

Surface Waves and Landau Resonant Heating in Unmagnetized Bounded Plasmas

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Kevin J. Bowers, Ph.D.*

This research conducted while in the:
Plasma Theory and Simulation Group
Electrical Engineering and Computer Science Department
University of California, Berkeley

* Presently at D. E. Shaw Research and Development
120 West 45th St, New York, NY, 10036

Outline

- Introduction
 - Basic mechanisms, Homogeneous Model, Two Approaches
- Surface Waves
 - Cold Slab Model, Warm Non-Uniform Model, Modeling Results, Simulation Results
- Landau Resonant Heating
 - Observations, Traveling Wave, Standing Wave, Resonant Enhancement, Simulations
- Conclusion
 - Acknowledgments

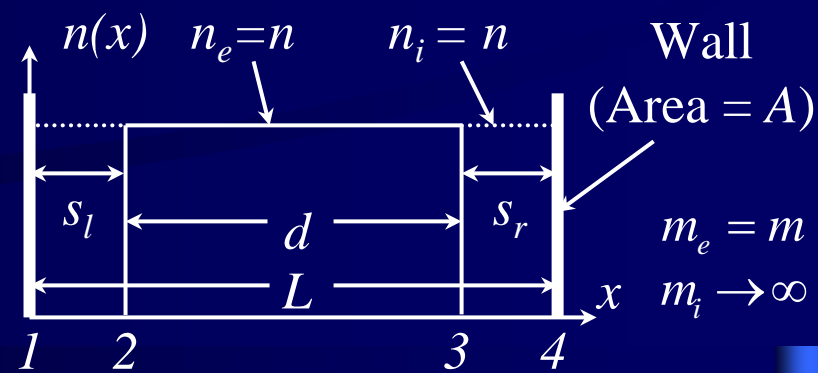
Introduction

- Understanding the plasma-wall interaction is critical in laboratory and industrial plasmas
- Large area plasmas pose difficult modeling, simulation and experimental problems.
- Surface Waves and Landau Resonant Heating can be exploited to generate plasmas with desirable properties:
 - Uniformity, low temperature, enhanced reactions

Mechanisms and Properties

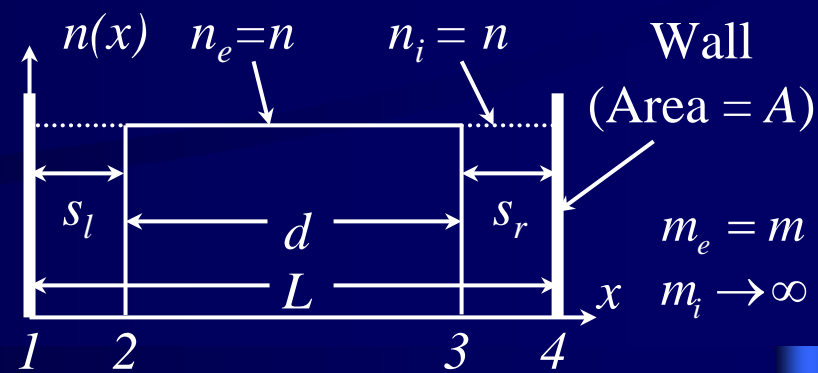
- Plasma Non-Uniformity
 - Capacitive sheaths, “Inductive” bulk (from e^- inertia)
 - Waves propagate near or below ω_{pe}
 - Strongest fields near plasma sheaths
- (Mostly) Longitudinal Waves
 - Waves exchange energy between e^- inertia and electric field
 - Waves of interest have slow group velocities, $v_{gr} \sim v_{th}$, and slow phase velocities, $v_{ph} \ll c$ (usually)
 - Compression of plasma: thermal effects - Bohm-Gross dispersion and Tonks-Dattner modes
- Wave-Particle Interactions
 - Wave fields suitable for trapping particles moving synchronously with the wave; Landau damping

Homogeneous Model



- Models the effects of space charge sheaths
 - Assume stationary uniform ions
 - Electrons are trapped in center of the plasma
 - Invoking quasi-neutrality, the bulk electron density is the same as the ion density
- Electron depleted sheaths at walls are ubiquitous in unmagnetized low temperature plasmas
 - Electrons mobility is far greater than ion mobility
- What is the relationship between the applied voltage and the device current?

Physical Viewpoint



- From Poisson's equation, the electric field in the bulk (E_p) is constant in space
 - Ignoring thermal effects, e⁻'s move as a rigid slab

- Newton:
$$\frac{d^2}{dt^2} \tilde{s}_l = -\frac{e}{m} \tilde{E}_p - \nu_m \frac{d}{dt} \tilde{s}_l$$
- Poisson:
$$\tilde{E}_p(t) = \frac{1}{L} \tilde{V}_{14}(t) - \frac{2en\bar{s}}{\epsilon_0 L} \tilde{s}_l(t)$$
- Damped SHO:
$$\frac{d^2}{dt^2} \tilde{s}_l + \nu_m \frac{d}{dt} \tilde{s}_l + \frac{2\bar{s}}{L} \omega_{pe}^2 \tilde{s}_l = -\frac{e}{mL} \tilde{V}_{14}$$
- Total Current:
$$\tilde{I}(t) = -enA \frac{d}{dt} \tilde{s}_l + \epsilon_0 A \frac{d}{dt} \tilde{E}_p$$

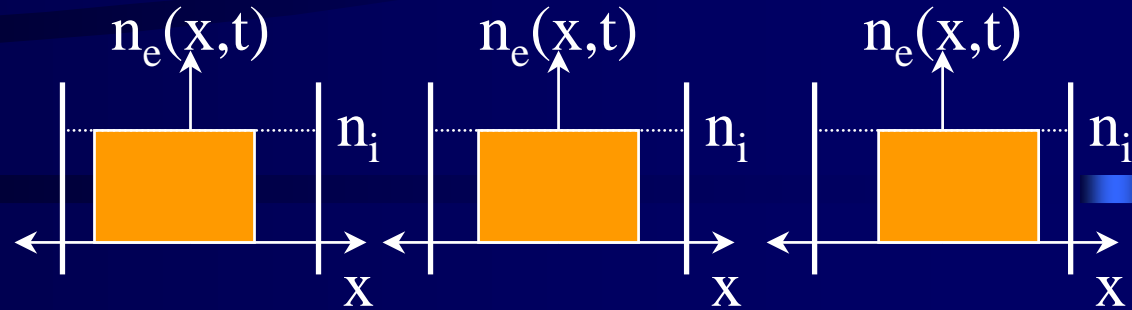
Governing Equation:

$$\frac{d^2}{dt^2} \tilde{I} + \nu_m \frac{d}{dt} \tilde{I} + \frac{2\bar{s}}{L} \omega_{pe}^2 \tilde{I} = \frac{\epsilon_0 A}{L} \left(\frac{d^3}{dt^3} \tilde{V}_{14} + \nu_m \frac{d^2}{dt^2} \tilde{V}_{14} + \omega_{pe}^2 \frac{d}{dt} \tilde{V}_{14} \right)$$

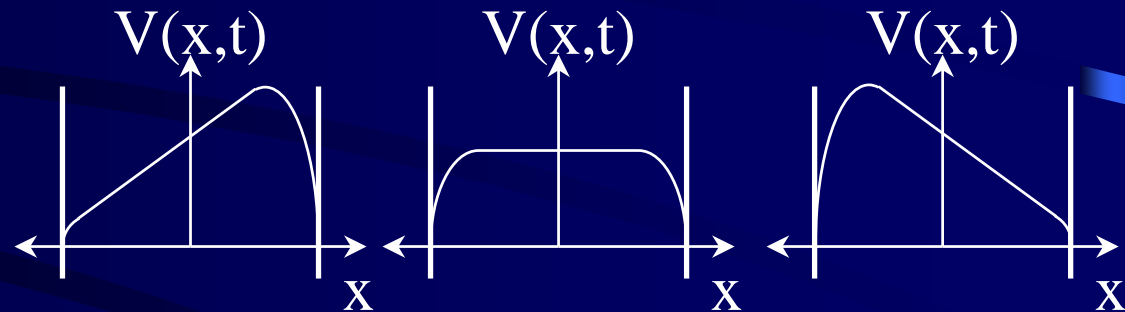
At the Series Resonance

- RF voltage drop across bulk plasma cancels sheath voltage drop
- Displacement current through bulk not negligible

