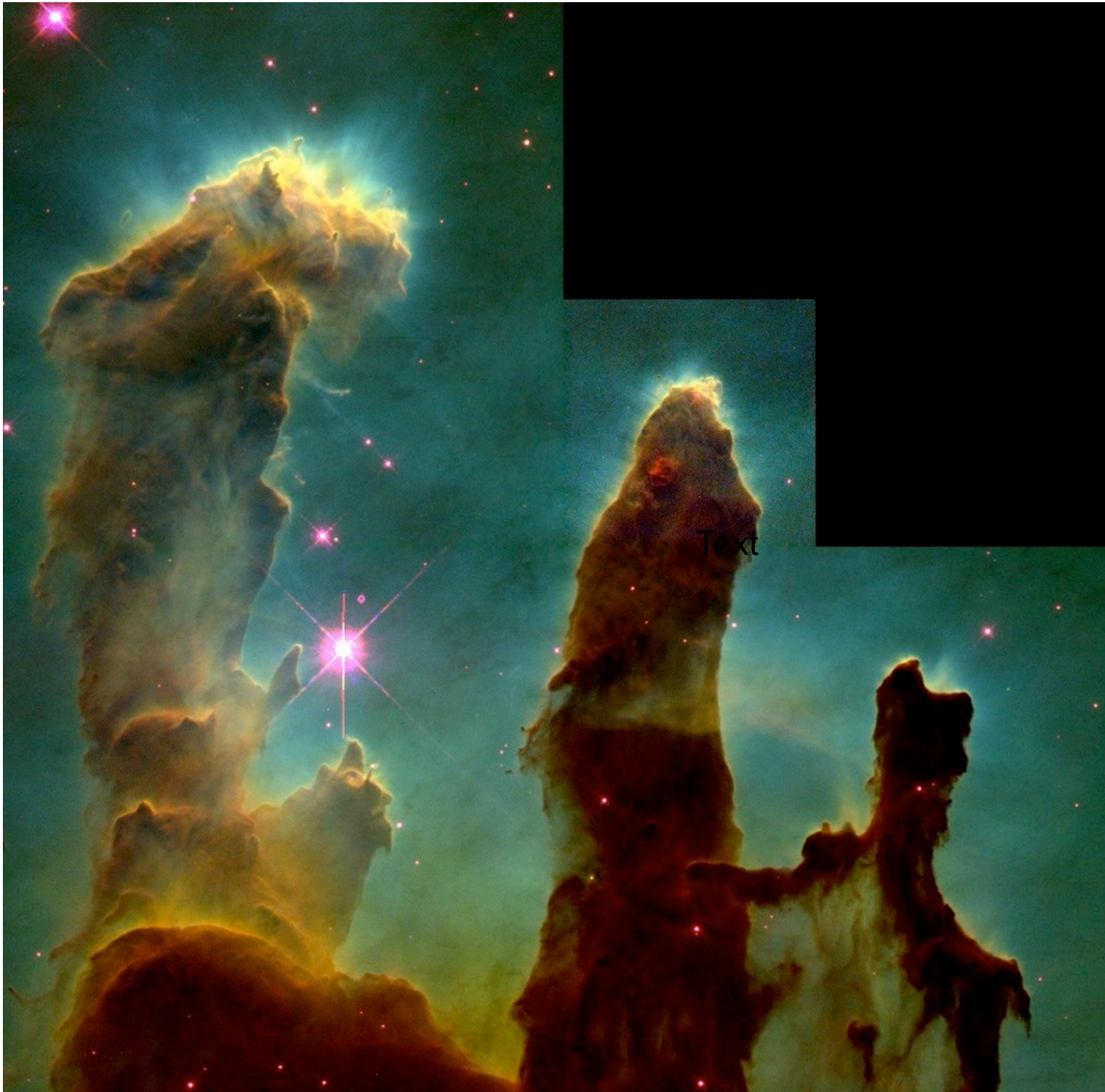


Lyman Spitzer's Legacy of Innovation in the Quest for Fusion Energy

- Some history of Spitzer's big ideas / innovations:
 - 1946: Telescopes in space (Hubble Space Telescope)
 - 1951: Figure-8 stellarator trick to make a fusion power source
- A fluid picture of the trick for how a figure-8 stellarator works (and basis for later stellarators).
- Continuing innovations at PPPL and elsewhere to improve fusion energy concepts
 - including ideas for further improving the stellarator concept, which is undergoing a renaissance.



- December 10, 1993: Space Shuttle fixed Hubble Space Telescope optics.
- <http://www.nytimes.com/1993/12/11/us/shuttle-releases-hubble-telescope.html>



The Eagle Nebula:
“Pillars of Creation”
gas pillars in a star-
forming region.

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