

Gyrokinetic predictions of momentum and impurity transport in NSTX

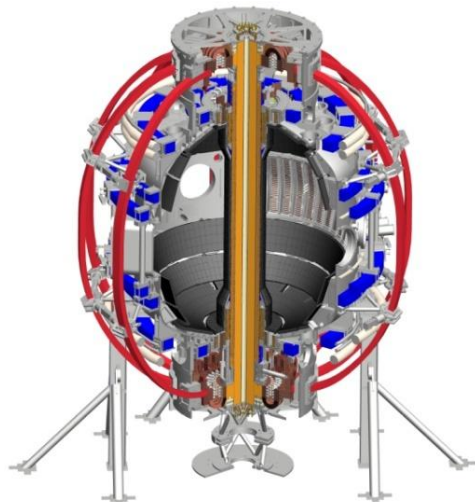
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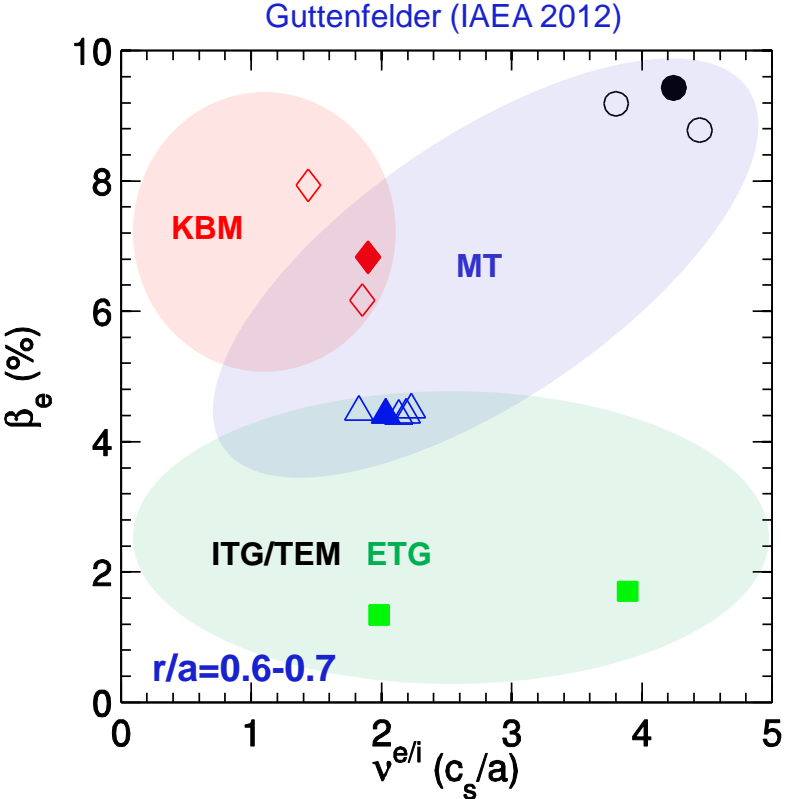
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Broad range of parameters in NSTX requires consideration of many micro-instabilities

- All of them of interest for electron thermal transport
 - Only ion scale ballooning instabilities (ITG, TEM, KBM) expected to transport momentum and impurity
- ⇒ Investigate multiple transport channels to help constrain theory



Transport Mechanism	Transport channel affected			
	ion energy	electron energy	particle/impurity	momentum
ITG	×	×	×	×
TEM	×	×	×	×
KBM	×	×	×	×
MT		×		
ETG		×		

Overview

Momentum transport

- Experimental motivation
- Quasilinear predictions of $Pr = \chi_\phi / \chi_i$ and RV_ϕ / χ_ϕ
 - L-modes unstable to ITG/TEM
 - H-modes unstable to microtearing and hybrid-KBM

Impurity (carbon) transport

- Experimental motivation
- Quasilinear prediction of carbon peaking (RV_c / D_c) in H-mode

Interpretation of toroidal angular momentum transport often assumes diffusive and convective components

- Transport equation:
$$\frac{\partial}{\partial t} (n_i m_i \langle R^2 \rangle \Omega) + \nabla \cdot \Pi_\varphi = S_\Omega \rightarrow \sum_s (\dots)$$

- Assumed* transport form:
$$\Pi_\varphi = -nmR \chi_\varphi (R \nabla \Omega) + nmV_\varphi (R\Omega)$$

$$\hat{\Pi}_\varphi = \hat{\chi}_\varphi \left(\hat{u}' + \frac{RV_\varphi}{\chi_\varphi} \hat{u} \right)$$

$$\hat{u}' = \frac{-R^2 \nabla \Omega}{c_s} \quad \hat{u} = \frac{R\Omega}{c_s}$$

- Can also have residual stress Π_{RS} contributions (from up-down asymmetric flux surfaces, finite ρ_* profile effects) leading to intrinsic torque \rightarrow intrinsic rotation when $u'=u=0$
 - Perhaps less important in core with large beam torque (co-NBI in NSTX)

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Prandtl number

$$\text{Pr} = \frac{\chi_\phi}{\chi_i}$$

$$\hat{\Pi}_\phi = \hat{\chi}_\phi \left(\hat{u}' + \frac{RV_\phi}{\chi_\phi} \hat{u} \right)$$

Pinch parameter

$$\frac{RV_\phi}{\chi_\phi}$$

$$\hat{u}' = \frac{-R^2 \nabla \Omega}{c_s} \quad \hat{u} = \frac{R\Omega}{c_s}$$

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Steady state Prandtl numbers $\chi_\phi/\chi_i < 1$ for NSTX L- mode and H-mode discharges

- $Pr = \chi_\phi/\chi_i \approx 0.3-1.0$ over many radii and discharges (assumes $V_\phi=0$)

- $\chi_\phi > \chi_{\phi,NC}$ for both L and H
In L-mode $\chi_i > \chi_{i,NC}$

$$Pr = \frac{\chi_\phi}{\chi_i} \approx \frac{\chi_{\phi,turb}}{\chi_{i,turb}}$$

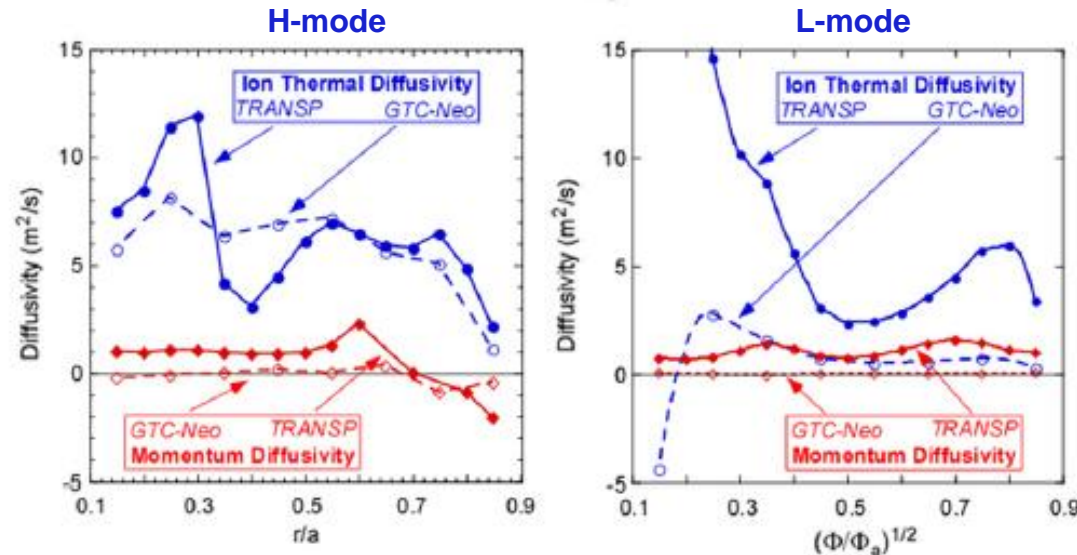
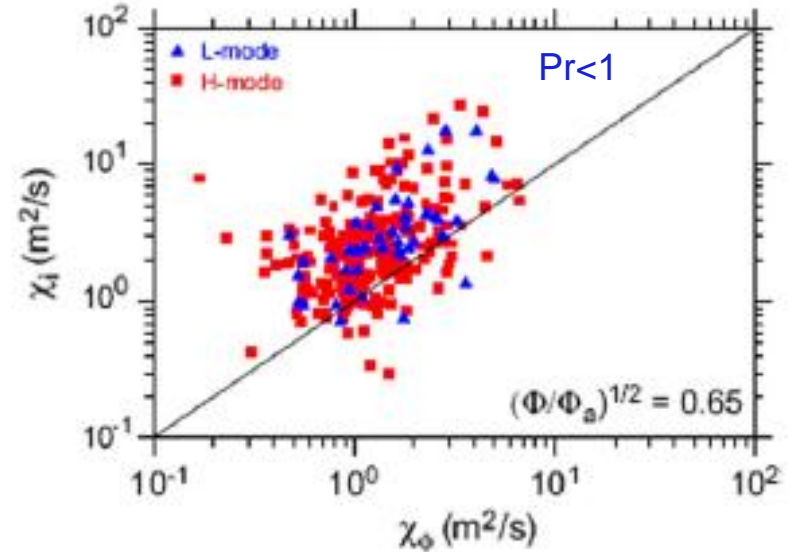
In H-mode $\chi_i \approx \chi_{i,NC}$

$$Pr = \frac{\chi_\phi}{\chi_i} = \frac{\chi_{\phi,turb}}{(\chi_{i,NC} + \chi_{i,turb})}$$

⇒ Pr ill-defined in H-mode?

- RV_ϕ/χ_ϕ less ambiguous

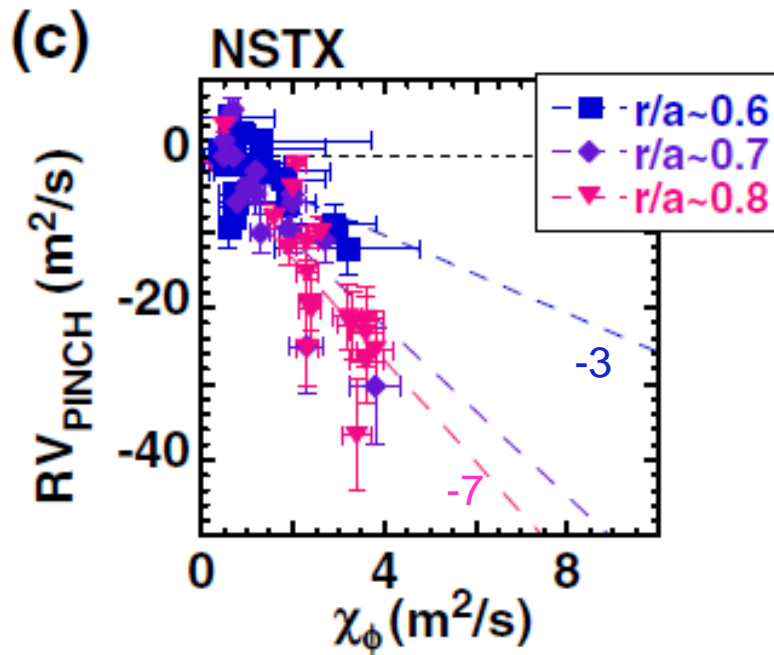
Steady state transport analysis (Kaye et al., 2009)



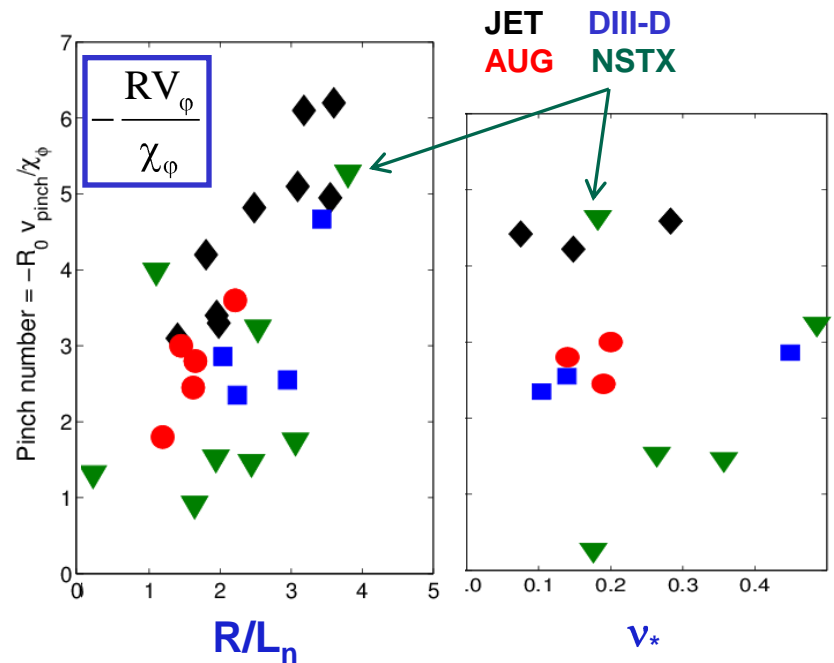
Perturbative H-mode experiments indicate existence of an inward momentum pinch

- $RV_\phi/\chi_\phi \approx -(1-7)$ for many NSTX discharges & radii
 - $Pr \sim 0.3-0.5$, smaller than other machines ($Pr \sim 0.6-2.0$) [Yoshida, NF 2012]
- Possible dependence on density gradient (R/L_n), less clear with collisionality (ν^*), but a lot of scatter

(Solomon et al., PRL 2008, PoP 2010; Yoshida et al., NF 2012)



(Tala et al., IAEA 2012)



Q: What are the relevant momentum transport mechanism(s) in NSTX?