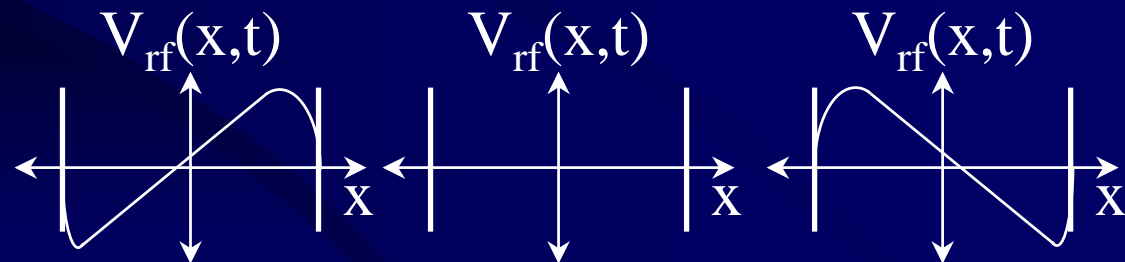
Bulk plasma sashes



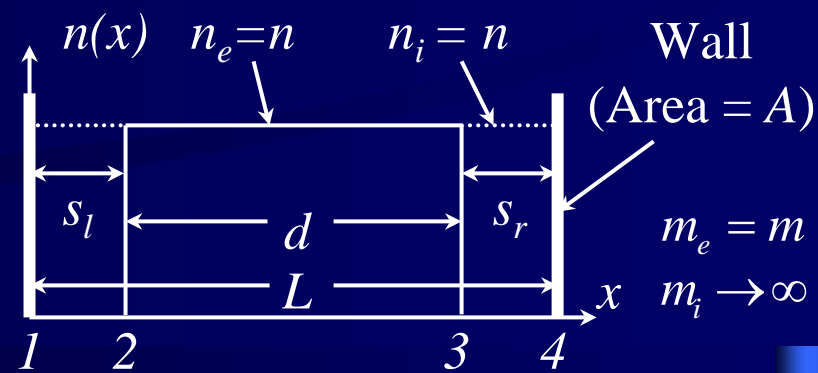
Instantaneous Potential



RF Potential



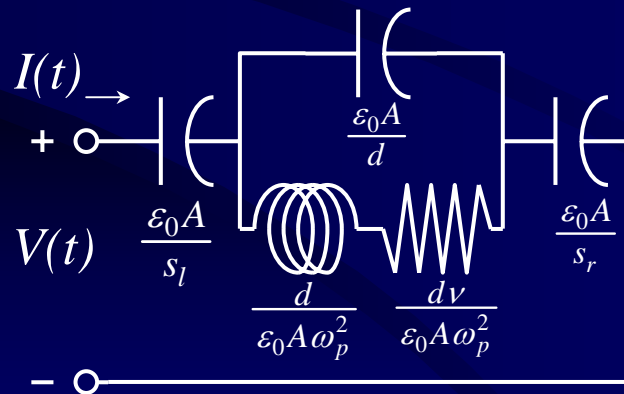
Circuit Viewpoint



- In the plasma bulk: $\epsilon_p = \epsilon_0 \left(1 - \frac{\omega_{pe}^2}{\omega(\omega - j\nu_m)} \right)$
- Three capacitors in series:

$$Z(\omega) = \frac{\tilde{V}_{14}(\omega)}{\tilde{I}(\omega)} = \frac{s_l + s_r}{j\omega\epsilon_0 A} + \frac{d}{j\omega\epsilon_0 A \left(1 - \frac{\omega_{pe}^2}{\omega(\omega - j\nu_m)} \right)} = \frac{L}{j\omega\epsilon_0 A} \left(\frac{\frac{2\bar{s}}{L} \omega_{pe}^2 - \omega^2 + j\nu_m \omega}{\omega_{pe}^2 - \omega^2 + j\nu_m \omega} \right)$$

- High frequency equivalent circuit:



What We Learned

- A bounded plasma slab has a natural oscillation frequency for sloshing motion
 - Series resonance: $\omega_{sr} = \omega_{pe}(2s/L)^{1/2}$
- Near the series resonance the $Z(\omega)$ is resistive
- Treating the plasma as a stationary dielectric medium implicitly accounts for e^- motion
 - Calculations are easier from the circuit point-of-view but physical point-of-view has more insight

Surface Waves

A Simple Model and Asymptotes

A Better Model

Modeling Results

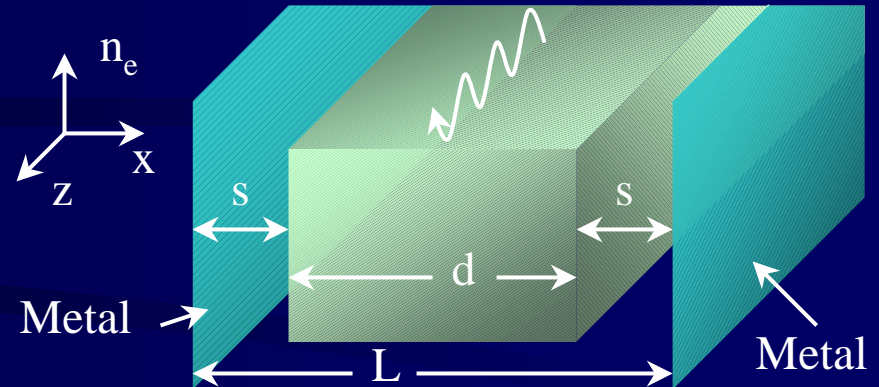
Theoretical Discussion

Electrostatic Simulation Results

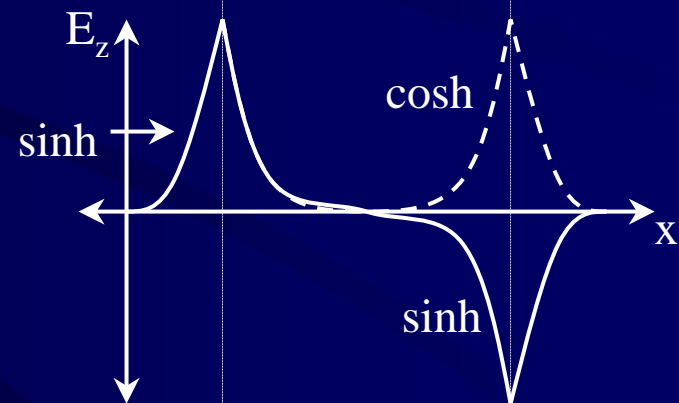
Electromagnetic Simulation Results

A Simple Model

- Treat as a dielectric loaded waveguide
 - Cold homogeneous bulk plasma
 - Vacuum sheaths
 - Longitudinal waves are TM polarized
 - Look for slow waves

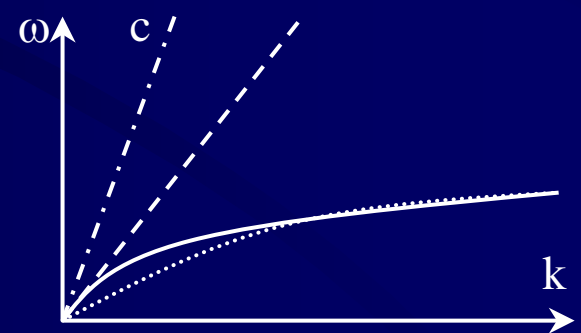
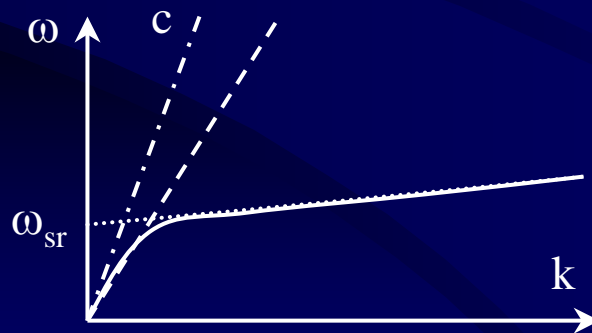


Mode Structure



Asymptotes

| | Anti-symmetric | Symmetric |
|-----------------------|--|--|
| Small k | $\omega = kc / \sqrt{1 + \frac{c}{s\omega_{pe}} \tanh \frac{\omega_{pe}d}{2c}}$ | $\omega = kc / \sqrt{1 + \frac{c}{s\omega_{pe}} \coth \frac{\omega_{pe}d}{2c}}$ |
| Large k | $\omega^2 = \omega_{pe}^2 / 2$ | $\omega^2 = \omega_{pe}^2 / 2$ |
| Large k (thermal) | $\omega^2 = \omega_{pe}^2 / 2 + 3v_e^2 / 2$ | $\omega^2 = \omega_{pe}^2 / 2 + 3v_e^2 / 2$ |
| Electrostatic | $\omega^2 = \omega_{pe}^2 \left(\frac{\coth kd / 2}{\coth ks + \tanh kd / 2} \right)$ | $\omega^2 = \omega_{pe}^2 \left(\frac{\tanh kd / 2}{\coth ks + \tanh kd / 2} \right)$ |
| Electrostatic small k | $\omega^2 = \frac{2s}{L} \omega_{pe}^2 = \omega_{sr}^2$ | $\omega = k \sqrt{sd \omega_{pe}^2 / 2}$ |



A Better Model

$$\hat{\epsilon}_p = 1 - \frac{\omega_{pe}^2 f}{\omega(\omega - j\nu_m)} + \frac{\gamma_e v_{te}^2}{\omega(\omega - j\nu_m)} \nabla(\nabla \cdot []) - \frac{v_{te}^2}{\omega(\omega - j\nu_m)} (\nabla \ln f)(\nabla \cdot [])$$

Cold Plasma Dielectric

e⁻ Pressure

Non-Uniformity

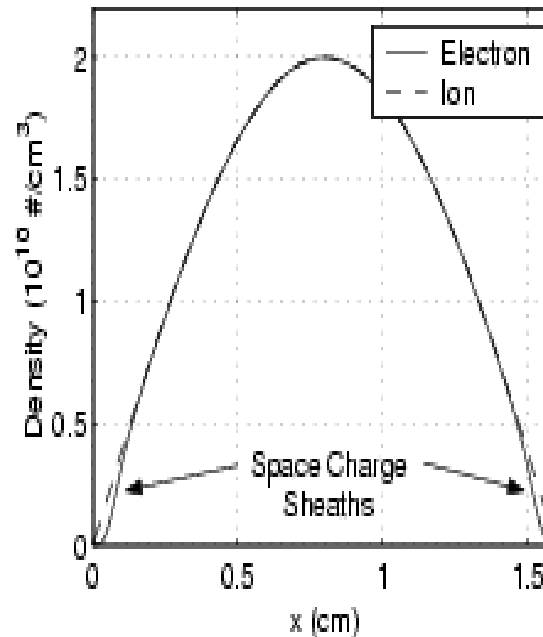
- **Warm Non-Uniform Plasma Model**

- Linearized fluid theory. Uniform temperature. Ideal equation of state. Stationary ions. Model is expressed as a dielectric operator above.
- Model first used to explain Tonks-Dattner resonances by Parker, Nickel and Gould (1964).
- Captures thermal effects but not wave-particle effects.
- Prior works were electrostatic and only could solve for plasmas a few tens of Debye lengths long
- The thermal terms avoid singularities where the wave frequency matches local plasma frequency

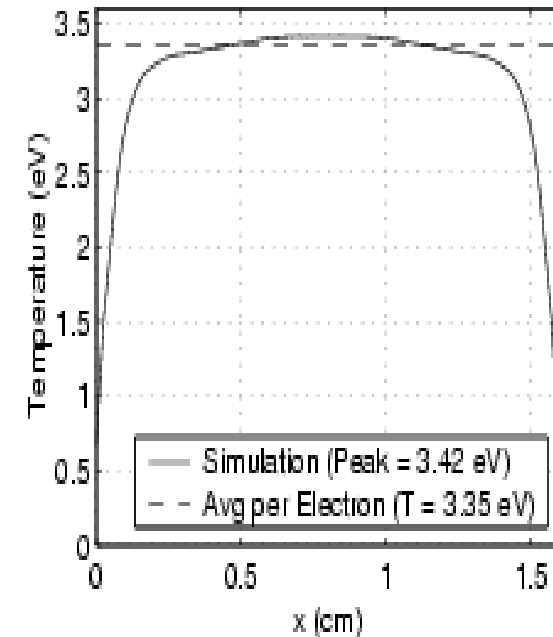
Modeling Results

- This profile is used for the results to follow
- Profile was obtained from an XPDP1 simulation of Tonks-Dattner resonances