Method for predicting quasi-linear Prandtl (χ_ϕ/χ_i) and Pinch numbers (RV_ϕ/χ_ϕ)

- Local linear GYRO simulations run between $r/a=0.6-0.8$ ($\rho_{\text{tor}}\approx 0.5-0.7$), with
 - deuterium, carbon, electrons
 - $\phi, A_{\parallel}, B_{\parallel}$
 - numerical equilibrium (EFIT/LRDFIT)
 - n_e profiles from averaged inboard/outboard measurements (no centrifugal effects in GYRO)

- Pr and RV_ϕ/χ_ϕ determined using momentum flux from different combinations of u, u'

$$\hat{\Pi}_\phi = \hat{\chi}_\phi \hat{u}' + (\hat{R}\hat{V}_\phi + \hat{R}\hat{\Gamma}_p)\hat{u} + \hat{\Pi}_{\phi,RS}$$

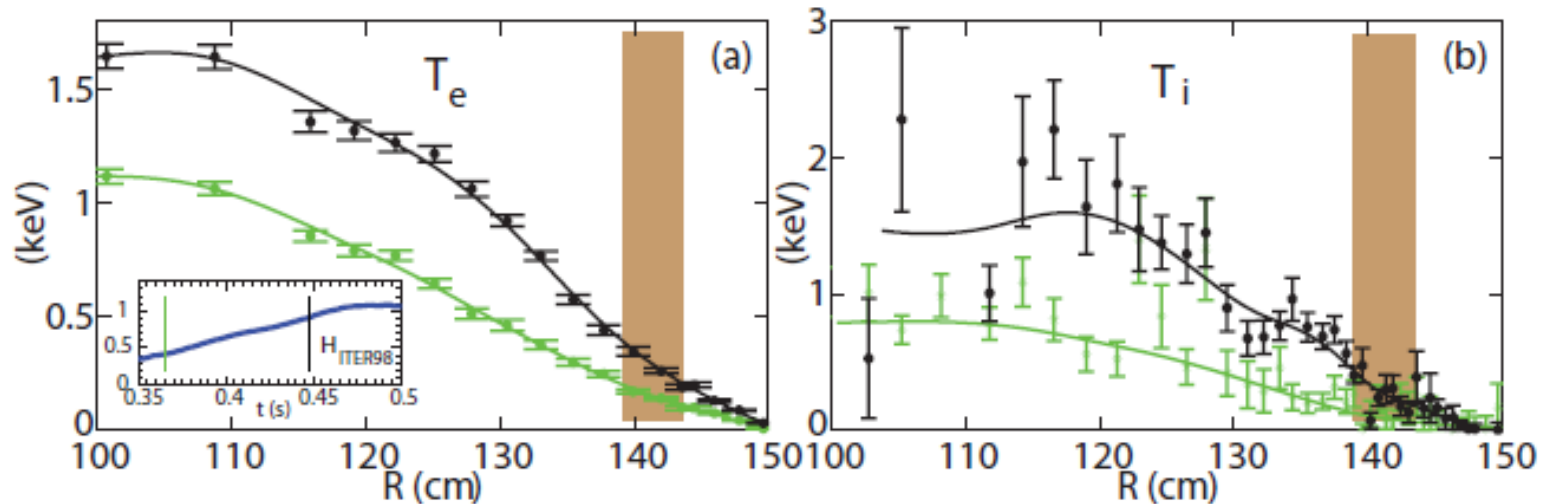
$$\text{Pr} = \frac{\hat{\chi}_\phi}{\hat{\chi}_i} = \frac{\hat{\Pi}_\phi(0, u') - \hat{\Pi}_\phi(0, 0)}{\hat{u}'} \cdot \frac{a/L_{Ti}}{\hat{Q}_i}$$

$$\left(\frac{RV_\phi}{\chi_\phi} \right) = \left[\frac{\hat{\Pi}_\phi(u, 0) - \hat{\Pi}_\phi(0, 0)}{\hat{u}} - \underline{\hat{m}\hat{R}\hat{\Gamma}_p(u, 0)} \right] \cdot \frac{\hat{u}'}{\hat{\Pi}_\phi(0, u') - \hat{\Pi}_\phi(0, 0)}$$

- Subtracting particle convection contribution

Example from NSTX L-mode (Ren, IAEA 2012, EX/P7-2)

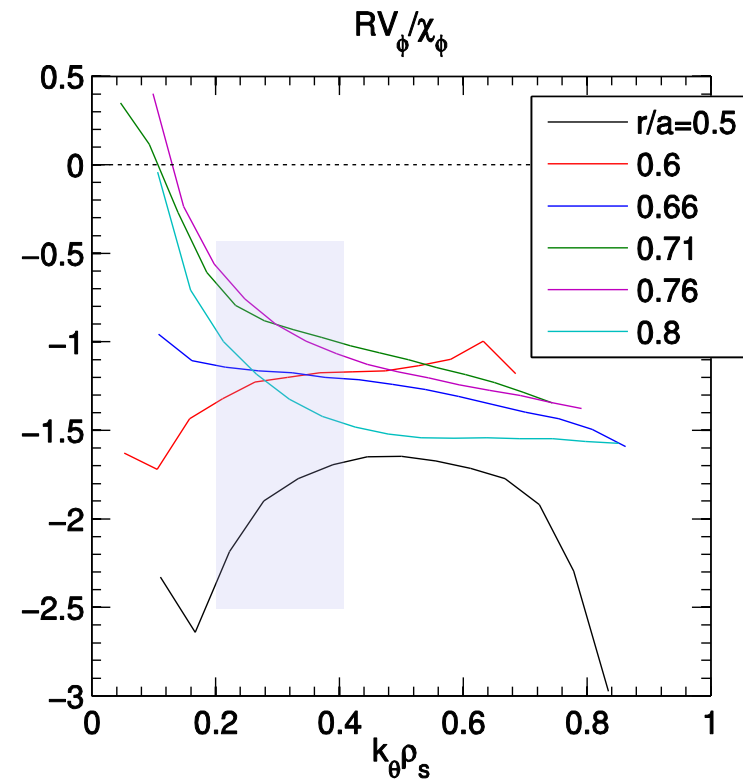
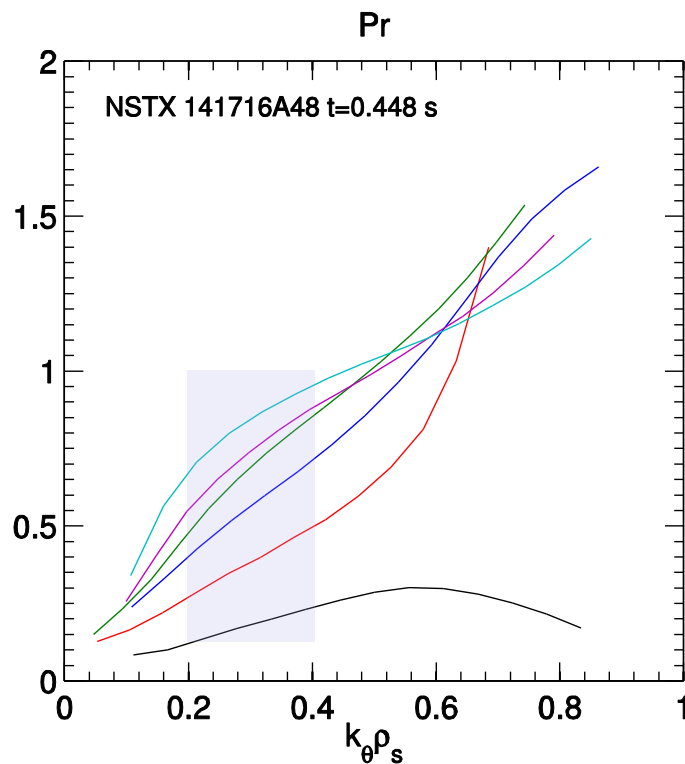
- Low k_θ stability dominated by ITG/TEM
- No perturbative momentum experiments in this case, but it provides a basis for comparing to conventional tokamaks
- MAST perturbative L-mode experiments planned this year



$$B_T = 0.55 \text{ T}, I_p = 0.9 \text{ MA}, P_{\text{NBI}} = 2 \text{ MW}, \langle n \rangle \approx 3 \times 10^{19} \text{ m}^{-3}$$

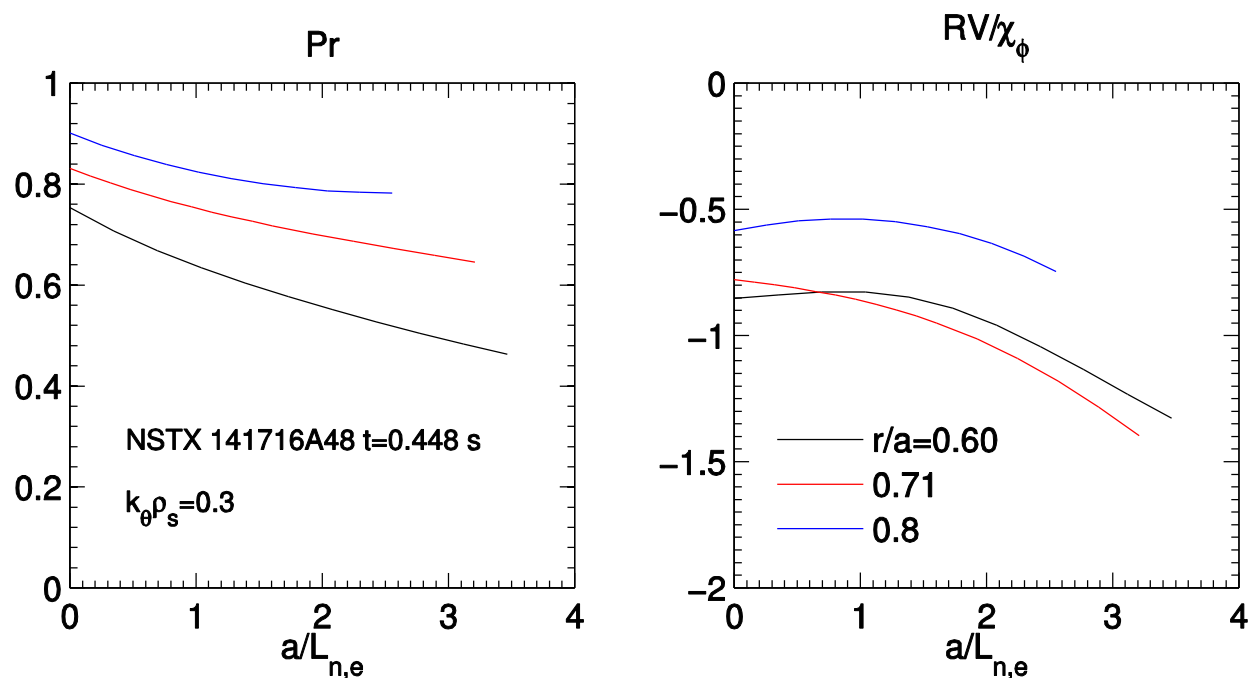
Quasilinear Prandtl number increases with radius, relatively weak momentum pinch predicted

- Range of $Pr \sim 0.2-0.8$ generally consistent with experiment (~ 0.5)
 - NL spectrum peak around $k_\theta \rho_s \sim 0.3$
 - Small inward pinch $RV_\phi/\chi_\phi \sim -(1-2)$
- \Rightarrow Investigate sensitivity to various parameters



Pinch remains relatively small even for increased density gradient ($a/L_n = -a\nabla n/n$)

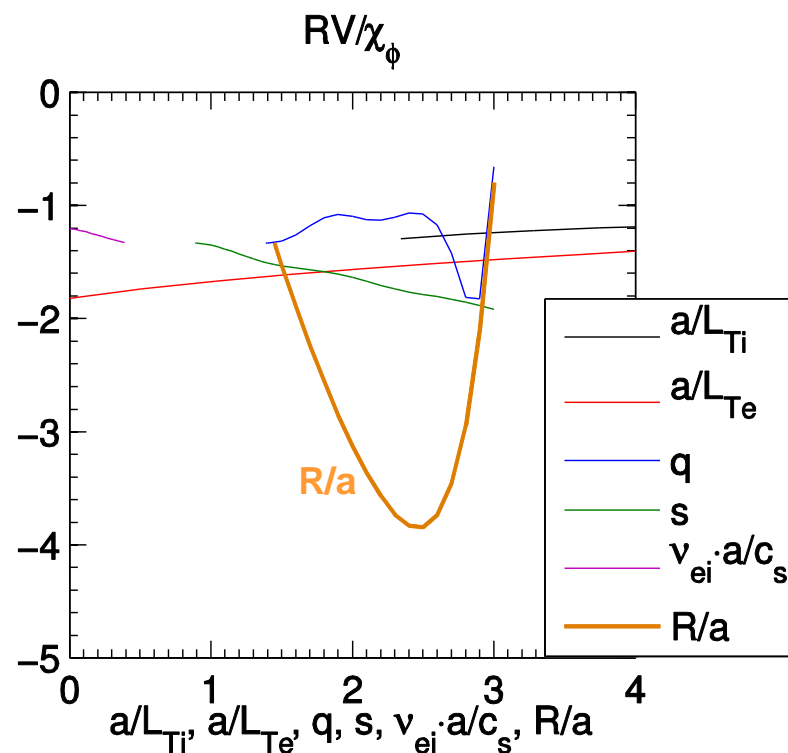
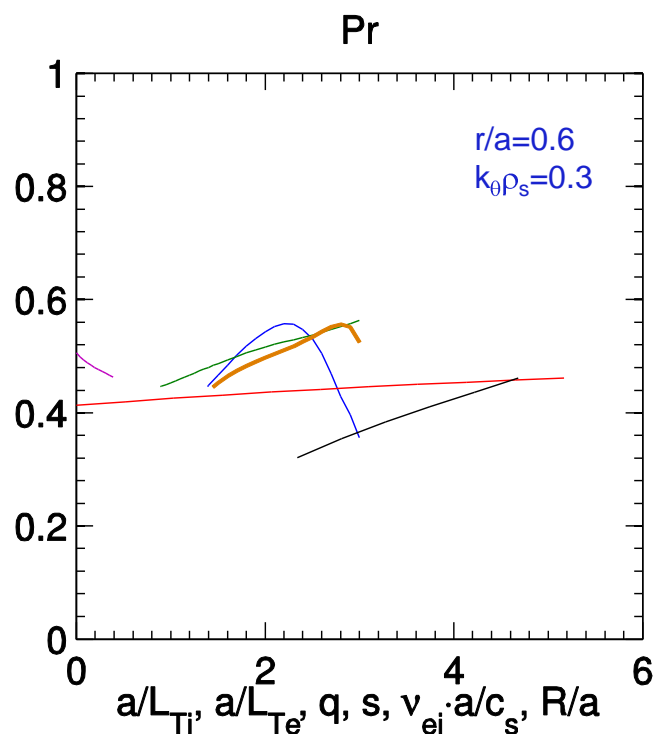
- Weaker dependence than predicted for ITG in conventional tokamaks



- Growth rates at $r/a=0.6$ increase with a/L_n
 - TEM-like at $r/a=0.6$
 - ITG-like at $r/a=0.8$
- Weaker pinch consistent with smaller RV_ϕ/χ_ϕ reported for TEM conditions at higher aspect ratio [Kluy et al., 2009]