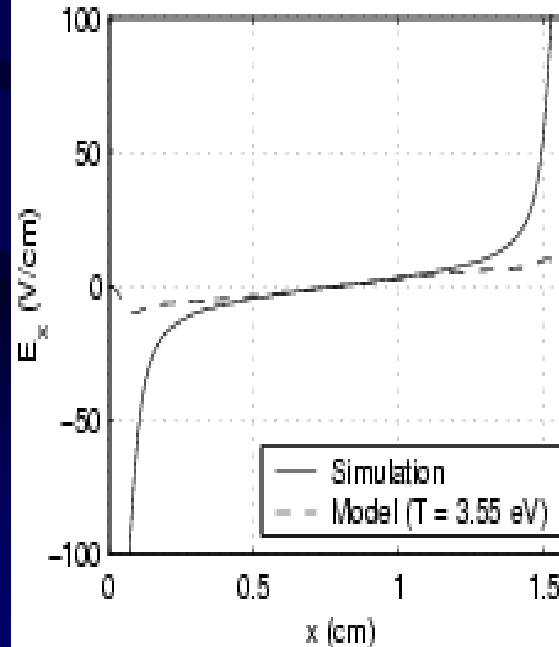
(a) Cycle-Averaged Density



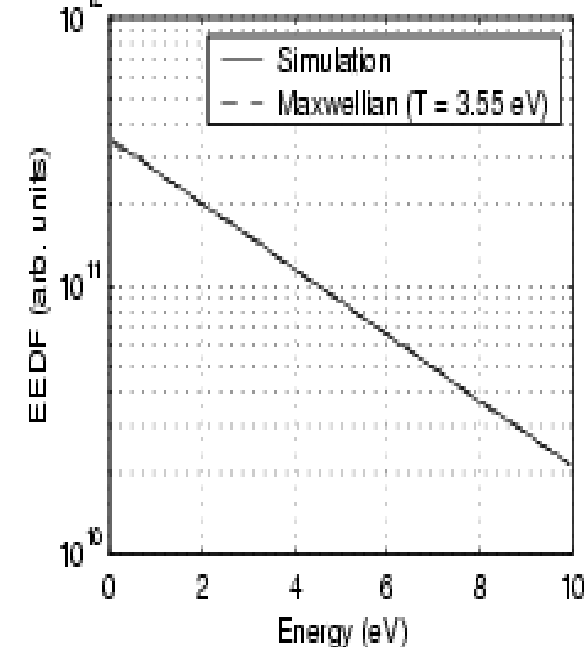
(b) x-Directed Random Energy



(c) Cycle-Averaged x-Directed Electric Field

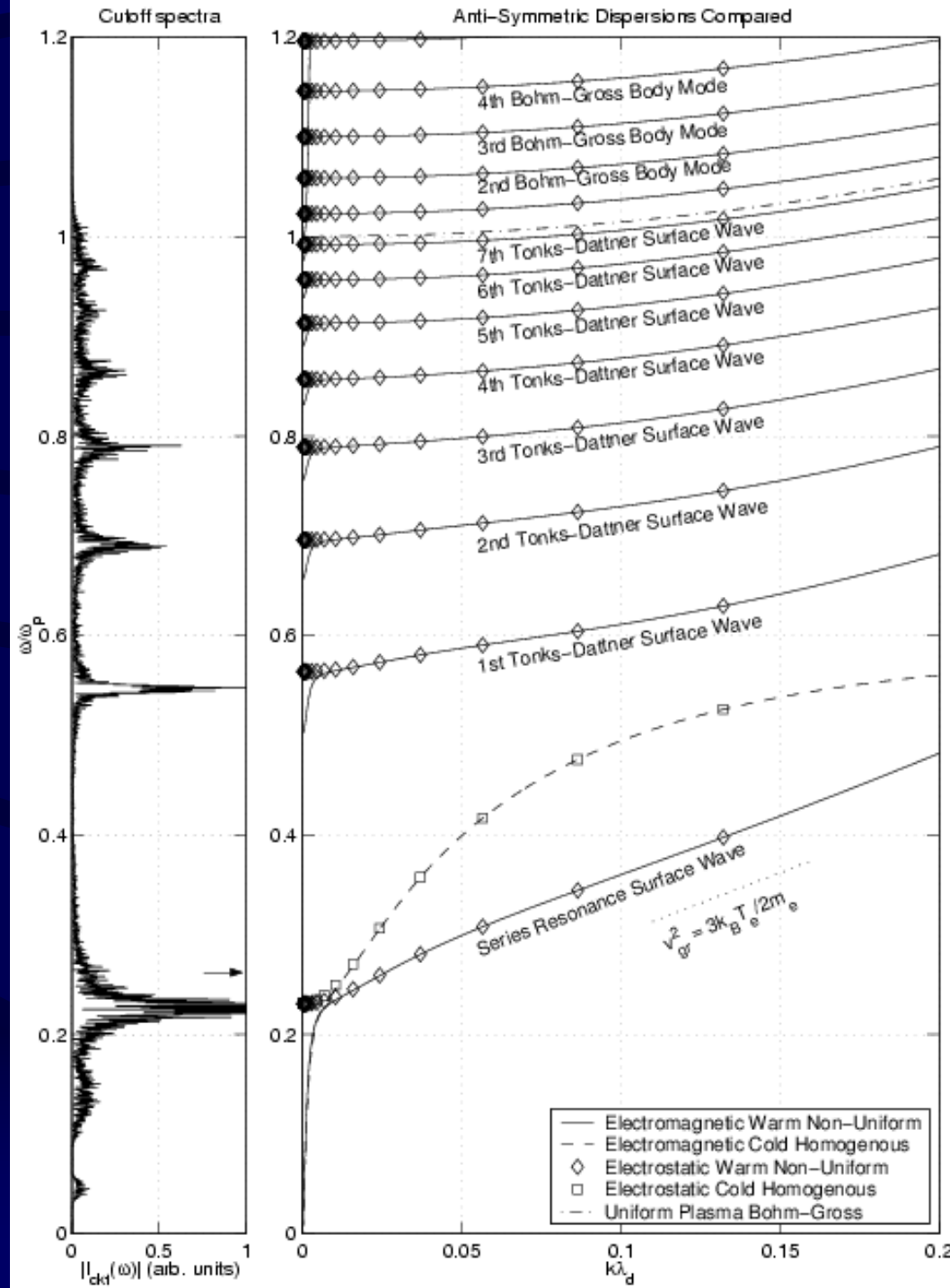


(d) Energy Distribution Function at Midplane



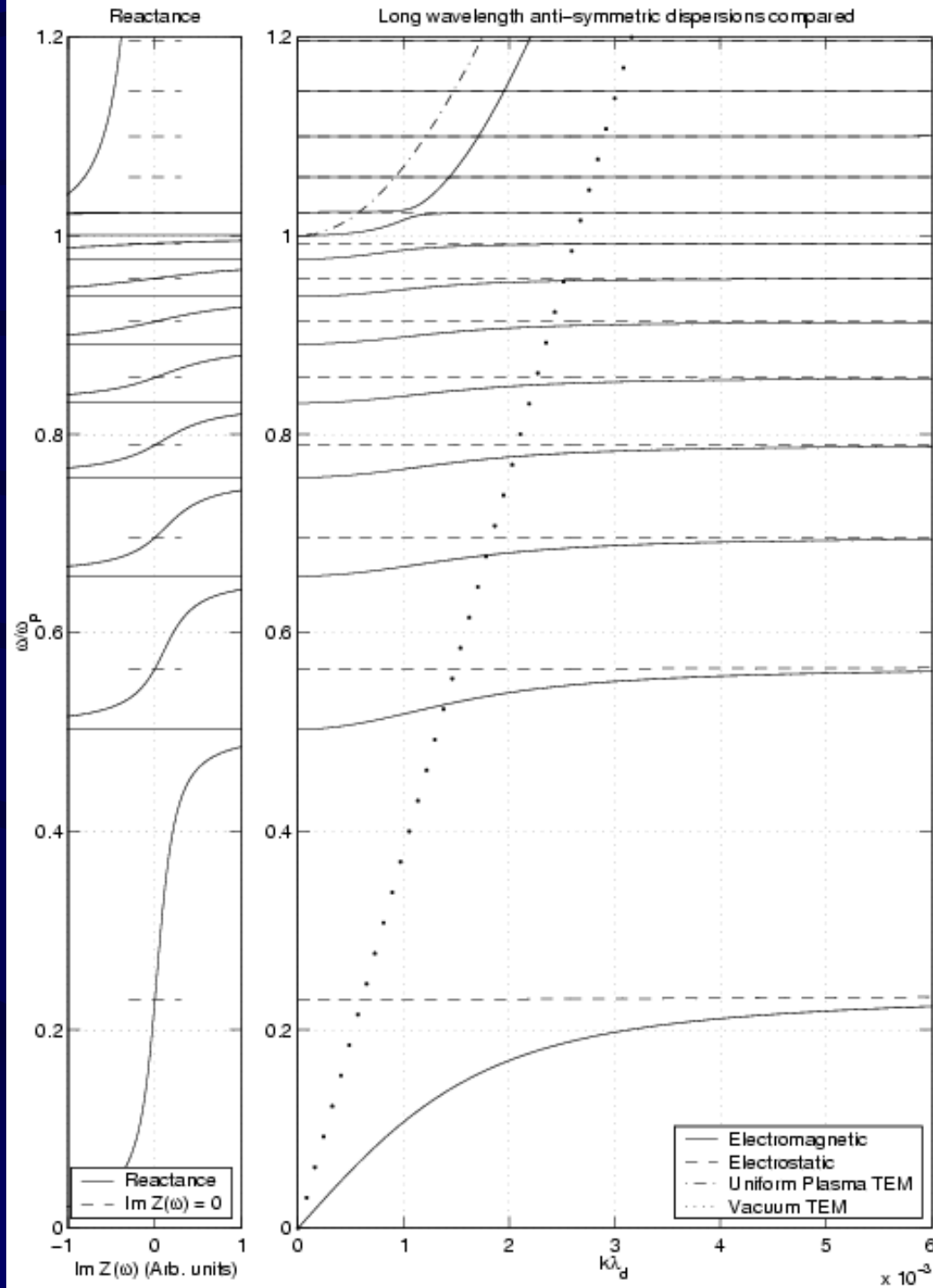
Anti-symmetric Results

- Cutoffs are Tonks-Dattner resonances
 - Agree within 5%
 - Series resonance wave very accurate
- “Knee” in the electromagnetic dispersion
- Bohm-Gross modes
 - Heavily Landau damped in the sim but not in the model



Closeup of “Knee”

- Only anti-symmetric modes exhibit this behavior
- Electromagnetic cutoffs are at poles in slab impedance
- Electrostatic cutoffs are at zeros

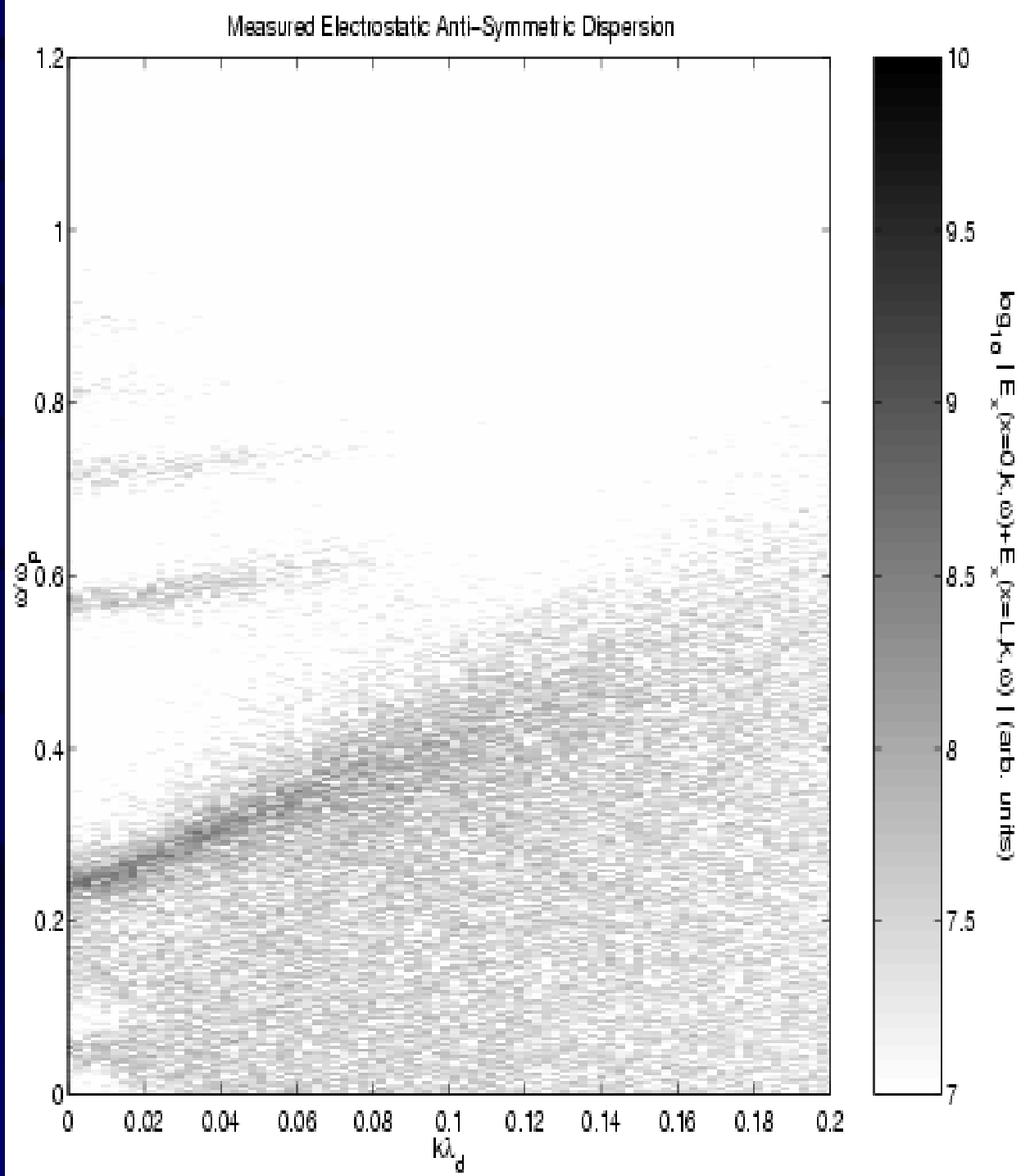


Discussion

- “Knee” was unexpected
 - Mathematically, knee is necessary to keep the magnetic field finite when no surface charges are added to the walls by plasma or external circuits (hence cutoffs at device Z poles).
 - Electrostatic model has no magnetic field, so there is no knee.
 - Electromagnetic model distinguishes between natural modes and modes driven by an external circuit (driven modes act similar to electrostatic model).
 - Theoretically, due to how charge continuity enforced.
 - Wave modes become TEM-like near knee.
- 1st Principles PIC Simulations confirm the “Knee”
 - 2d3v EM-PIC simulation of ~1 meter of plasma loaded parallel plate waveguide (tens of million of particles for tens of thousands of steps on home comp 6 yrs ago)
 - FDTD-EM solver that eliminates mesh Courant condition and damps transverse radiation PIC noise without altering charge conservation properties developed (~150X faster)
 - Cache optimal PIC techniques also developed (~1.5-2X faster)