Pinch predicted to be weakly dependent on many parameters except aspect ratio (R/a)

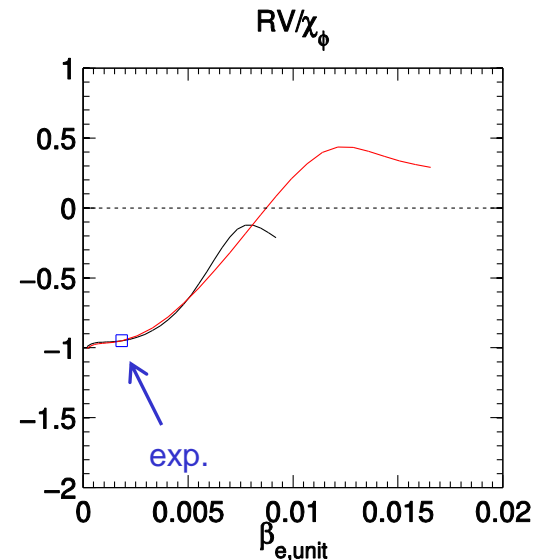
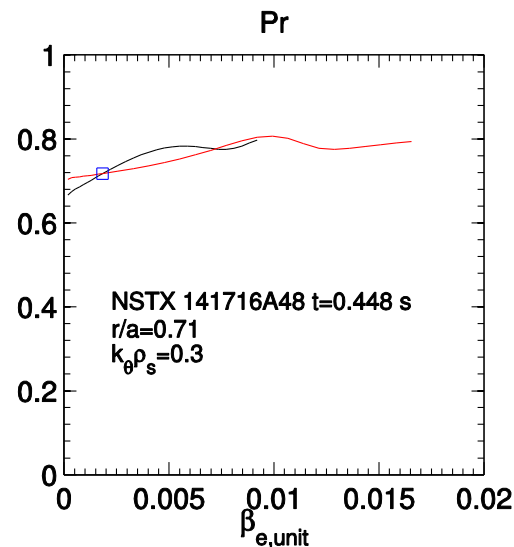
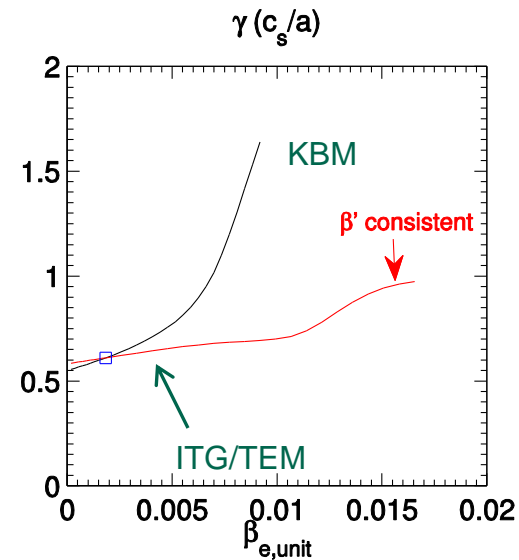
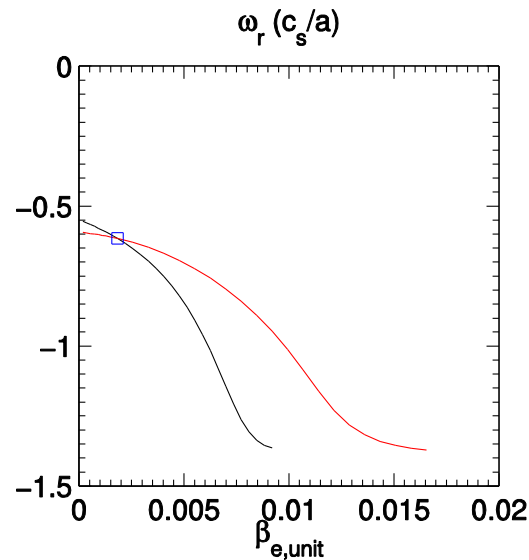
- Prandtl number remains constant $\sim 0.4-0.6$
- RV_ϕ/χ_ϕ relatively insensitive to $a/L_{Ti,e}$, q , s , v_{ei}
- Becomes much larger (inward) for **increased aspect ratio (R/a)**



- q , s , R/a scans using local Miller equilibrium model \Rightarrow not consistent with any particular global equilibrium

Growth rates increase with beta, eventually transition to KBM (preview for H-modes)

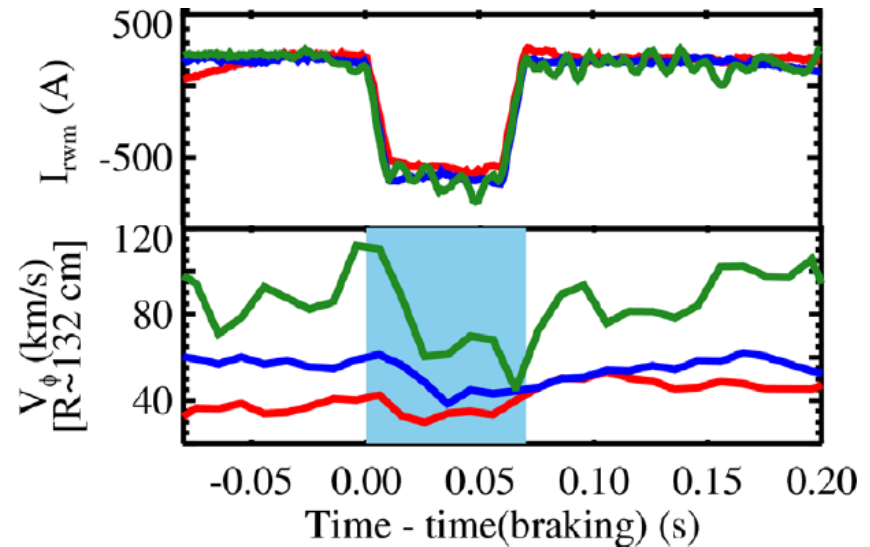
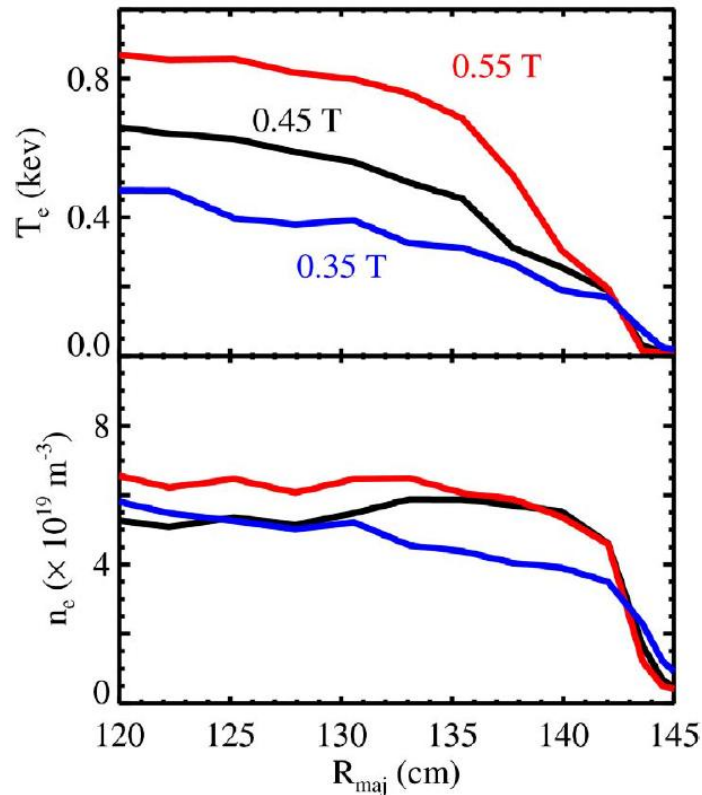
- ITG/TEM growth rates *increase* with β_e , opposite to traditional results (e.g. “cyclone base case”)
- Eventually transitions to KBM (similar to hybrid ITG/KBM [Belli, Candy 2010])
 - Increasing β'_{eq} consistently is stabilizing [Bourdelle, 2003]
- Pr remains ~constant
- Pinch goes toward zero, even positive/outward (depending on β'_{eq})
 - similar to EM behavior predicted in conventional aspect ratio [Hein, 2010]



NSTX H-modes

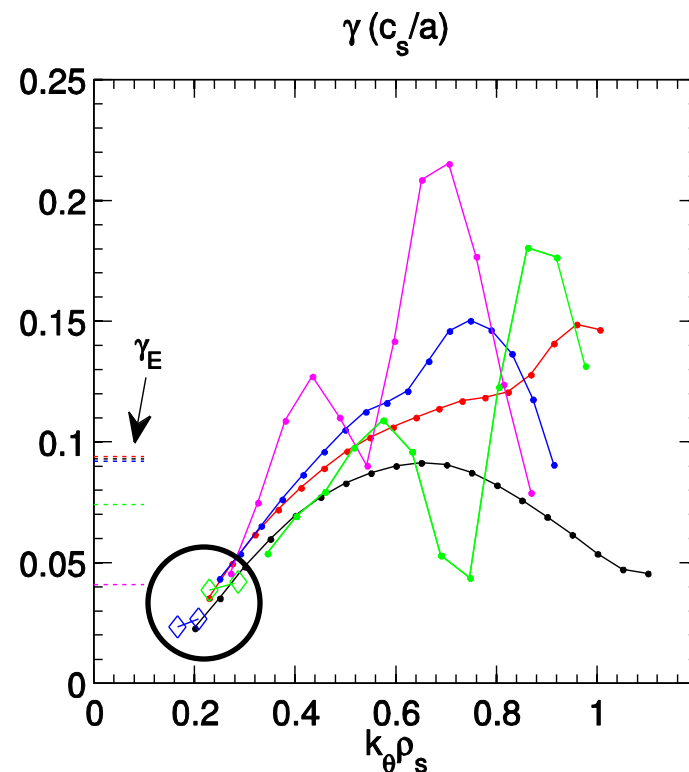
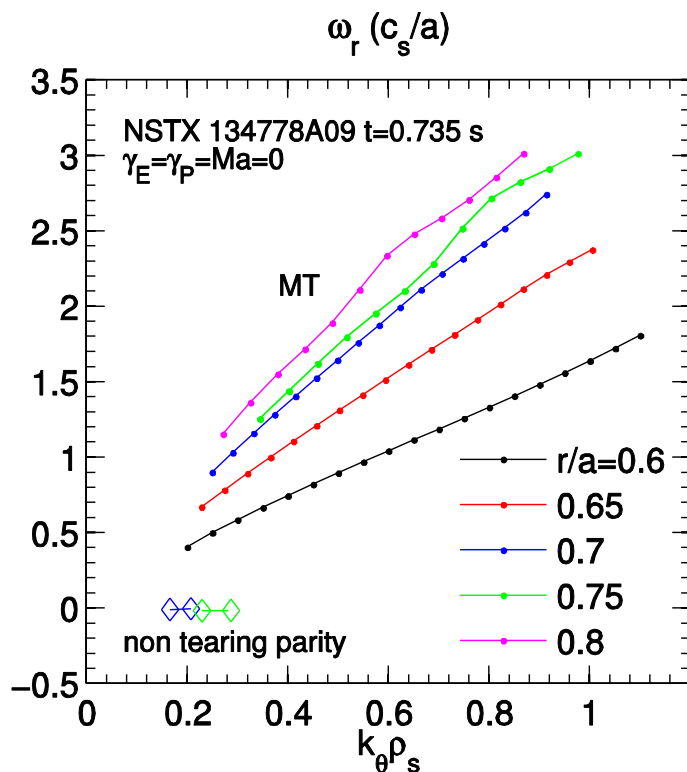
- Simulations run for 7 NBI H-modes with $n=3$ perturbations [Solomon, 2010]

$$B_T = 0.35 - 0.55 \text{ T} \quad I_p = 0.7 - 1.1 \text{ MA}$$
$$P_{\text{NBI}} = 4 - 6 \text{ MW} \quad \langle n \rangle \approx 4 - 6 \times 10^{19} \text{ m}^{-3}$$



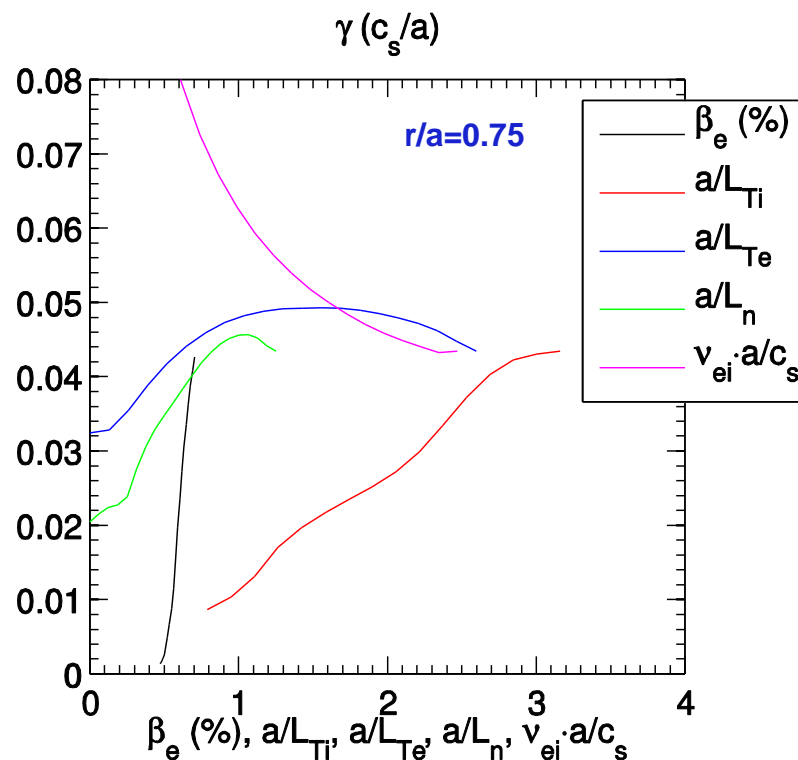
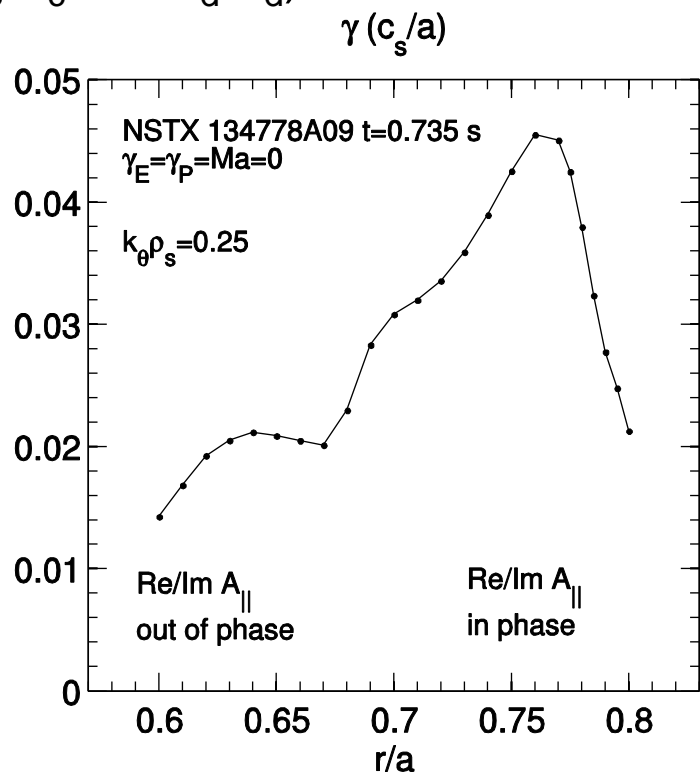
Most cases show broad spectra of microtearing modes