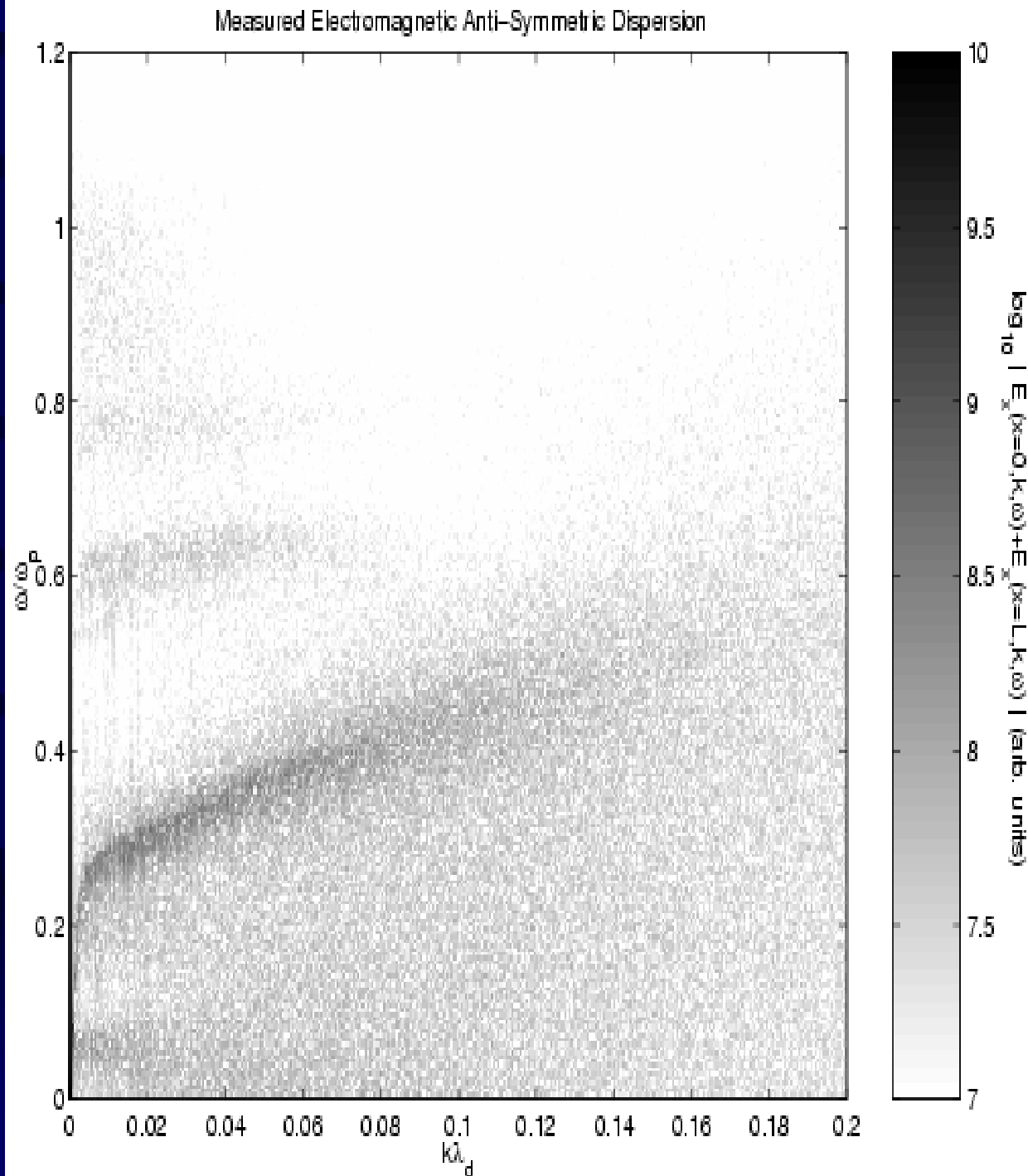
ES Simulation

- Series resonant surface wave and Tonks-Dattner surface waves visible



EM Simulation

- Knee clearly visible
- Simulation would not be feasible without implicit FDTD EM solver



Landau Resonant Heating

Early Observations

Overview

Traveling Waves

Standing Waves

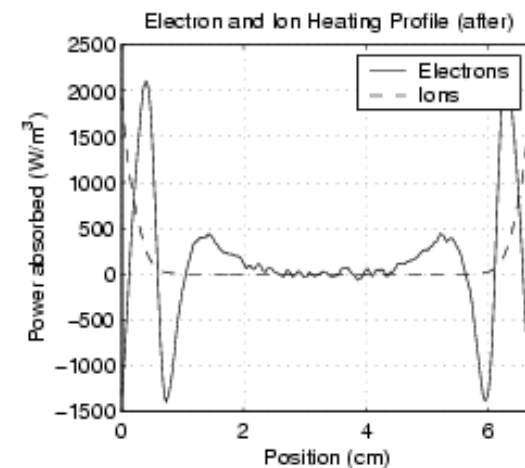
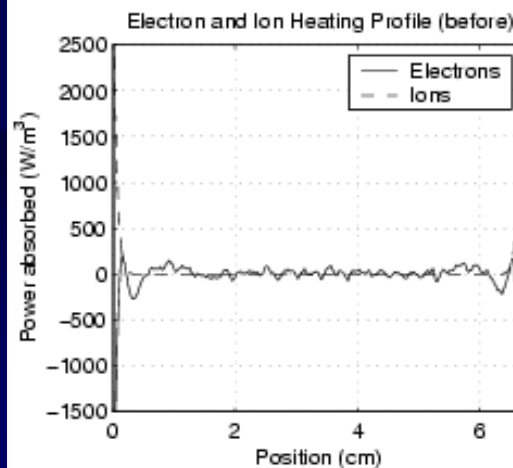
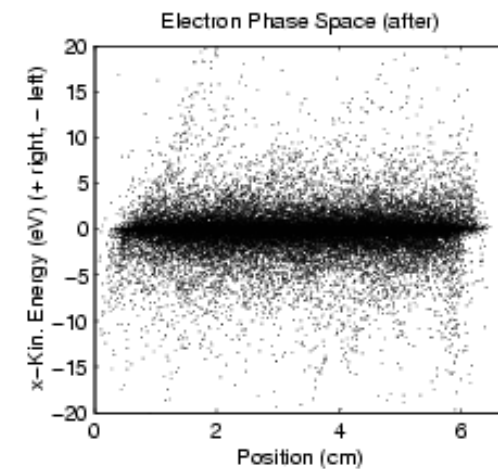
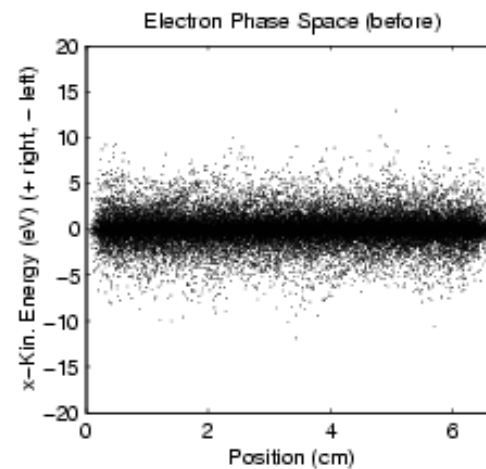
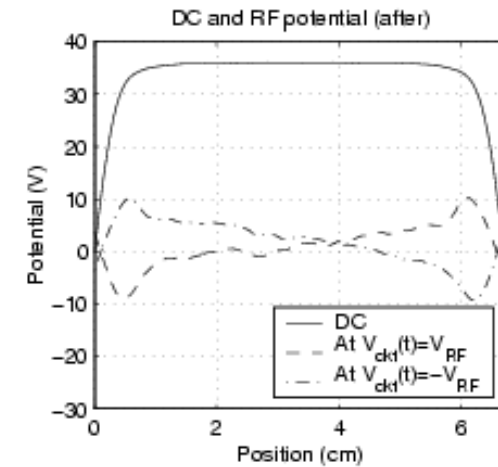
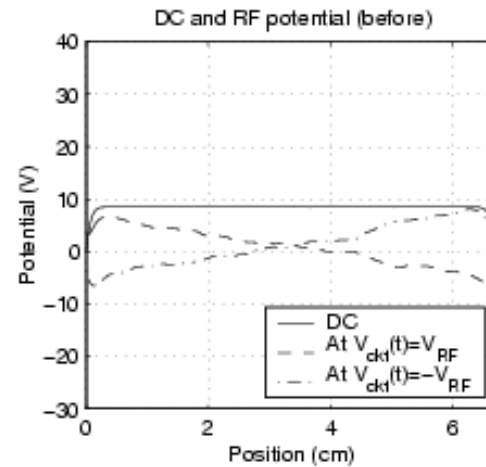
Reaction Enhancement