- Apparent in eigenfunctions (not shown) and near linear dispersion $\omega \approx \omega_{*e}$
 - Microtearing only transports electron energy
- Often see hints of subdominant ballooning modes (\diamond)
 - Unknown whether they survive nonlinearly
- $E \times B$ shearing rates comparable to γ_{lin} ($\gamma_{\text{lin}}/\gamma_E \uparrow$ as $r/a \uparrow$)



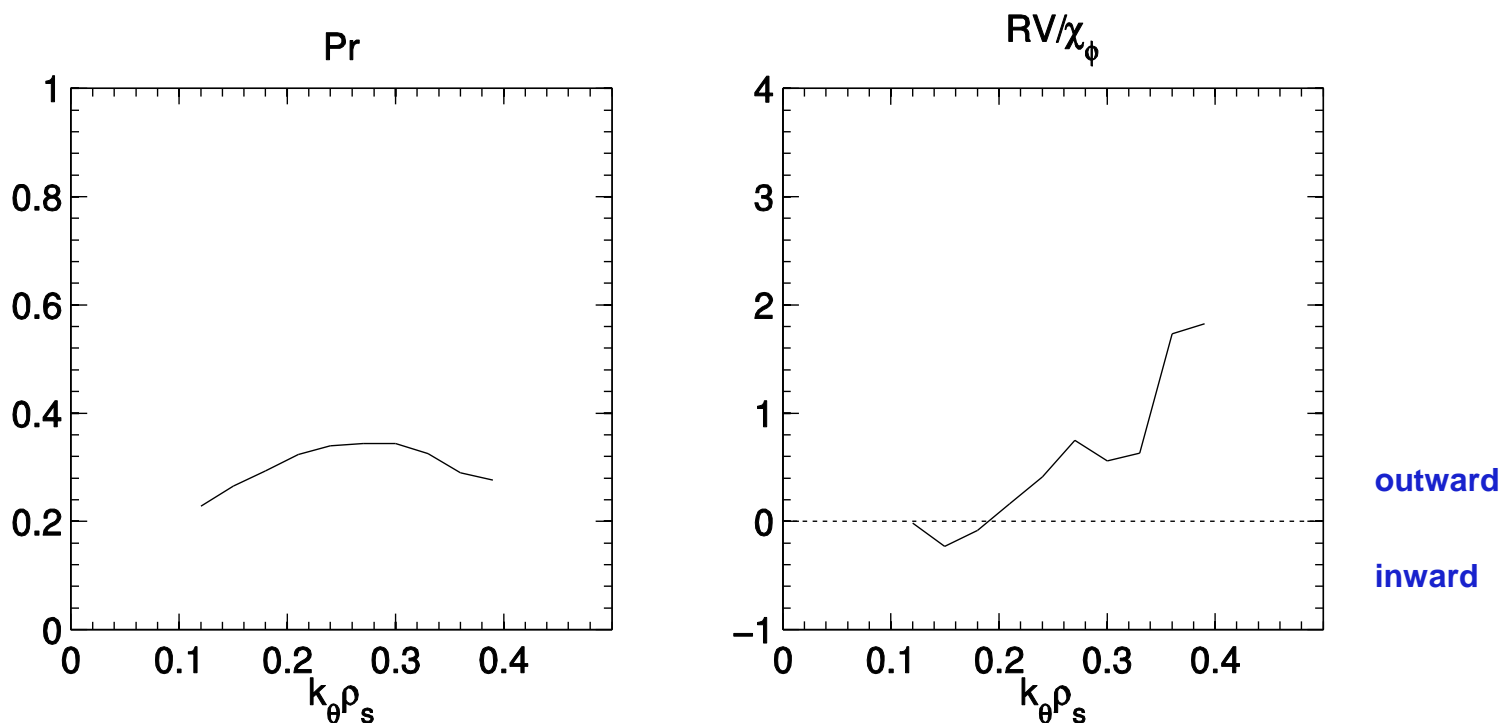
Ballooning modes exist over a $r/a=0.6-0.8$, exhibit KBM behavior

- Very sensitive to $\beta_e \rightarrow$ KBM ($\alpha_{\text{MHD,unit}} > 0.6$)
 - Unstable from a/L_{Ti} - similar to hybrid ITG/KBM behavior found by Belli, Candy [2010]
 - Similar hybrid-KBM modes often predicted in NSTX H-modes [Guttenfelder, IAEA 2012; Canik, IAEA 2012; TTF 2013]
- Transport contributions come from both ϕ and $B_{||}$; also D and C ($Z_{\text{eff}} \approx 3$, $n_c m_c \sim 0.7 n_d m_d$)



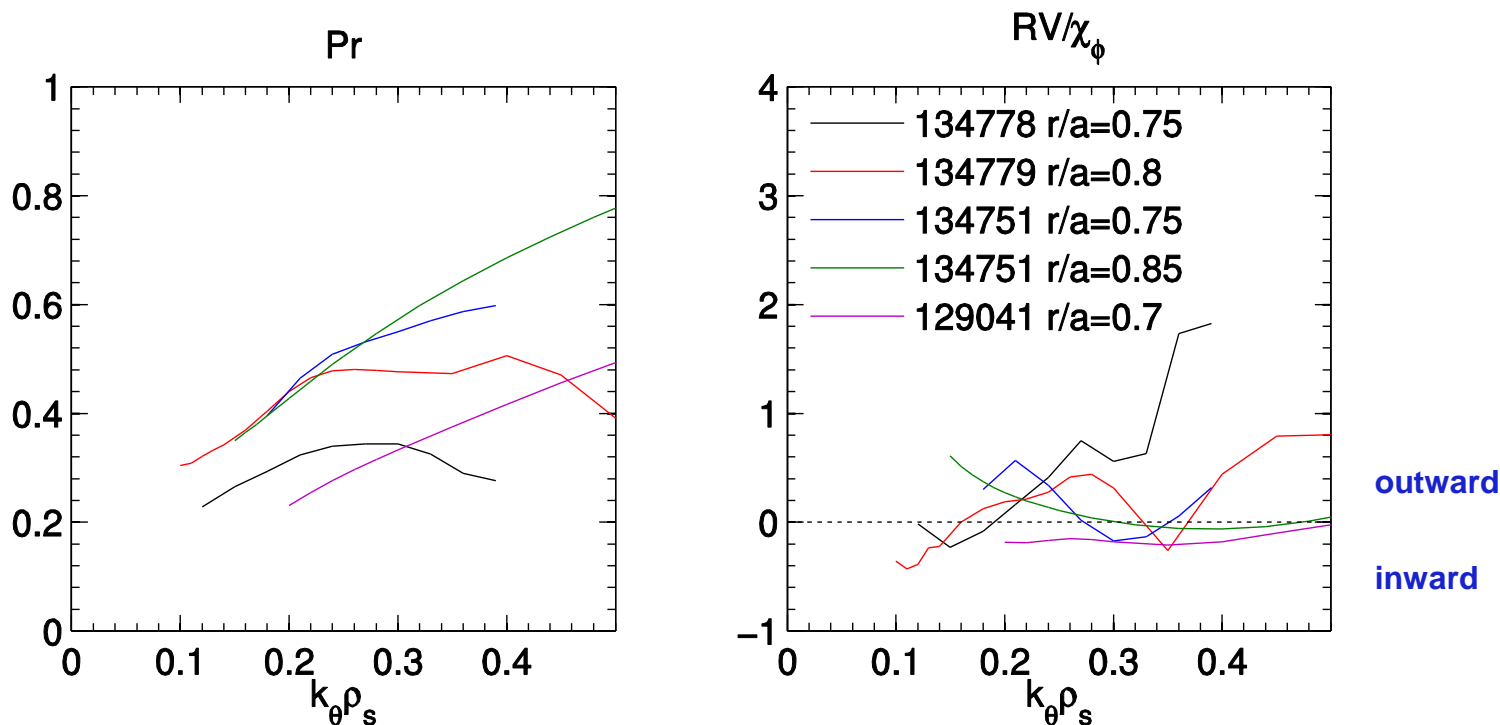
Small Prandtl numbers over KBM range of $k_{\theta}\rho_s$, small/outward Pinch parameter

- Interpreted Pr would be smaller for $\chi_{i,nc} > \chi_{i,turb}$
- Small/outward RV_{ϕ}/χ_{ϕ}
 - consistent with KBM predictions using conventional tokamak parameters [Hein, 2010]



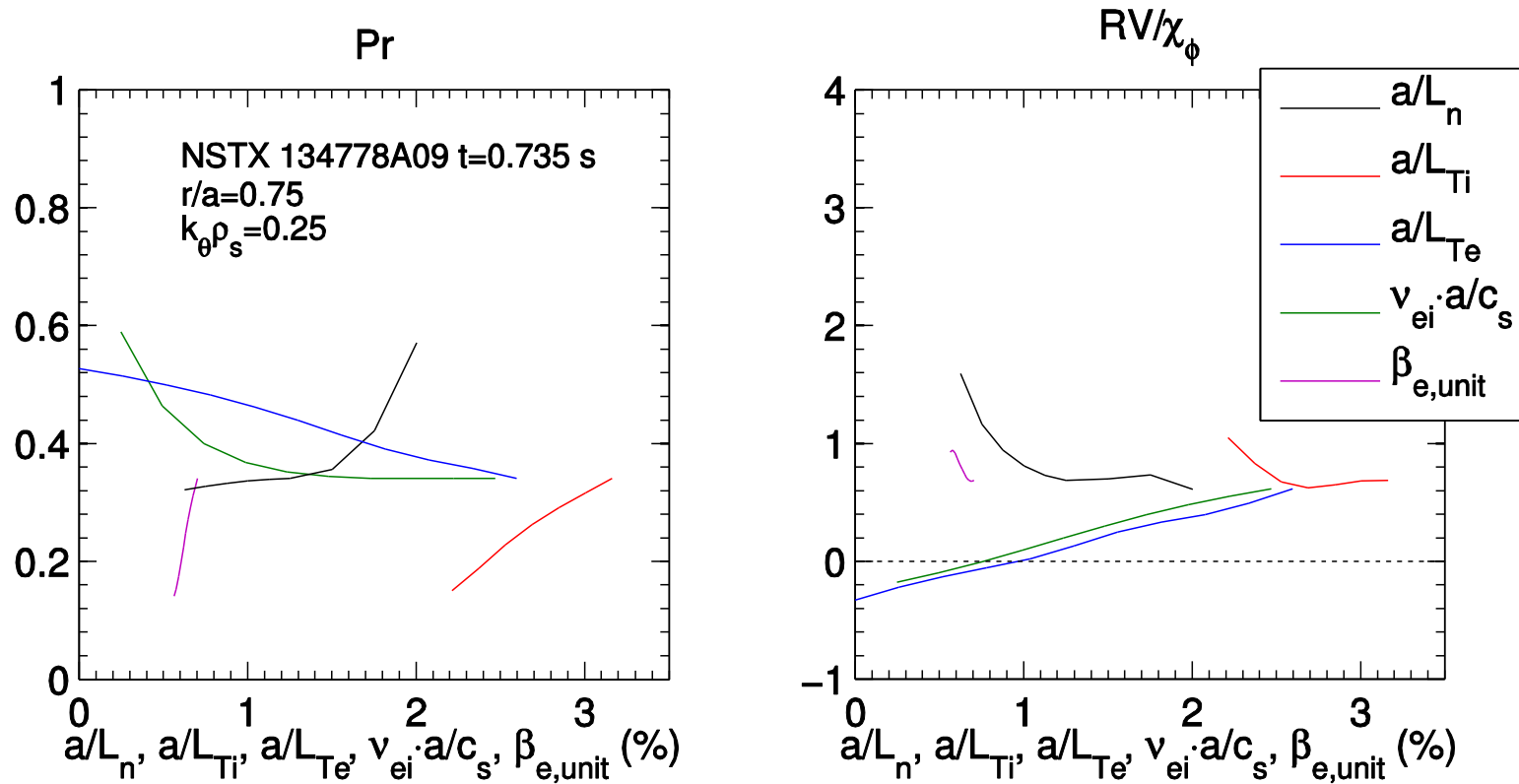
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- Interpreted Pr would be smaller for $\chi_{i,nc} > \chi_{i,turb}$
- Small/outward RV_{ϕ}/χ_{ϕ}
 - consistent with KBM predictions using conventional tokamak parameters [Hein, 2010]
- Small/positive RV_{ϕ}/χ_{ϕ} predicted in multiple cases, never approaches larger inward experimental values (-7)



Pinch parameter shows minor changes with parameters, always remains near zero or outwards

- Never approaches larger inward experimental values (-7)



- What else is missing?