Bohm-Gross Demonstration

Surface Wave Demonstration

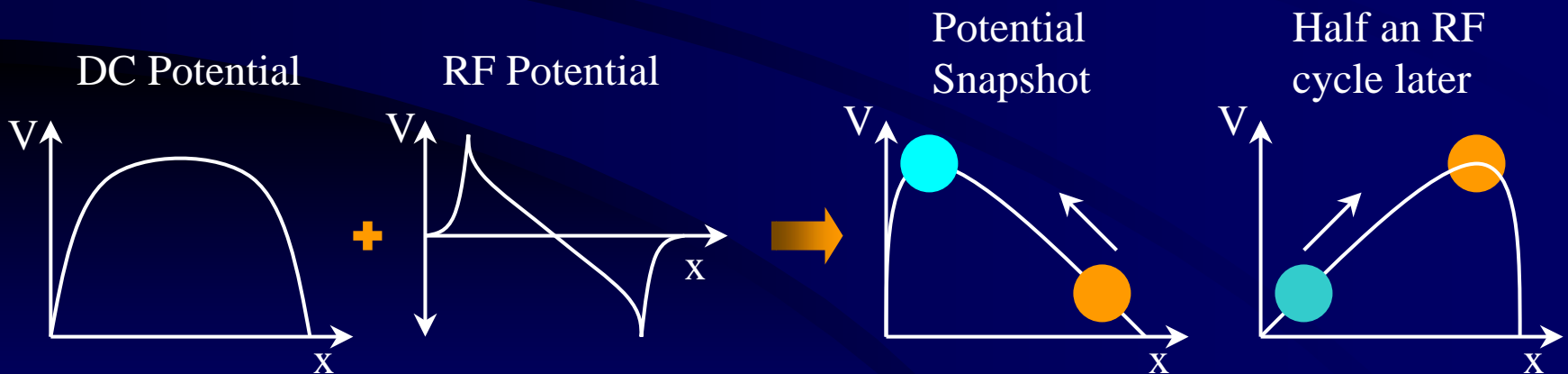
Resonant Discharge

- Unique Heating Mechanisms Observed in Simulations of Discharges Sustained at Cutoff of the Series Resonant Surface Wave Mode



Phase Space Bunching

- Mode potential interacts with the DC potential to form bunches of electrons.
- Half an RF cycle later, bunches are accelerated out of the sheaths
- What other heating mechanisms could surface waves exploit ...

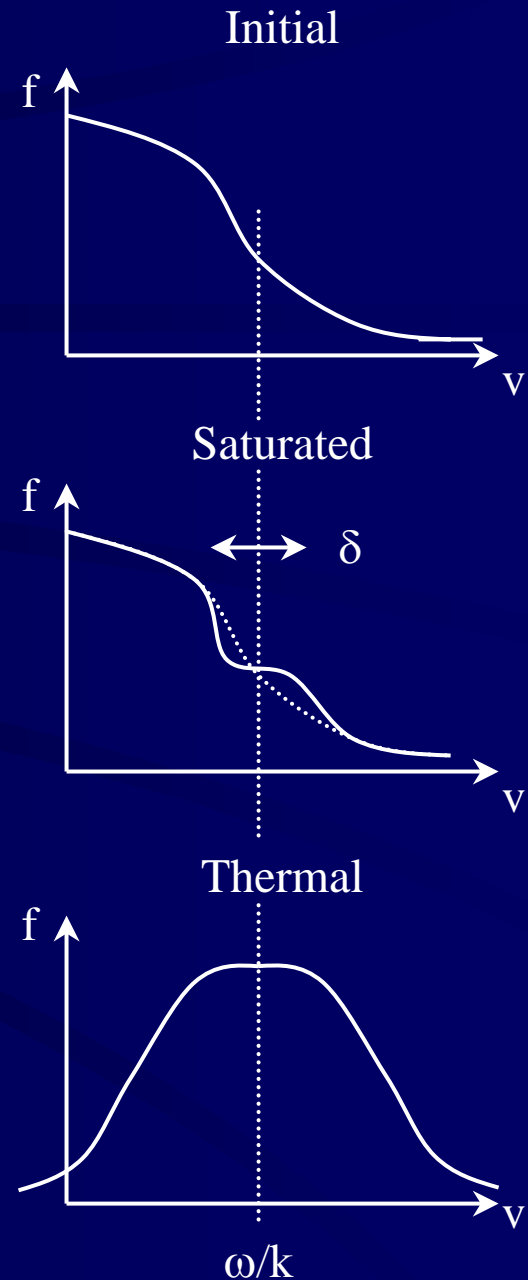


Landau Damping Overview

- Predicts that for monotonically decreasing EEDFs, a slow longitudinal wave will be damped from wave-particle interaction
 - Particles moving just below (accelerated) the wave phase velocity gain (lose) energy.
 - In linear stage, damping is exponential
 - In non-linear stage, particles trapped in wave potential wells phase mix (interesting ...)

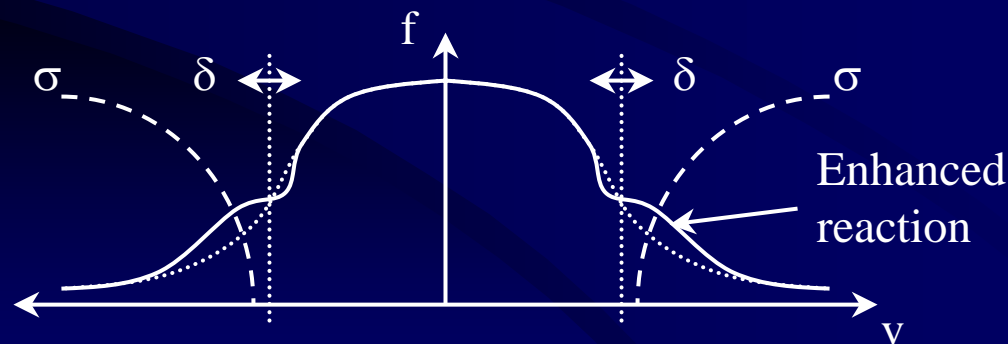
Landau Heating - Driven Traveling Wave

- If a wave is applied such that it does not damp, a non-thermal quasi-equilibrium will be established
- Saturated state reached after several Landau bounce times
 - Bounce time: $\tau = \sqrt{4\pi^2 m_e / ek^2 V_0}$
 - Plateau width: $\delta = \sqrt{16 eV_0 / m_e}$
- Thermal equilibrium usually not reached in effectively collisionless systems.



Landau Heating – Driven Standing Wave

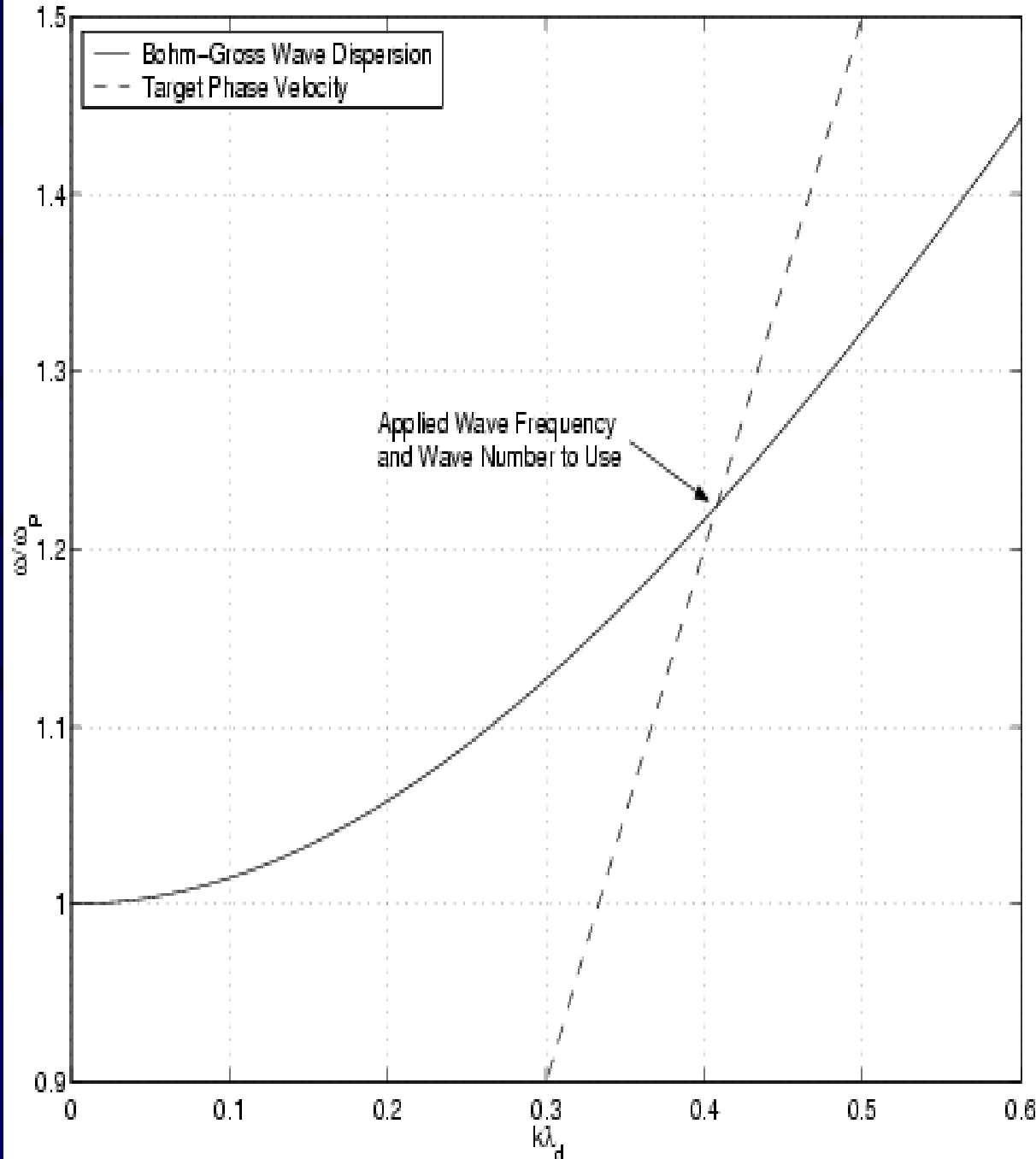
- A standing wave consists of two oppositely directed traveling waves; each wave creates a (smaller) plateau
- No thermal equilibrium; the applied wave potential is time varying in all frames
- Reactions driven by electrons in the tail of the distribution function will have the reaction rate modified
- Landau Resonant Heating: If driven wave is resonant with natural plasma waves, plateau can be enhanced