Additional considerations

- Nonlinear transport possibly different from quasilinear (simulations beginning)

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- Perpendicular ($E \times B$) flow shear (Dominguez, Casson, Waltz)

$$\Pi_{\varphi} = (\chi_{\varphi} u' + \chi_{\varphi \perp} \gamma_E) + (R V_{\varphi} + R \Gamma_p) u + \Pi_{\varphi, RS}$$

purely toroidal flow
 $\gamma_E \sim r/qR \cdot u'$

After factoring out reduced transport due to turbulence suppression, $E \times B$ shear can increase or decrease momentum flux, depending on magnetic shear [Casson, 2009]

→ Nonlinear simulations

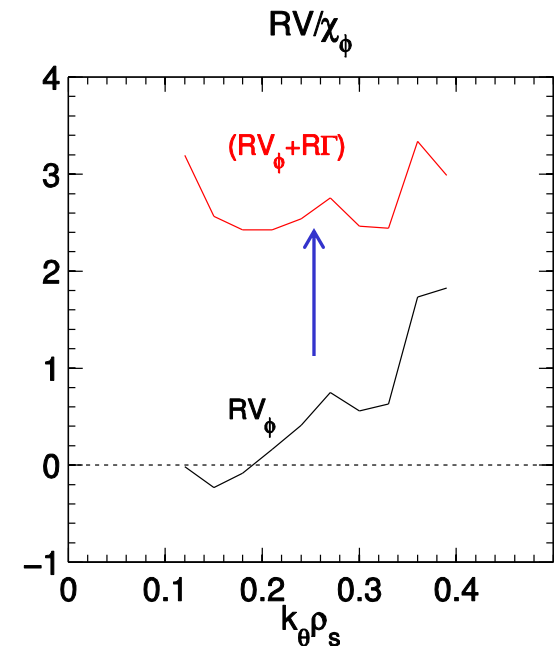
Additional considerations

- Nonlinear transport possibly different from quasilinear (simulations beginning)
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$$\Pi_{\phi} = (\chi_{\phi} u' + \chi_{\phi\perp} \gamma_E) + (RV_{\phi} + R\Gamma_p)u + \Pi_{\phi,RS}$$

- Influence of particle flux

In all cases investigated this adds outward momentum flux



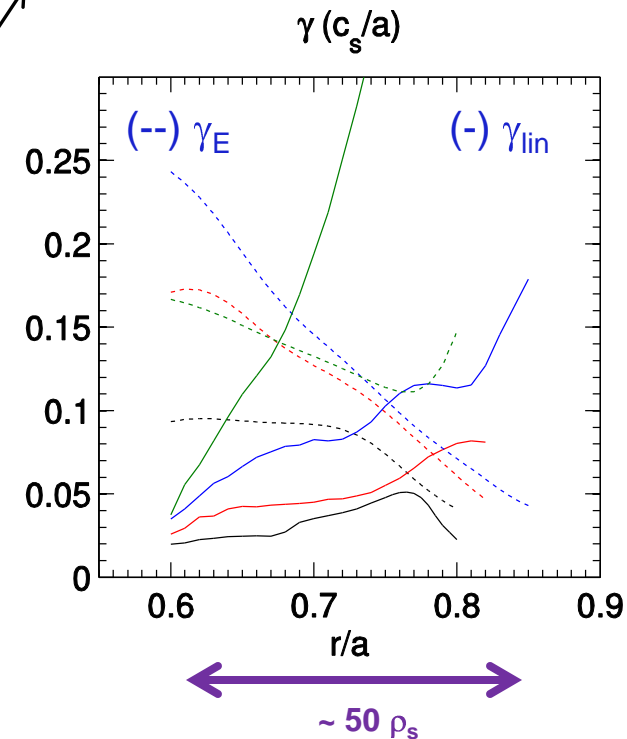
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- Influence of particle flux
- Finite ρ_* effects: profile shear, non-local effects, influence from pedestal

Possible that perturbations in profiles could indirectly lead to inferred inward momentum pinch
 → global EM simulations (with A_{\parallel} & B_{\parallel})



Additional considerations

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- Perpendicular ($E \times B$) flow shear (Dominguez, Casson, Waltz)

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- Influence of particle flux
- Finite ρ_* effects: profile shear, non-local effects, influence from pedestal
- Centrifugal effects on transport and stability

e.g. $M_c > 1$ on Π_c or $R/L_n(\theta)$ on KBM vs. MT thresholds
(GKW work in progress, R. Buchholtz, W. Hornsby)

Additional considerations

- Nonlinear transport possibly different from quasilinear (simulations beginning)
- Perpendicular ($E \times B$) flow shear (Dominguez, Casson, Waltz)

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- Influence of particle flux
- Finite ρ_* effects: profile shear, non-local effects, influence from pedestal
- Centrifugal effects on transport and stability
- Some other unaccounted for mechanism (MHD, ...)

⇒ Mechanism(s) for strong observed inward pinch remains unresolved

Impurity transport

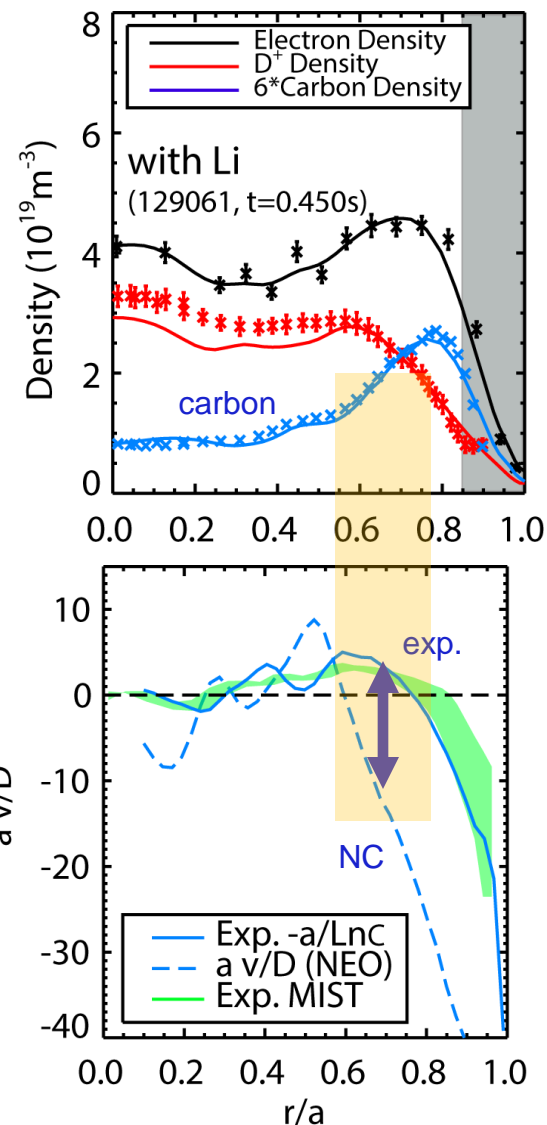
Occasional evidence for non-neoclassical impurity transport in Lithium conditioned H-modes [Scotti, IAEA 2012]

- Impurity transport often close to neoclassical levels in H-modes [Delgado-Aparicio, NF 2009, 2011; Clayton, PPCF 2012]
- With lithium wall conditioning, ELMs are suppressed and carbon accumulates
 - Lithium does NOT accumulate (better scrape-off layer screening + neoclassical $D_{Li} \gg D_c$)

$$\Gamma_c = -D_c \nabla n_c + V_c n_c \approx 0 \Rightarrow \boxed{\frac{aV_c}{D_c} = -\frac{a}{L_{n,c}}}$$

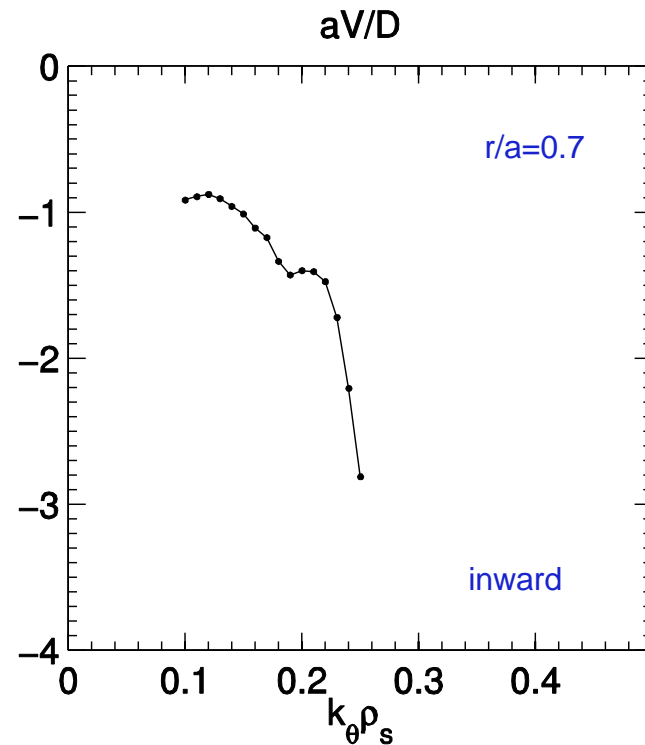
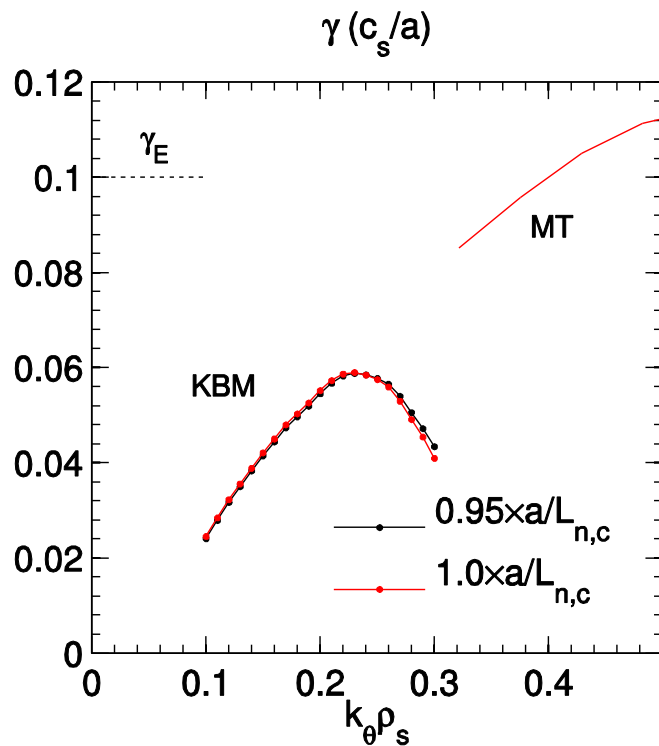
- Profile shape can diverge significantly from neoclassical theory (don't have quantitative source in these cases)

Q: Can ballooning modes influence impurity transport in NSTX H-modes?



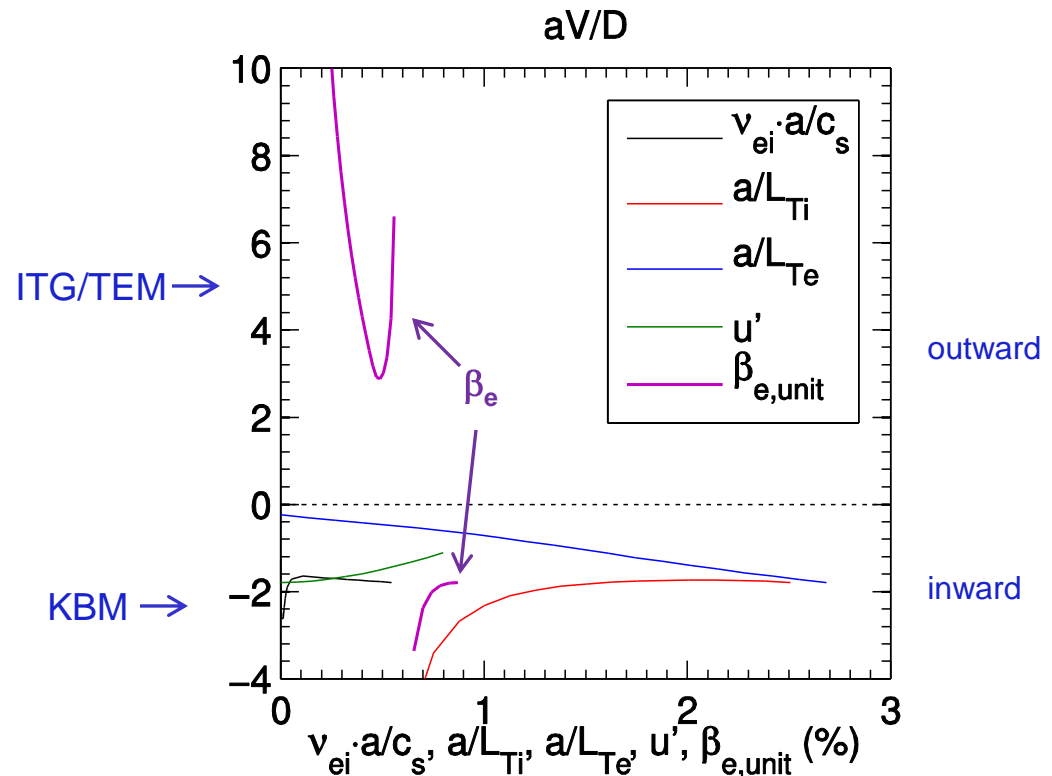
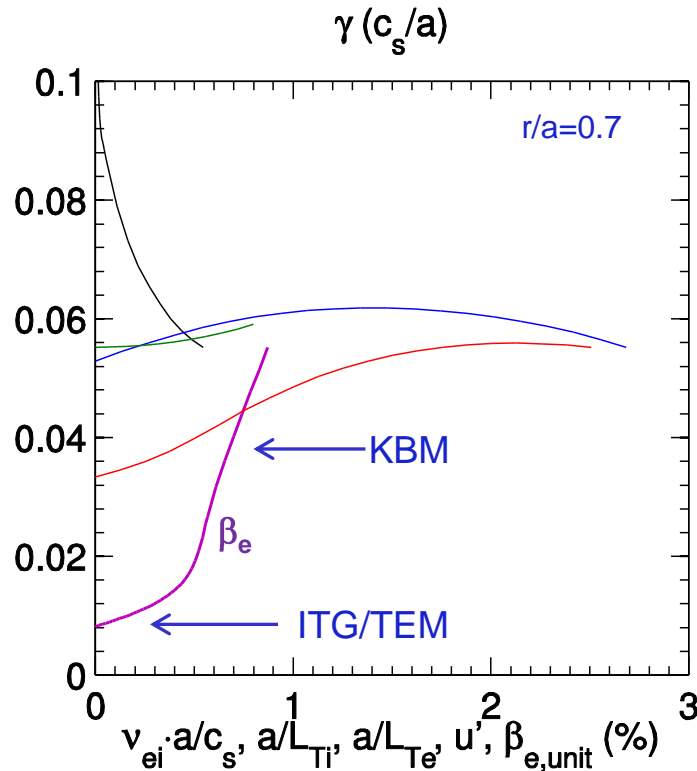
Microtearing modes dominate, sub-dominant KBM modes predict inward carbon pinch

- Microtearing dominates (no particle flux)
- Weaker hybrid-KBM ($\gamma_{\text{KBM}} < \gamma_{\text{E}}$) – unknown if this survives nonlinearly
- KBM predicts inward carbon pinch ($r/a=0.6-0.7$)
 - Opposite to experiment, similar to neoclassical



Inward carbon pinch predicted for KBM over a range of parameters

- Direction of carbon convection insensitive to v_{ei} , a/L_{Ti} , a/L_{Te} , and u'
 - Outward carbon convection predicted as beta is reduced and mode transitions to ITG/TEM
- ⇒ Does not appear to reconcile non-neoclassical impurity profile



Summary

- NSTX L-modes governed by ITG/TEM, linear simulations predict:
 - $Pr \sim 0.2-0.8$ generally consistent with experimental analysis (~ 0.5)
 - Relatively weak inward pinch ($RV_\phi/\chi_\phi \sim -1$) insensitive to many parameters except R/a
- NSTX $n=3$ nRMP H-mode experiments dominated linearly by microtearing ($r/a=0.6-0.8$)
 - Sub-dominant ITG/KBM exist, $Pr \sim 0.3-0.6$ but will be smaller depending on $\chi_i/\chi_{i,nc}$
 - $RV_\phi/\chi_\phi \sim -1 - +2$ small/outward compared to stronger inward experimental values, relatively insensitive to parameter variations
- In lithiated H-mode cases where impurity carbon transport appears to be anomalous:
 - KBM modes (sub-dominant to microtearing) predict inward carbon pinch opposite to experiment
- A big to-do: Nonlinear simulations of “mixed-modes” (ITG/KBM+MT)

Method for inferring quasi-linear Prandtl (χ_ϕ/χ_i) and Pinch numbers (RV_ϕ/χ_ϕ)

- Assuming momentum flux due to:

Diffusion

$\sim u'$

Convection (momentum pinch)

} $\sim u$

Particle convection

Residual stress (up-down asymmetry, finite ρ_* , etc...)

independent of u, u'

$$\hat{\Pi}_\phi = \hat{\chi}_\phi \hat{u}' + (\hat{R}\hat{V}_\phi + \hat{R}\hat{\Gamma}_p) \hat{u} + \hat{\Pi}_{\phi,RS}$$

⇒ Using u, u' perturbations, **subtracting particle convection contribution**

$$Pr = \frac{\hat{\chi}_\phi}{\hat{\chi}_i} = \frac{\hat{\Pi}_\phi(0, u') - \hat{\Pi}_\phi(0, 0)}{\hat{u}'} \cdot \frac{a/L_{Ti}}{\hat{Q}_i}$$

$$\left(\frac{RV_\phi}{\chi_\phi} \right) = \left[\frac{\hat{\Pi}_\phi(u, 0) - \hat{\Pi}_\phi(0, 0)}{\hat{u}} - \underline{\hat{m}\hat{R}\hat{\Gamma}_p(u, 0)} \right] \cdot \frac{\hat{u}'}{\hat{\Pi}_\phi(0, u') - \hat{\Pi}_\phi(0, 0)}$$

Transport of toroidal angular momentum calculated from delta-f gyrokinetics (GYRO*)

- Transport calculated for **toroidal momentum** from correlation of **perturbed distribution function** and **effective radial drifts** from all EM fields

$$\delta f_s(\vec{x}) = -\frac{e\delta\phi(\vec{x})}{T_s} F_{s0} + H_s(\vec{R}) \quad (3.22)$$

$$\Pi_s = \oint_{\text{flux surface average}} \int d^3v H_s^*(\vec{R}) \left\langle \underbrace{[m_s \mathbf{R}(\vec{V}_0 + \vec{v}) \cdot \vec{e}_\phi]}_{\text{red line}} \underbrace{\frac{c}{B} \vec{b} \times \nabla}_{\text{blue line}} \left[\underbrace{\delta\phi(\vec{x})}_{\text{green line}} - \frac{1}{c} (\vec{V}_0 + \vec{v}) \cdot \delta\vec{A}(\vec{x}) \right] \cdot \nabla \mathbf{r} \right\rangle_{\text{gyro average}} \quad (3.55)$$

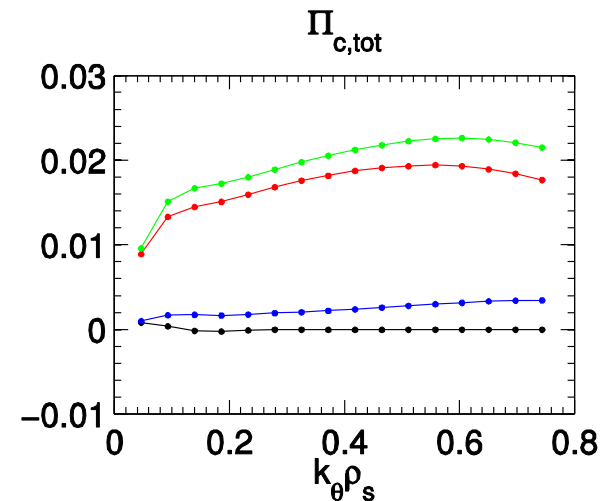
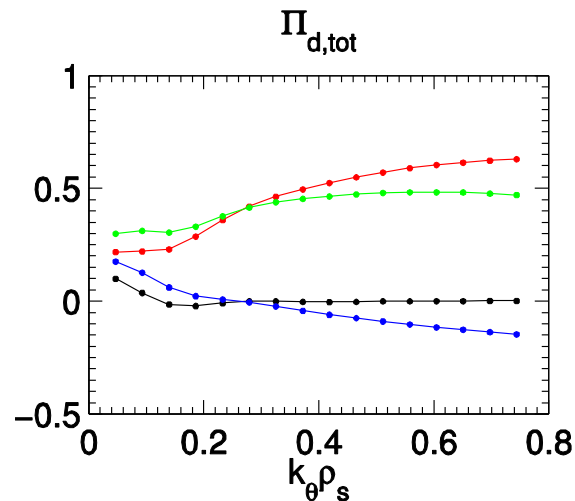
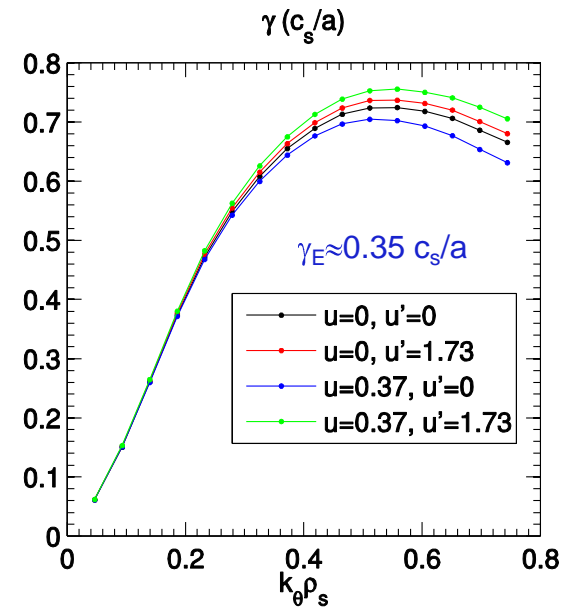
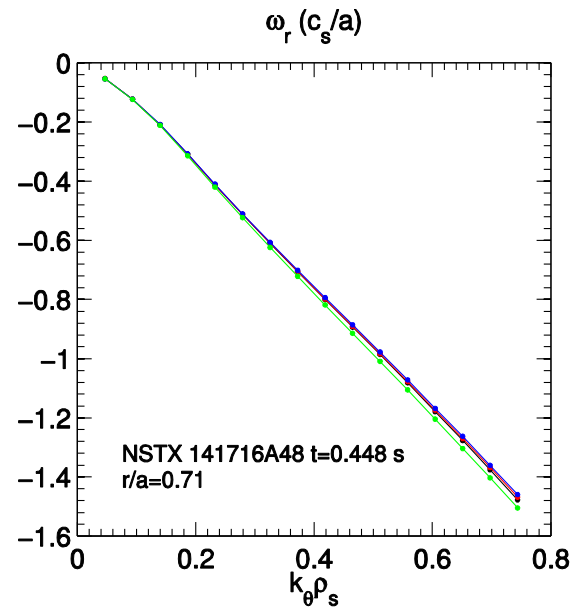
↓ Electrostatic E×B drift
↓ Drifts from shear ($v_{\parallel} \nabla A_{\parallel} \sim v_{\parallel} B_r$) and compressional ($v_{\perp} \nabla A_{\perp} \sim v_{\perp} B_{\parallel}$) magnetic perturbations

- EM contributions are important in NSTX H-modes*

*Candy & Belli, GYRO Technical Guide, <https://fusion.gat.com/theory/Gyro>

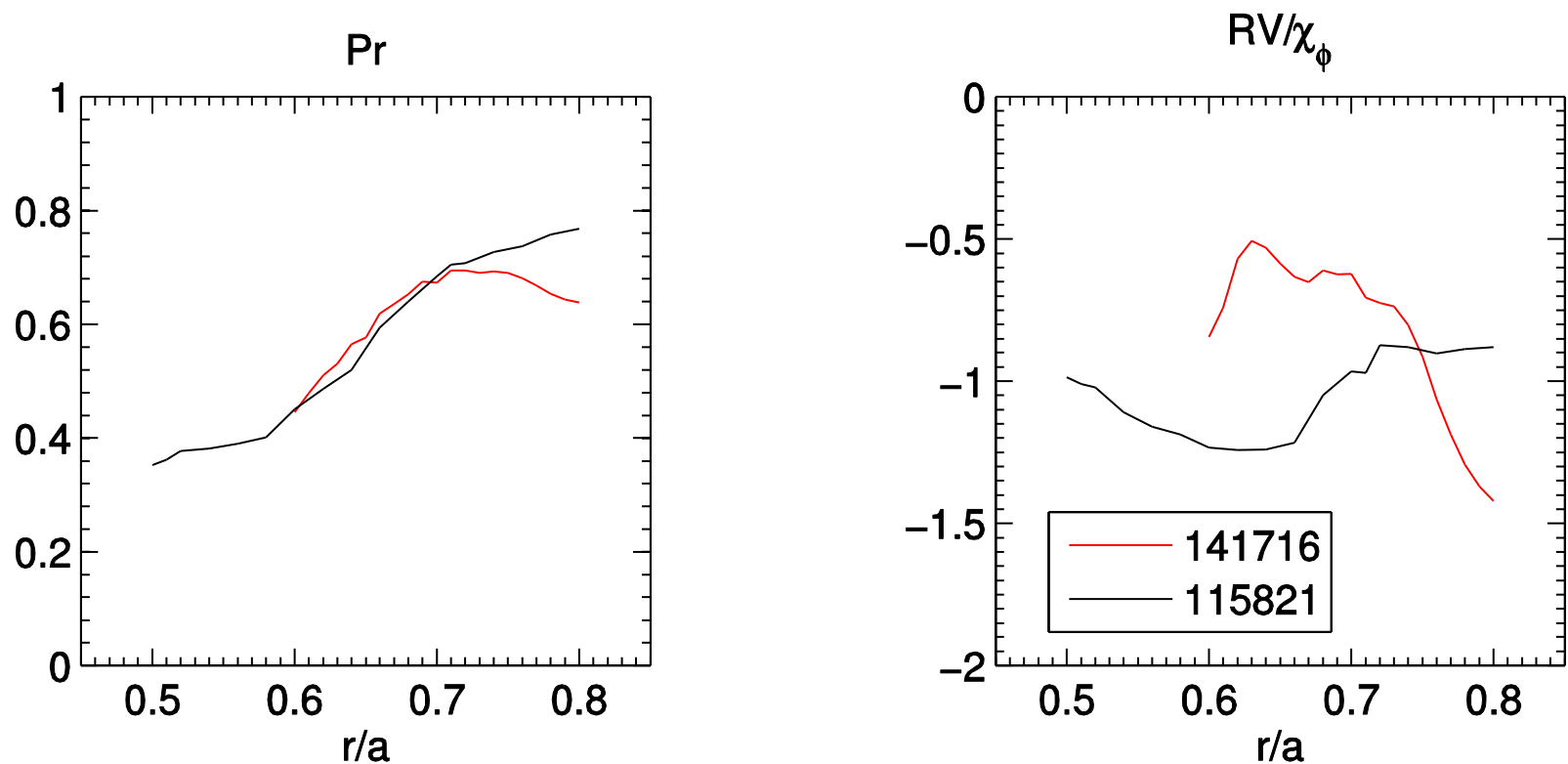
L-mode unstable to ITG/TEM, momentum fluxes vary with u, u'

- Growth rates, change little with u, u'
 - u' can drive instability if large enough
- Momentum fluxes vary with u, u' as expected
 - All fluxes normalized by $k_{\theta}\rho_s|\phi|^2$
- Deuterium dominates carbon
 - Very little impurity in this L-mode, $Z_{\text{eff}}\sim 1.2$, $n_c m_c \ll n_d m_d$)