Bohm-Gross LRH Sim

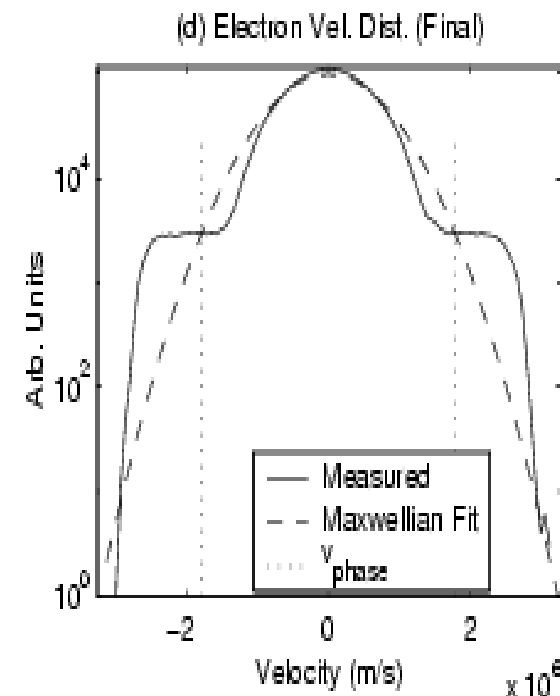
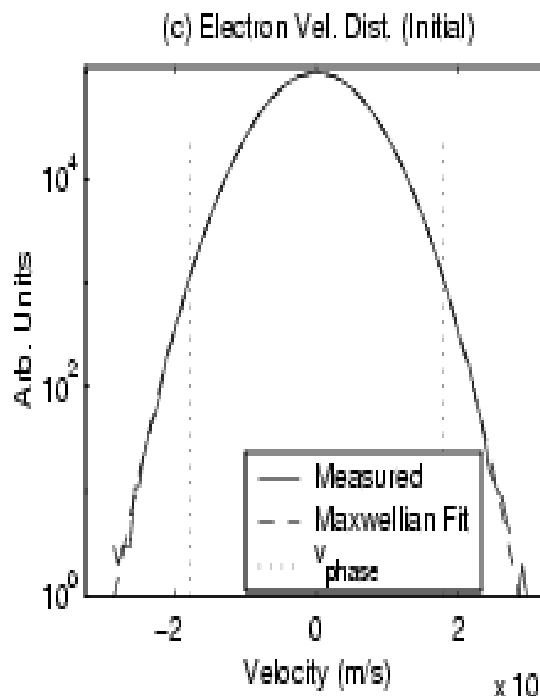
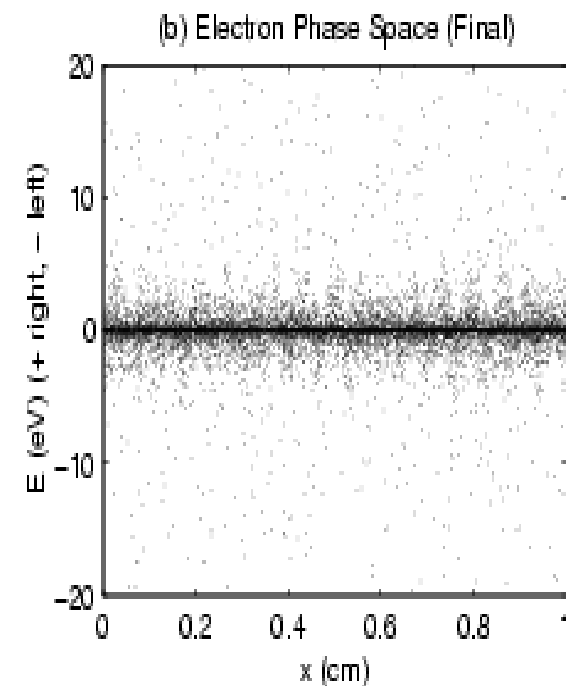
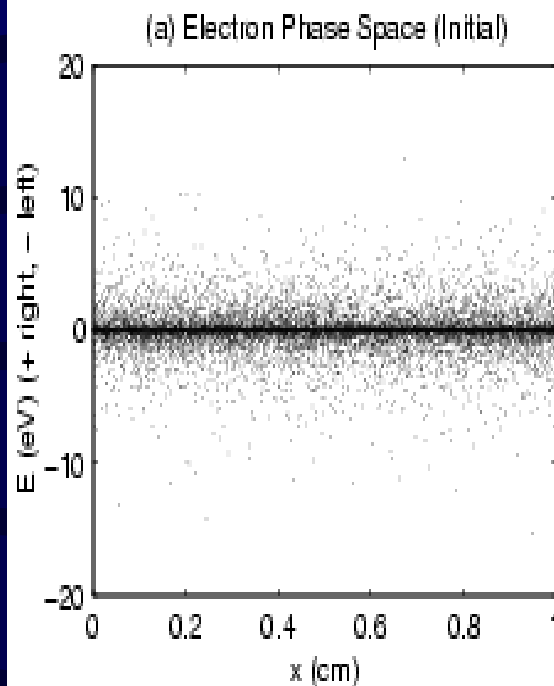
- Plasma properties
 - $n_0 = 0.745 \times 10^{11} \text{ cm}^3$
 - $T_e = 2 \text{ eV}$
- Interaction Point
 - $v = 3v_{th}$ ($E = 9T_e$)
- Wave properties
 - $f_{\text{wave}} = 3.00 \text{ GHz}$
 - $\lambda_{\text{wave}} = 0.588 \text{ mm}$
 - $V_{\text{applied}} = 0.2 \text{ V}$

Landau Resonant Interaction ($\omega/k = 3v_{th}$)



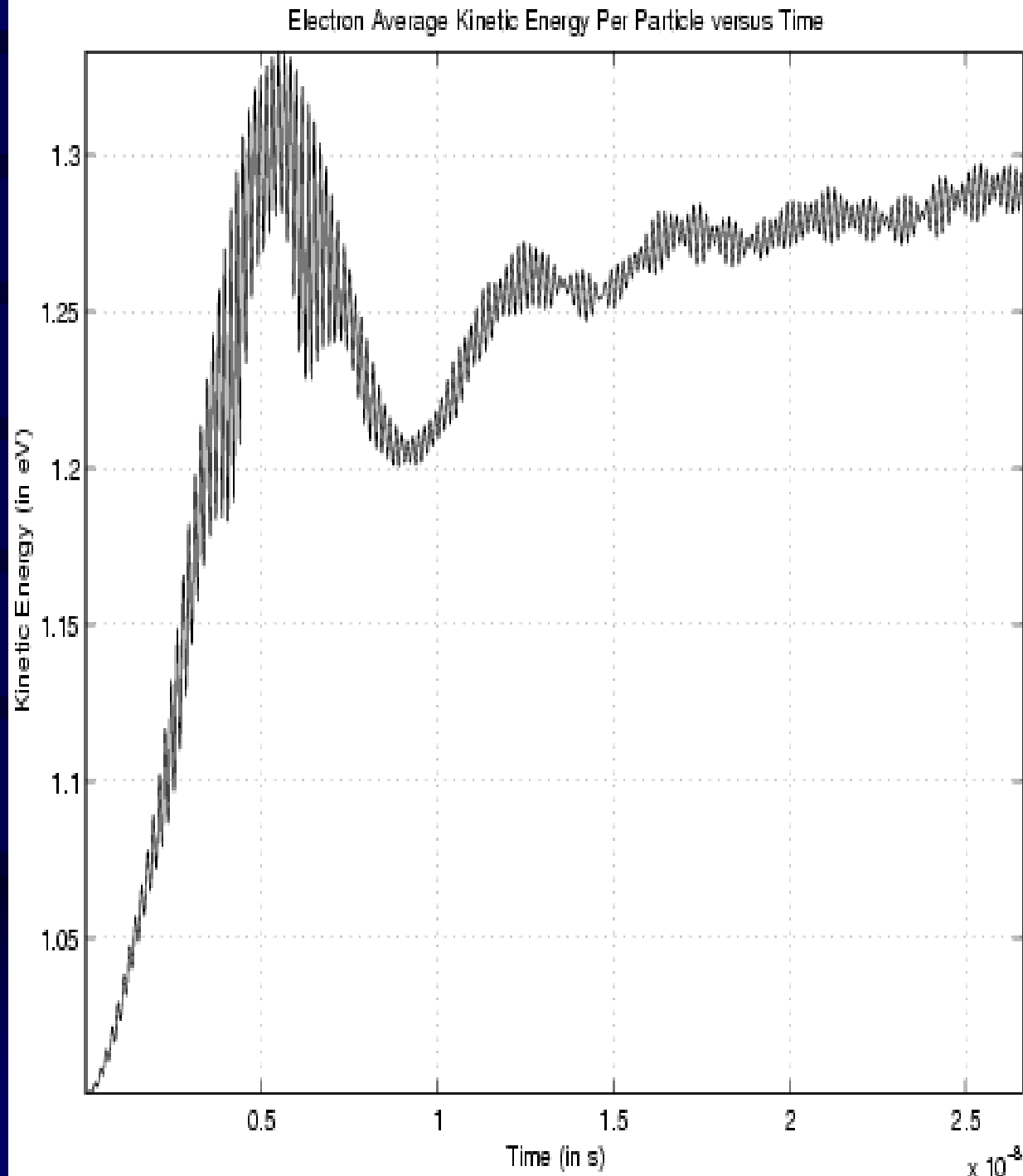
Before and After

- Nearly 100X enhancement of hot electron population at some energies
- Plateaus are much wider than the applied 0.2V