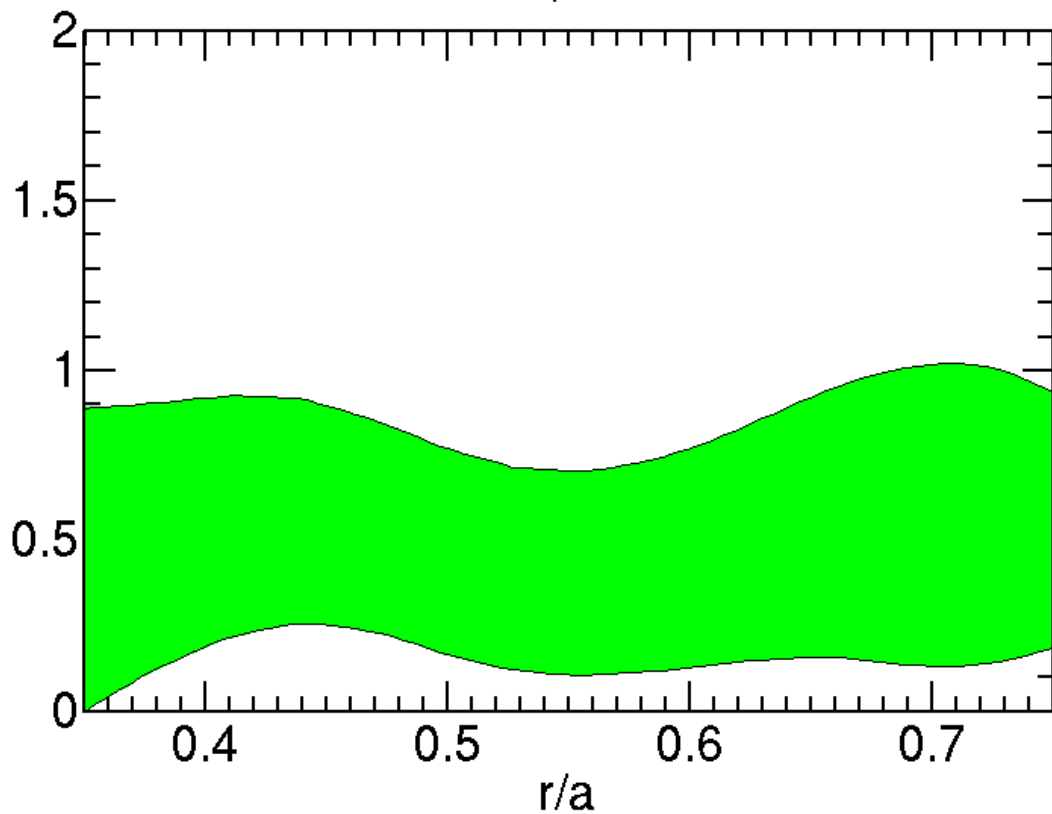
Predicted quasilinear Pr and RV/c very similar for additional L-mode case

- 141716 from [Ren et al., IAEA, 2012]
- 115821 from [Kaye et al., NF 2009]

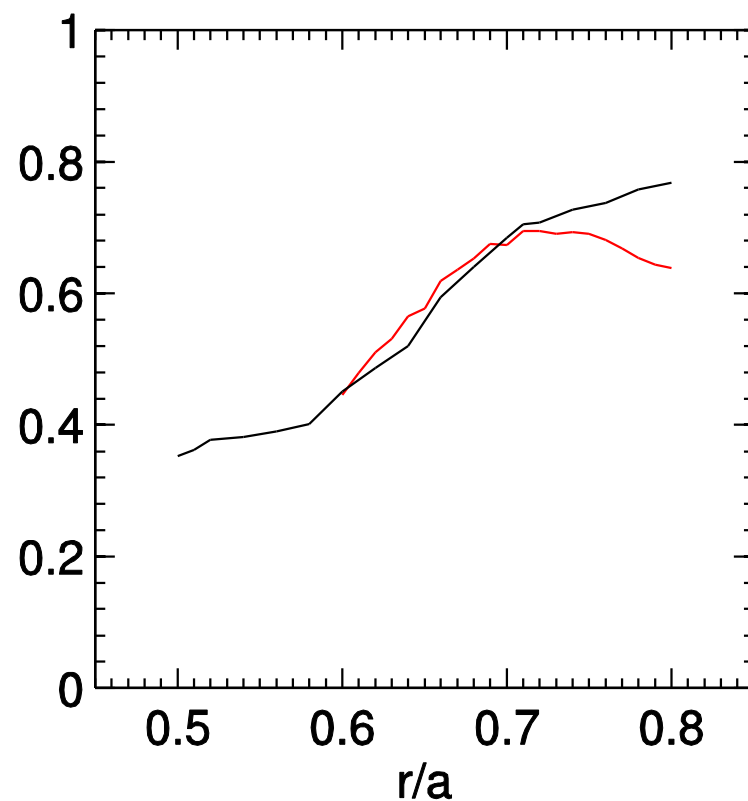


Experimental Pr profile for L-mode

χ_ϕ/χ_i

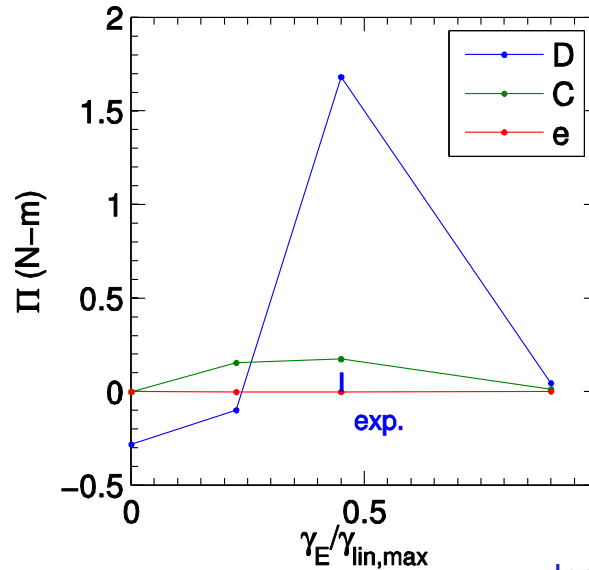
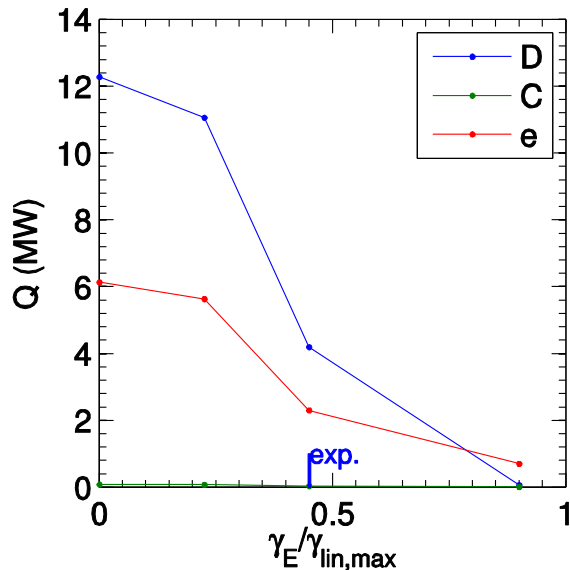


Pr



Nonlinear simulations predict significant momentum flux

- At $r/a=0.71$ nonlinear simulation (with $E \times B$ shear) overpredicts heat fluxes [Ren, IAEA 2012]
- Predicted momentum flux also too large (using u, u' for purely toroidal rotation)
 - “Effective” $Pr \approx 0.3 \rightarrow$ have yet to determine RV_ϕ/χ_ϕ from nonlinear simulations
- $E \times B$ shear driven momentum flux [Dominguez; Casson] and profile shearing (finite ρ_*) effects [Camenen] could also be important
 - Require global simulations



$r/a=0.71$

$Q_{i,exp} \approx 0.3$ MW

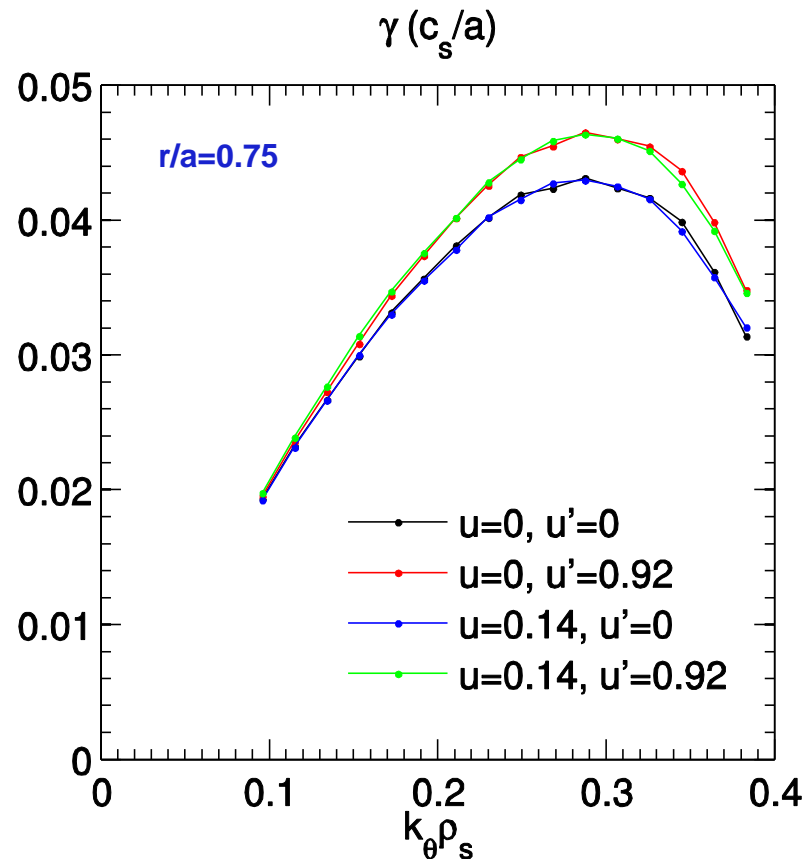
$Q_{e,exp} \approx 0.8$ MW

$\Pi_{exp} \approx 0.5$ N-m

Increasing, u, u' & γ_E consistently
 ($\gamma_E \sim r/qR \cdot u'$ for purely toroidal flow)

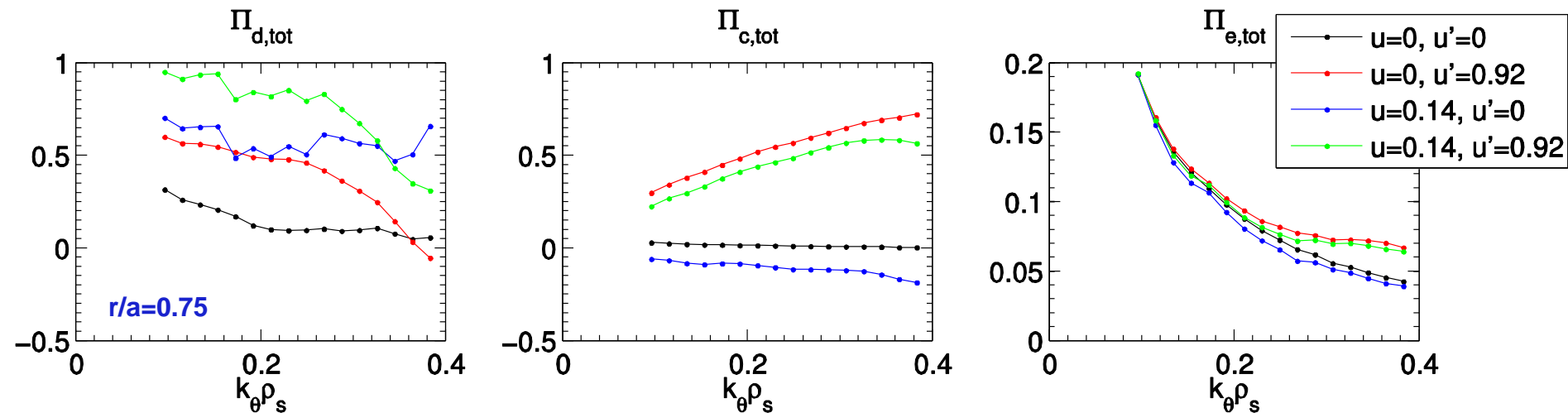
Little change in KBM linear growth rates when including toroidal flow and/or parallel flow shear

- Small increase due to parallel velocity gradient



Change in quasi-linear momentum fluxes due to u & u'

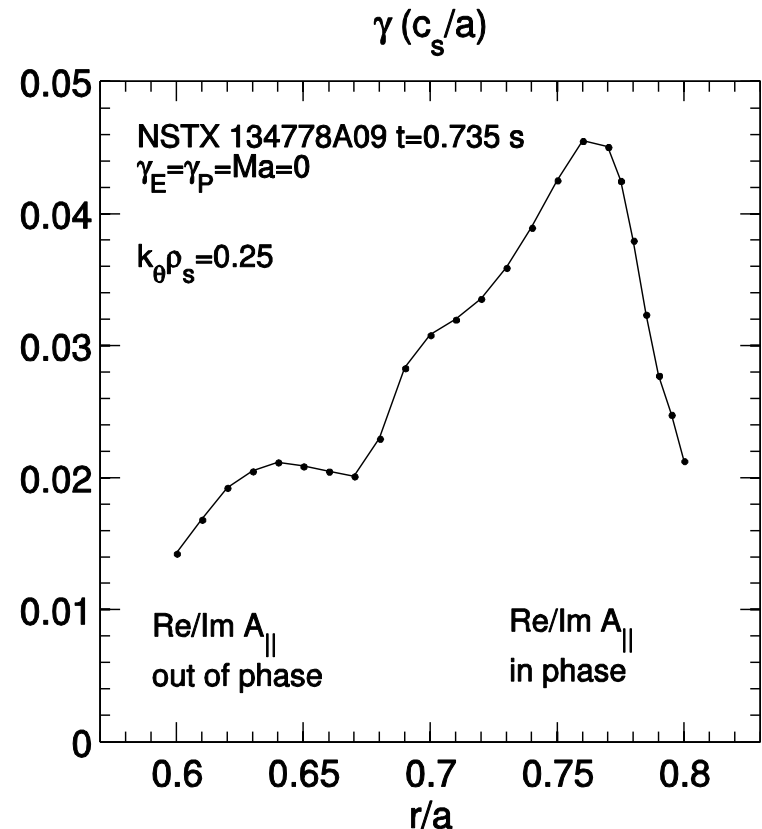
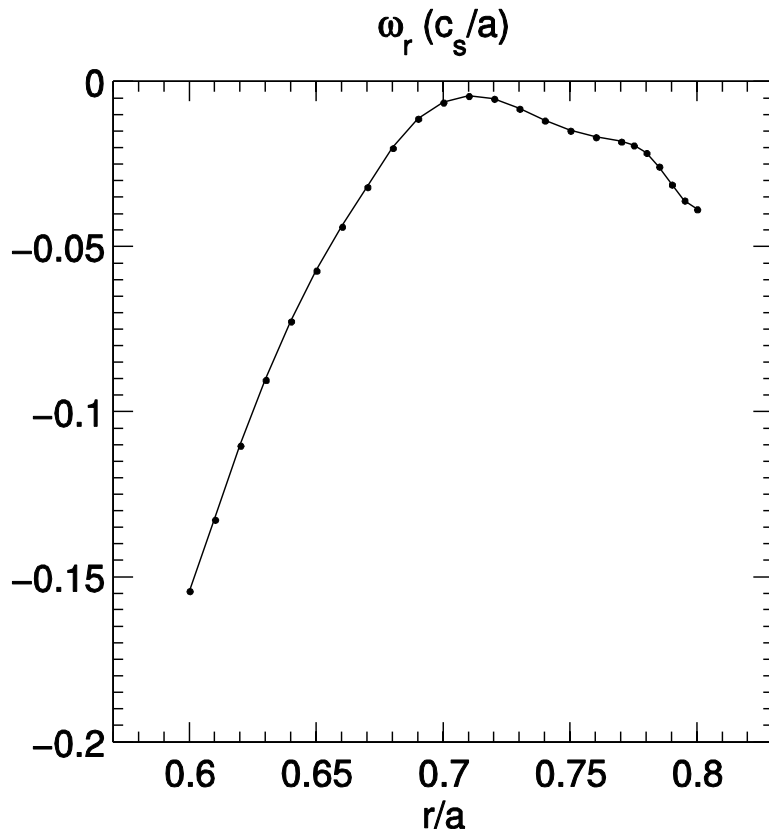
- Comparable momentum flux from D & C ($Z_{\text{eff}} \approx 3$, $n_c m_c \sim 0.7 n_d m_d$)
 - different u , u' dependencies
- Transport contributions come from both φ and B_{\parallel} for these KBM-like modes [Guttenfelder, IAEA TH/6-1]