Electron Heating

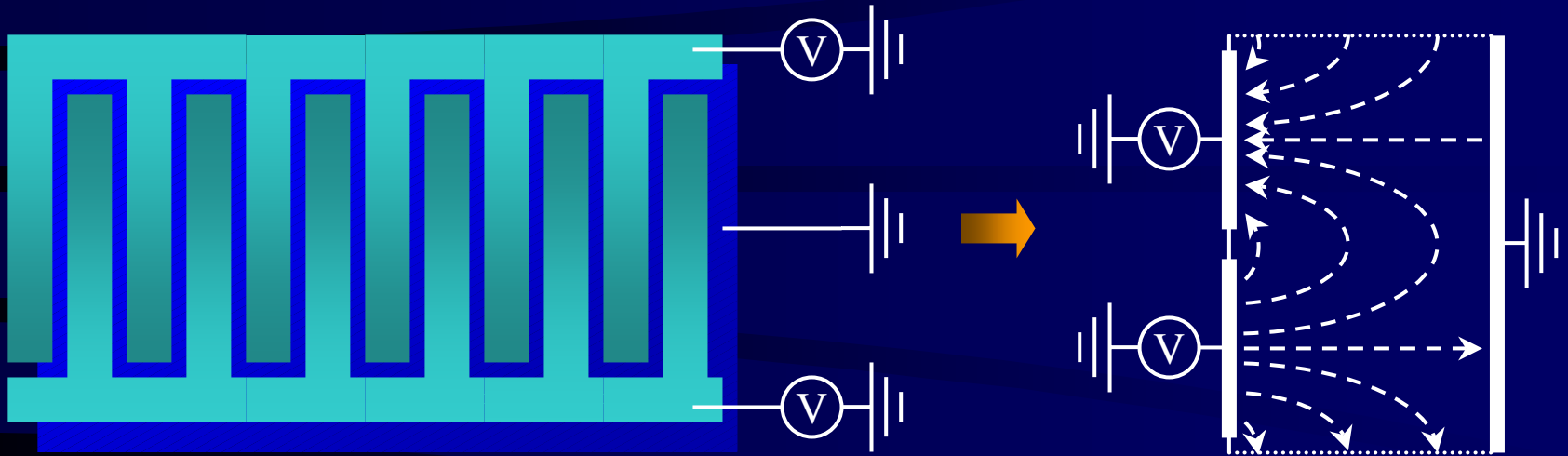
- Plateaus form and heating saturates in several hundred plasma oscillation times.



Demonstration with Series Resonant Surface Wave

- Series Resonant Surface Wave is ideal wave to use for Landau Resonant Heating in a practical device
 - Easy to excite with antennas / slow wave structures as its fields are edge concentrated
 - Mode cutoff is not dependent on thermal effects
- Goal: Enhance electron-impact ionization over a comparable non-LRH discharge
 - Background Gas: Argon ($p = 3$ mTorr, $E_{iz} = 15.76$ eV)
 - Plasma density: $\sim 10^{10}$ / cm³, width 3 cm
 - Initial electron temperature: 2eV ($\lambda_{de} = 105$ μ m)
 - Target phase velocity: $v_{ph} = (2E_{iz}/m_e)^{1/2} = 2.35 \times 10^6$ m/s
 - Electrode: $f = 315$ MHz, $\lambda = 0.75$ cm, $V_{applied} = 10$ V

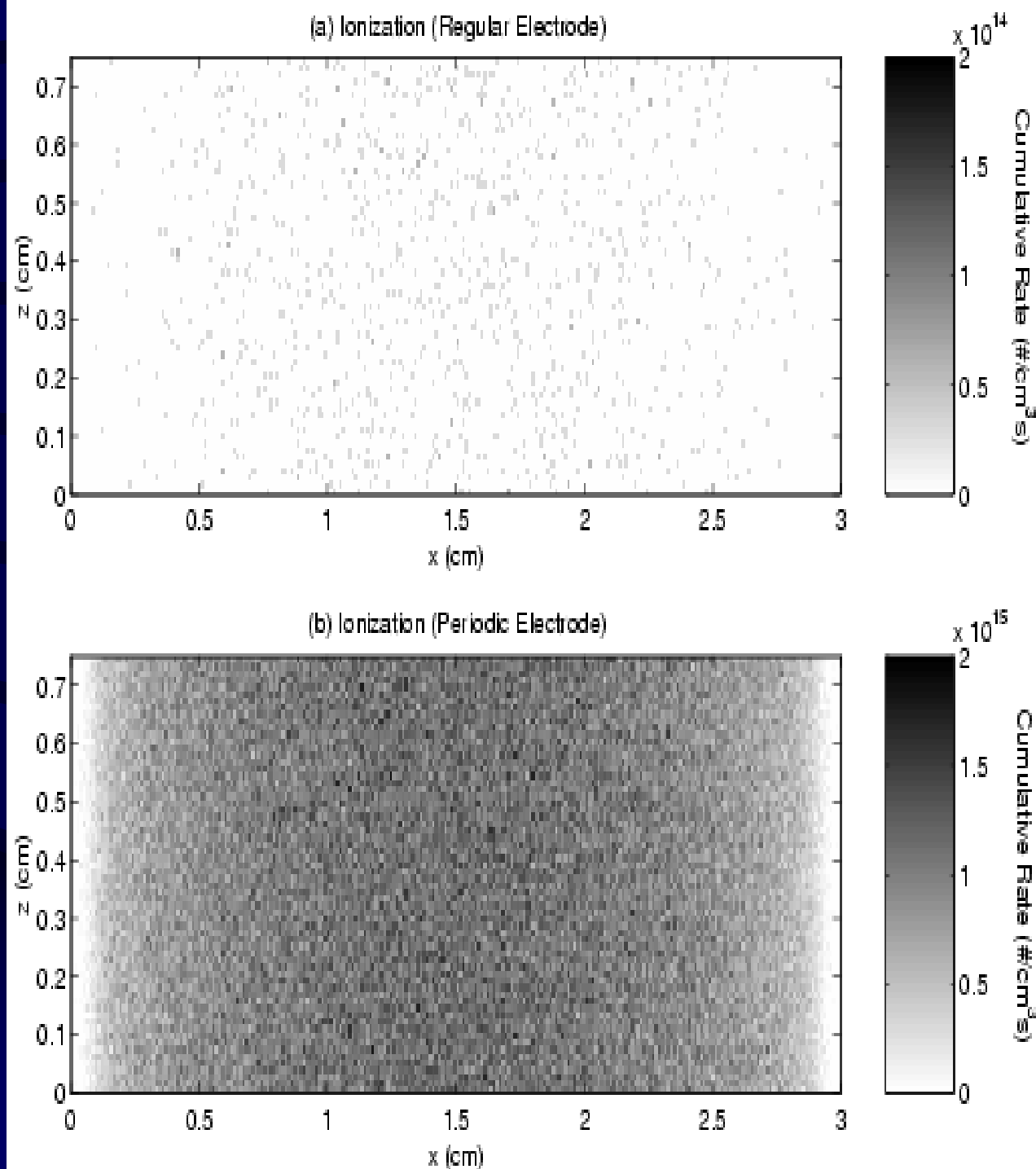
Device and Simulation Model



- 2d3v PIC-MCC simulation
 - Monte-Carlo collision package for atomic physics
- Non-LRH simulation operates structure at 0° phase difference between teeth (that is, a parallel plate capacitive discharge).
- LRH simulation operates structure at 180° phase difference between teeth.

Results

- Non-LRH simulation quickly extinguishes due to lack of ionization
- LRH simulation heats rapidly and is sustained



Conclusions

- Natural electromagnetic surface waves exhibit new phenomenology at long wavelengths (“knee”)
- Landau Resonant Heating permits the manipulation of the particle velocity space distribution functions.
- Surface waves may be used in conjunction with Landau Resonant Heating to manipulate the electron velocity space distribution function in order to modify electron reaction rates

Acknowledgments

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