- Again, little change in growth rates with finite u , u'

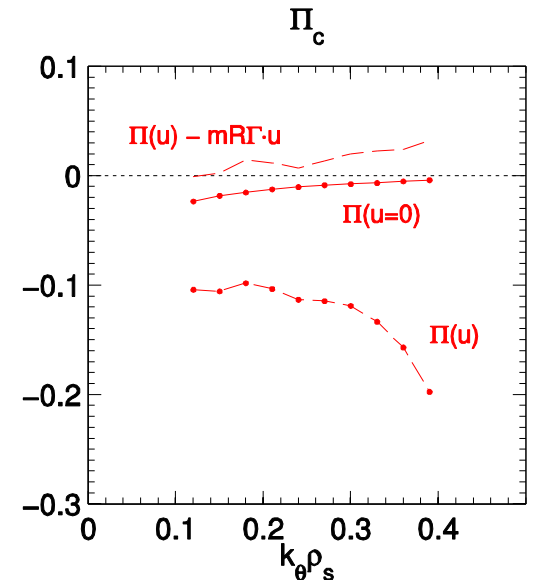
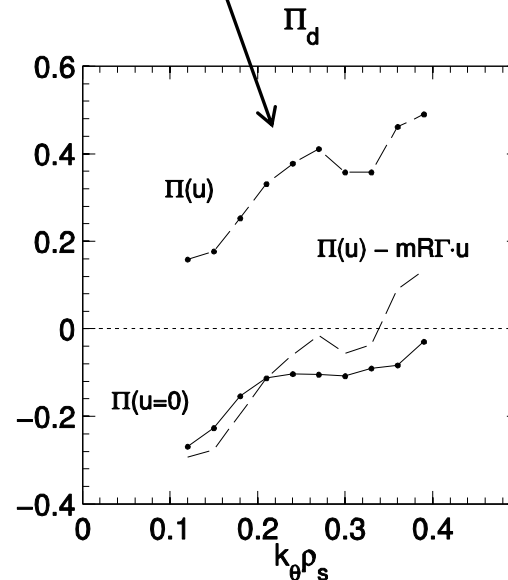
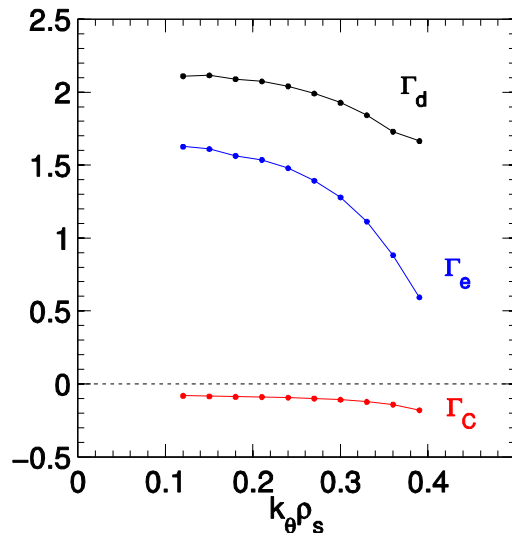
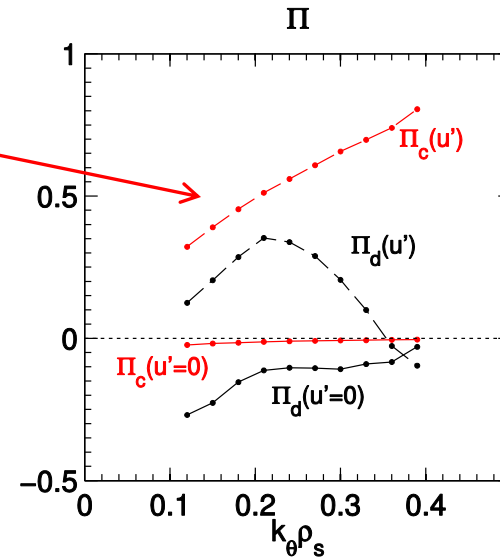
Subdominant ballooning mode unstable across $r/a=0.6-0.8$

- Tracking ballooning root using eigenvalue solver [Belli, Candy 2010]
- $\gamma_E=0.04-0.09 c_s/a$ over this range, always bigger than ballooning mode growth rates – **don't yet know whether this survives nonlinearly**



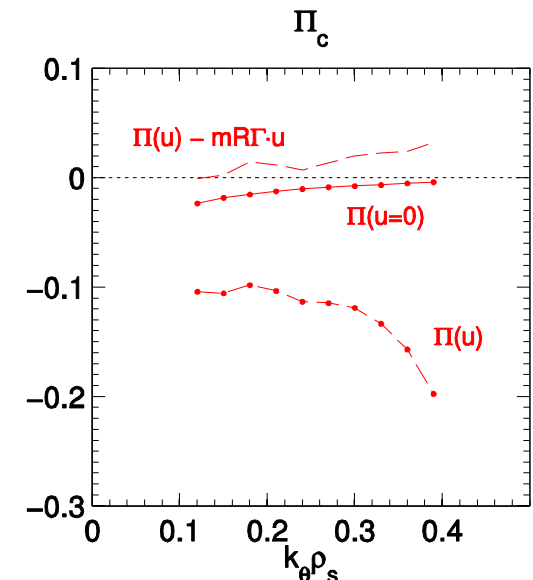
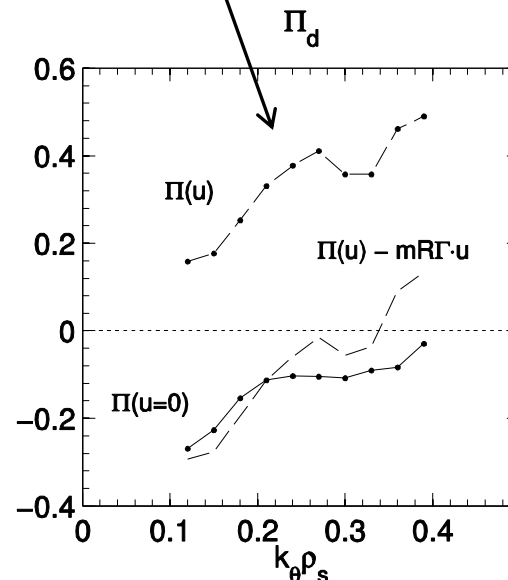
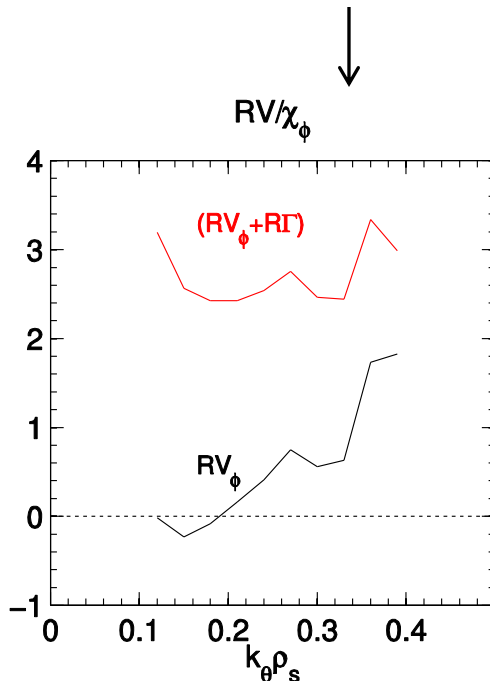
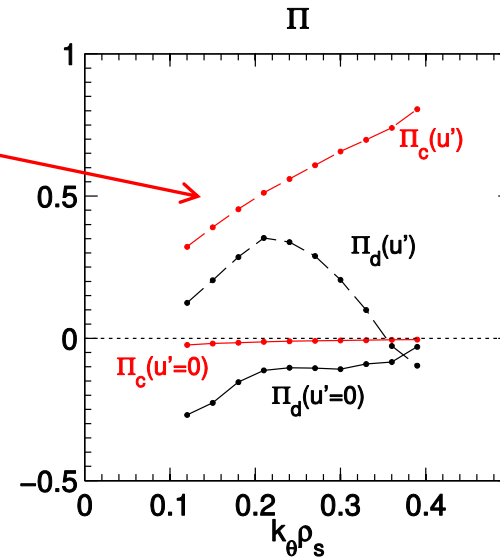
Contribution of particle convection to momentum flux

- Momentum diffusion strongly influenced by carbon
- Momentum convection dominated by deuterium

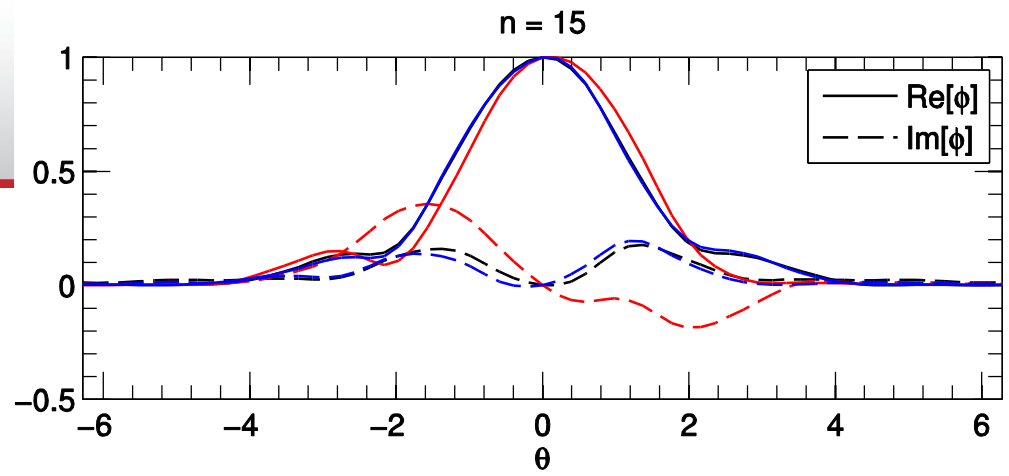


Contribution of particle convection to momentum flux

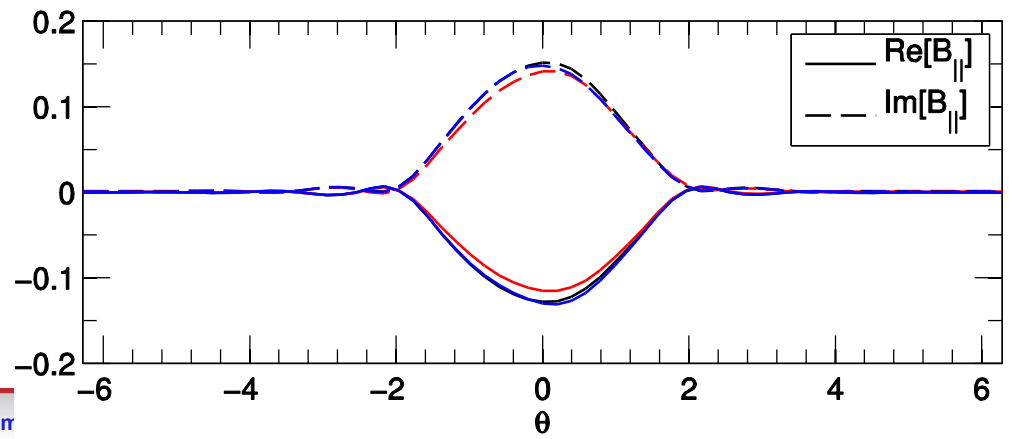
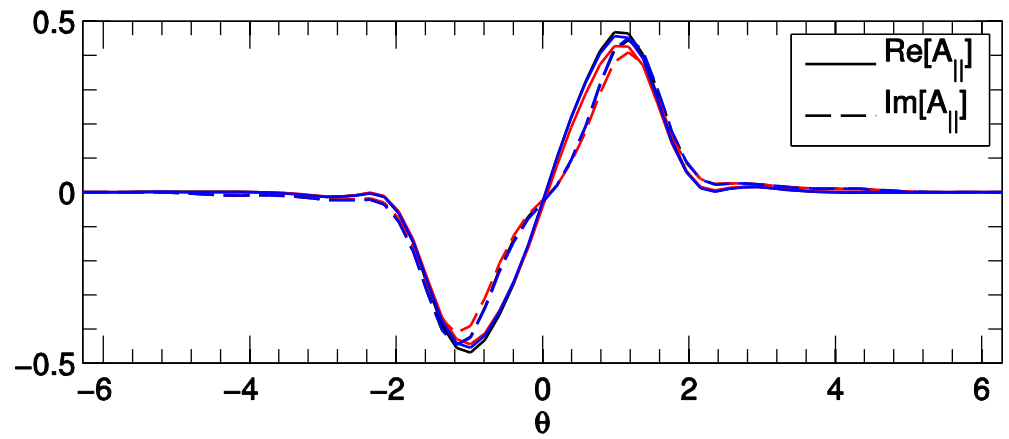
- Momentum diffusion strongly influenced by carbon
- Momentum convection dominated by deuterium
- In this case, deuterium convection ($mR\Gamma \cdot u$) predicted to dominate momentum (Coriolis) pinch



Eigenfunctions



$u=0, \quad u'=0$
 $u=0, \quad u'=0.92$
 $u=0.14, \quad u'=0$



A couple cases show increased ballooning mode growth rates, but always weaker than microtearing

- Higher v_* discharge, all MT
- Lower v_* discharge, much less MT

